

Electrical Engineering

Electronic II , 3<sup>rd</sup> class

- 1- Frequency Response
- 2- Feedback
- 3- Operational Amplifier
- 4- Oscillator
- 5- Active Filter
- 6- Power Amplifier
- 7- Integrated circuit Design
- 8- Integrated circuit Fabrication

## Chapter One :- Frequency Response characteristics.

Frequency Response is a measure of any system output with varying in the frequency of the applied signal.

Decibels: The term decibel has its origin in fact that power and audio levels are related on a logarithmic basis.

$$\log_b a = x \quad \Rightarrow \quad b^x = a$$

$$\text{bel} \Rightarrow G = \log_{10} \frac{P_o}{P_i} \quad \text{Alexander Graham bel}$$

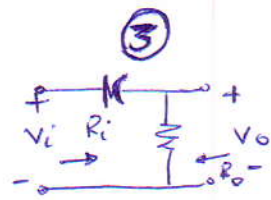
$$1 \text{ bel} = 10 \text{ decibel} = 10 \text{ dB}$$

$$G_{\text{dB}} = 10 \log_{10} \frac{P_o}{P_i} \quad \text{dB}$$

$$G_{\text{dBm}} = 10 \log_{10} \frac{P_o}{1 \text{ mW}} \quad \text{dBm}$$

at  $600 \Omega$  } characteristic impedance of }  
Audio Transmission line }

$$G_{dB} = 10 \log_{10} \frac{P_o}{P_i} = 10 \log_{10} \frac{V_o^2/R_i}{V_i^2/R_i} = 10 \log_{10} \left( \frac{V_o}{V_i} \right)^2 \quad (2)$$

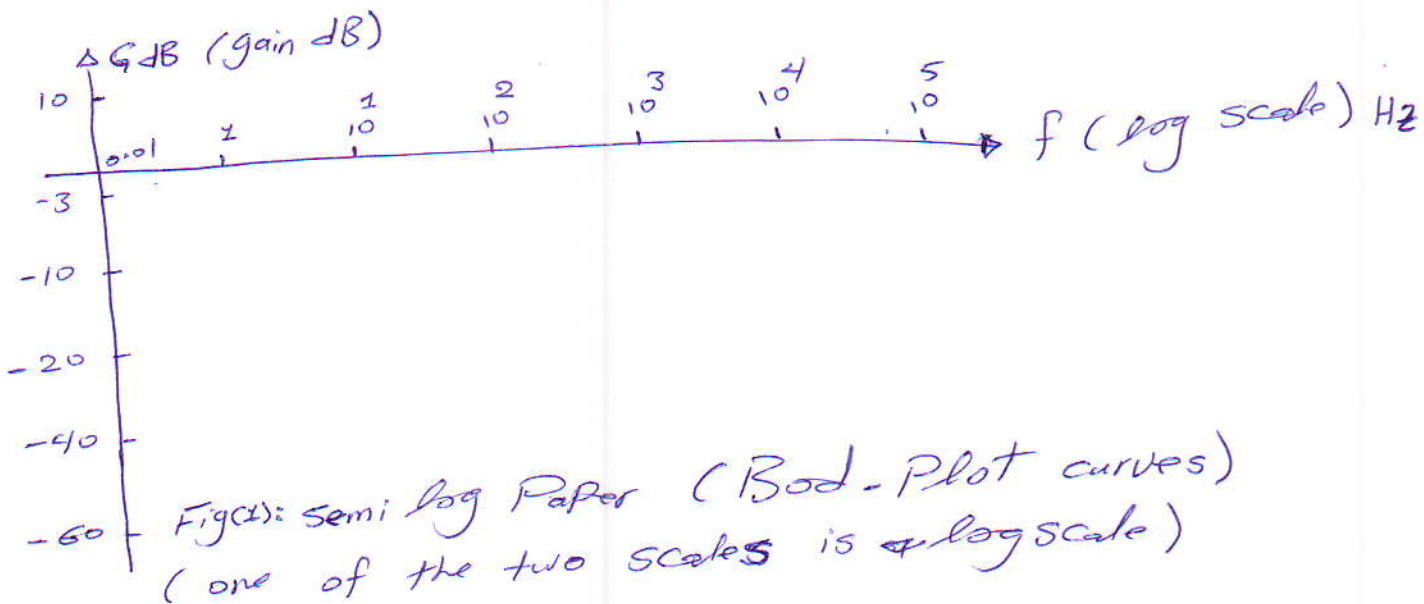


$$\Rightarrow \boxed{G_{dB} = 20 \log_{10} \left| \frac{V_o}{V_i} \right|} \text{ dB}$$

and

$$\boxed{G_{dB} = 20 \log_{10} \left| \frac{I_o}{I_i} \right|} \text{ dB}$$

$$\begin{aligned} \log_{10} 1 &= 0 & ; & \quad \frac{1}{10} = 0.1 \Rightarrow \log_{10} 0.1 = -1 \\ \log_{10} 10 &= 1 & ; & \quad \frac{1}{100} = 0.01 \Rightarrow \log_{10} 0.01 = -2 \\ \log_{10} 100 &= 2 & ; & \quad \frac{1}{1000} = 0.001 \Rightarrow \log_{10} 0.001 = -3 \end{aligned}$$



For a cascade stages:- voltage gain overall is given:

$$A_{or} = A_{v1} \cdot A_{v2} \cdot A_{v3} \dots$$

Applying logarithmic relationship (decibel gain)  $G_{dB}$

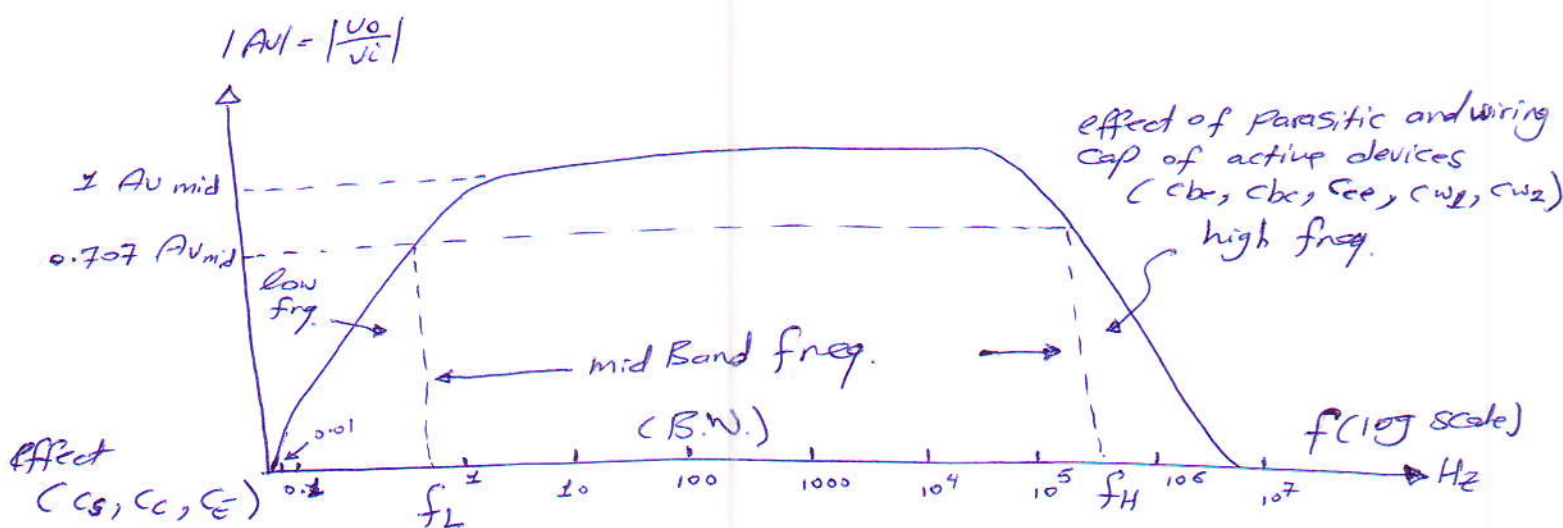
$$G_{dB} = 20 \log_{10} A_{or} = 20 \log_{10} A_{v1} + 20 \log_{10} A_{v2} + \dots$$

$$\boxed{G_v = G_{v1} + G_{v2} + G_{v3} + \dots} \text{ dB} \quad \text{voltage gain of system}$$

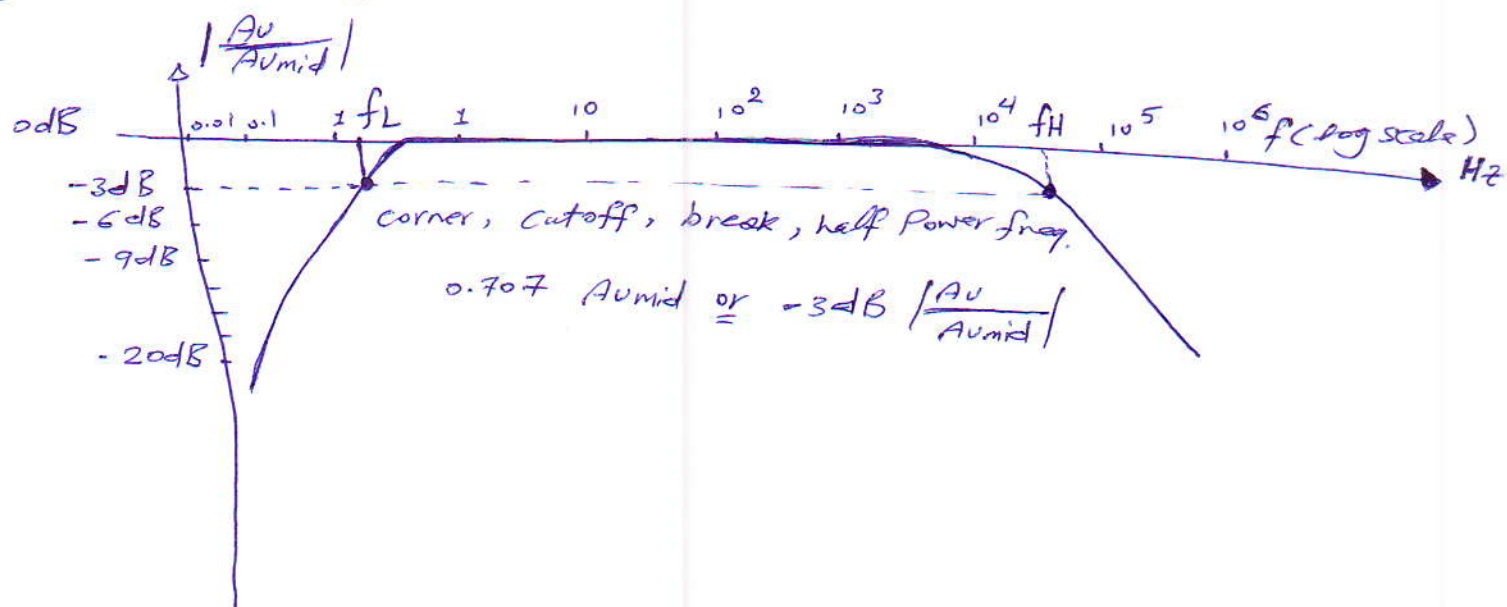
$$\boxed{G_i = G_{i1} + G_{i2} + G_{i3} + \dots} \text{ dB} \quad \text{current gain of system.}$$

\* At a low frequency of the input signal, the reactance of the coupling and by Pass Capacitors ( $C_C, C_E$ ) increase also the impedance to the Passage signal increase causing the gain to be reduced.

\* while at high freq. Component of the input signal, the connection wires capacitances ( $C_{W1}$  and  $C_{W2}$ ) and miller effect Cap. ( $C_{be}, C_{bc}, C_{ce}$ ), the last Cap. can be called Parasitic Cap. All these Cap. will effect on the gain to reduce.



fig(2): Normalized gain versus freq. Plot.



fig(3): Decibel Plot of the normalized gain versus freq. Plot.

(5)

from the Bode plot, the gain decrease at both low and high freq. regions with a midband region where the gain is relatively constant; the two corner frequencies ( $f_L, f_H$ ) define the midband region, the Bandwidth  $(BW = f_H - f_L)$  and extends from  $f_L$  to  $f_H$ .

0.707 was chosen as corner, cutoff, break or half power frequencies to fix the freq. ~~boundaries~~ boundaries of relatively high gain of the midband value and at this ~~low~~ level the output power is half of the midband power output, that is, at this frequencies;

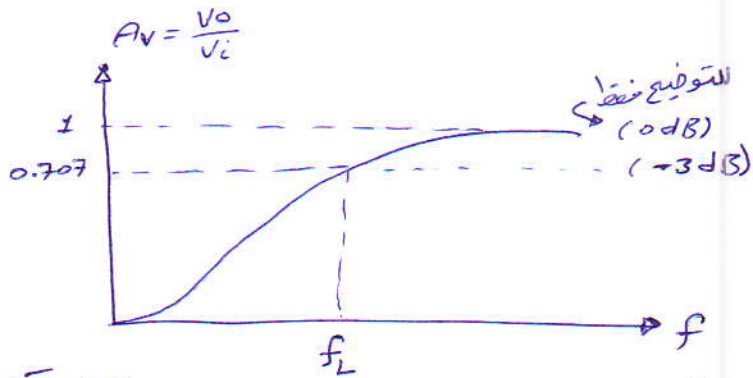
$$P_{mid} = \left| \frac{V_o^2}{R_o} \right| = \left| \frac{(A_{mid} V_i)^2}{R_o} \right|$$

$$\Rightarrow P_{HPF} = \frac{|0.707 A_{mid} V_i|^2}{R_o} = \boxed{\frac{0.5 |A_{mid} V_i|^2}{R_o}}$$

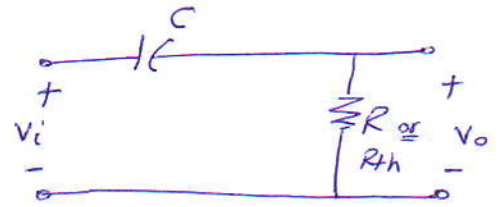
half power freq.

(6)

## \* Low frequency analysis - Bode Plot:



Fig(5): Low freq. response for the RC circuit.



Fig(4): high Pass RC network

$$X_c = \frac{1}{2\pi f C} \quad \therefore A_v = \frac{V_o}{V_i}$$

At high frequencies  $V_o \approx V_i$  ;  $X_c = \frac{1}{2\pi f C} \approx 0 \Omega$  (s.c)

At low frequencies  $V_o = 0$  ;  $X_c = \frac{1}{2\pi(0)C} = \infty$  (o.c)

\* As the freq. increases, the capacitive reactance decreases and more i/p voltage appear across the o/p terminals.

$$V_o = \frac{R_{th} V_i}{R_{th} + X_c} \Rightarrow \frac{V_o}{V_i} = A_v = \frac{R_{th}}{R_{th} + X_c}$$

and the gain magnitude is:

$$|A_v| = \frac{R_{th}}{\sqrt{R_{th}^2 + X_c^2}} = \frac{R_{th}}{\sqrt{2} R_{th}} = \frac{1}{\sqrt{2}} = 0.707 \quad |_{X_c = R_{th} \text{ (special case)}}$$

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at the frequency where  $X_c = R_{th}$ , the output will be 70.7% of the input for the network

$$X_c = \frac{1}{2\pi f_L C} = R_{th} \quad \therefore \boxed{f_L = \frac{1}{2\pi R_{th} C}}$$

In terms of logs :

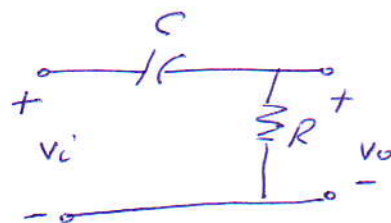
$$G_v = 20 \log_{10} A_v \Rightarrow A_v = \frac{V_o}{V_i} = 0.707 \Rightarrow G_v = 20 \log_{10} \frac{1}{\sqrt{2}} = -3 \text{ dB}$$

while at  $A_v = 1$  or  $V_i = V_o$  (max value)  $\Rightarrow G_v = 20 \log_{10} 1 = 0 \text{ dB}$

that means there is a 3dB drop in gain when  $\boxed{f = f_L}$

In the single transistor amplifier, the cap  $C_s, C_c, C_E$  will effect on the gain at low freq. response

$$A_v = \frac{V_o}{V_i} = \frac{R_{th}}{R_{th} + \frac{1}{j\omega C}} = \frac{1}{1 - j\left(\frac{1}{\omega C R_{th}}\right)} \quad \text{--- ①}$$



$$R_{th} = X_c = \frac{1}{j\omega C} = \frac{1}{j 2\pi f_L C} \quad (\text{special case})$$

$$f_L = \frac{1}{j 2\pi R_{th} C} \quad (\text{From above}) \text{ and subs in equation ①}$$

and we get:

$$\boxed{A_v = \frac{1}{1 - j \frac{f_L}{f}}}$$

In the magnitude and Phase form:

$$A_v = \frac{V_o}{V_i} = \frac{1}{\sqrt{1+(f_L/f)^2}} \left[ \tan^{-1}\left(\frac{f_L}{f}\right) \right]$$

If  $f = f_L \Rightarrow |A_v| = \frac{1}{\sqrt{2}} = 0.707 = -3\text{dB}$  (cutoff)

If  $f \gg f_L \Rightarrow |A_v| = 1 = 0\text{dB}$  (midband)

If  $f \ll f_L$  Ignore

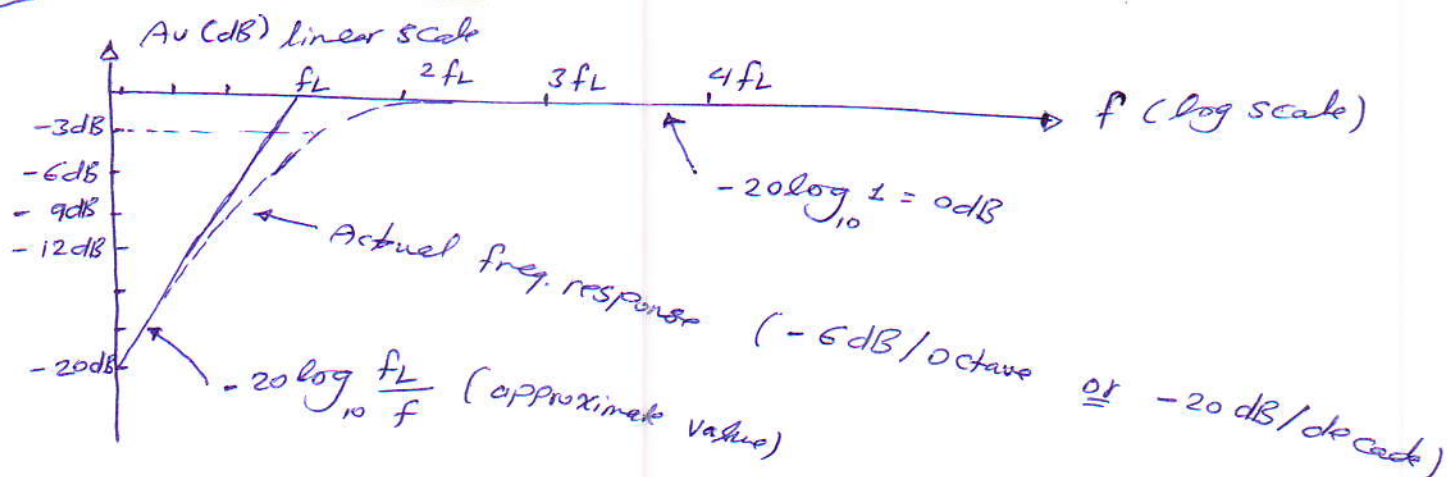
$$A_{v\text{dB}} = 20 \log_{10} \frac{1}{\sqrt{1+(f_L/f)^2}}$$

$$\Rightarrow A_{v\text{dB}} = 20 \log_{10} \left[ 1 + \left(\frac{f_L}{f}\right)^2 \right]^{-\frac{1}{2}}$$

$$\therefore A_{v\text{dB}} = \left[ -10 \log_{10} \left[ 1 + \left(\frac{f_L}{f}\right)^2 \right] \right] \text{ actual equation for gain value}$$

or for the frequencies  $f \ll f_L$  or  $\left(\frac{f_L}{f}\right)^2 \gg 1$  the equation above can be approximated by

$$A_{v\text{dB}} = -20 \log_{10} \frac{f_L}{f} \text{ APPROXIMATE gain value}$$



Fig(6): Bode Plot for low freq. region.

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## \* Low Frequency Response - BJT Amplifier 30

The analysis of this section will employ the loaded voltage divider BJT bias configuration, but the result can be applied to any BJT.

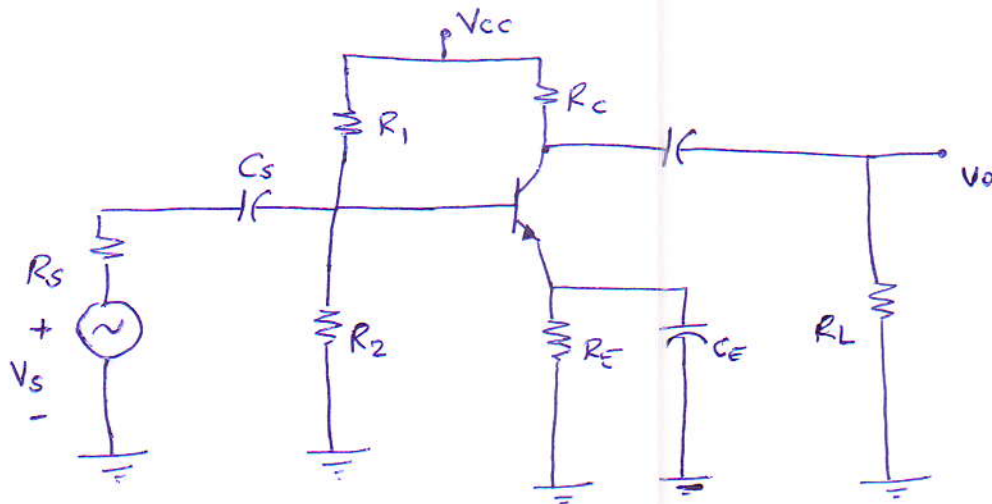


Fig (7) : BJT amplifier network

$$f_L = \frac{1}{2\pi R_{th} C}$$

① Effect of  $C_s$  :

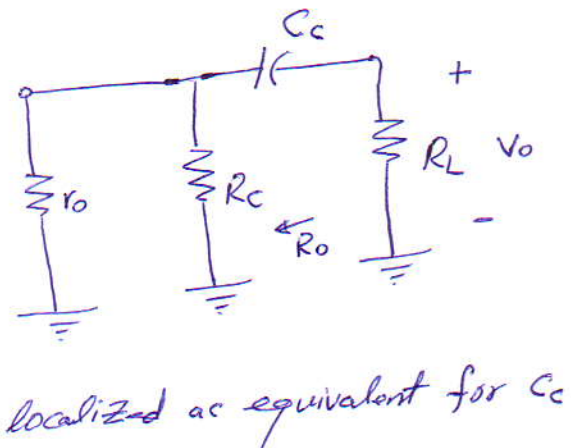
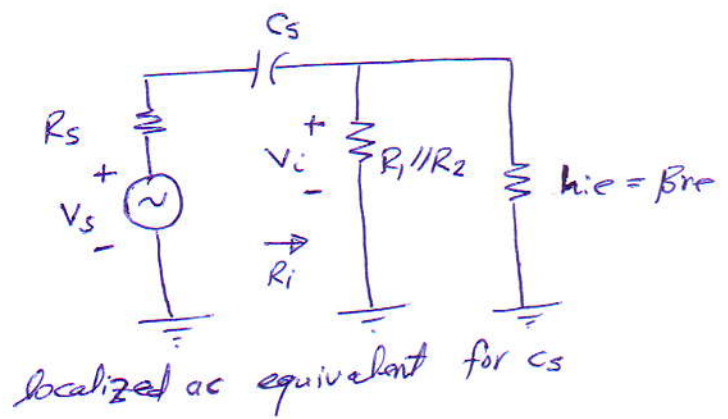
$$f_{Ls} = \frac{1}{2\pi (R_s + R_i) C_s}$$

$$R_i = R_1 \parallel R_2 \parallel \beta r_e$$

② Effect of  $C_c$  :

$$f_{Lc} = \frac{1}{2\pi (R_o + R_L) C_c}$$

$$R_o = R_c \parallel r_o$$

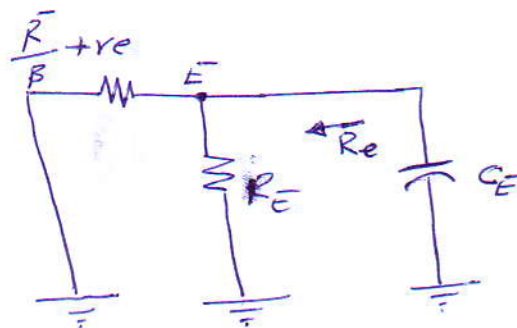


③ Effect of  $C_E$ :

$$f_{L_E} = \frac{1}{2\pi R_E C_E}$$

$$R_E = R_E \parallel \frac{\bar{R}_S}{\beta} + r_e$$

where  $\bar{R}_S = R_S \parallel R_1 \parallel R_2$



Ex: ① Determine the lower cutoff freq. for the network of fig (7) using the following Parameters:

$$C_S = 10 \mu F, C_E = 20 \mu F, C_C = 1 \mu F$$

$$R_S = 1 k\Omega, R_1 = 40 k\Omega, R_2 = 10 k\Omega, R_E = 2 k\Omega, R_C = 4 k\Omega$$

$$R_L = 2.2 k\Omega, \beta = 100, r_o = \infty, V_{CC} = 20 V$$

② Sketch the freq. response using a bode Plot



Solution:

① To determine  $r_e$  for dc conditions, we first apply the test equation:

$$\beta R_E = (100)(2k) = 200k \gg 10R_2 = 100k\Omega$$

∴ approximate analysis can be applied.

Since

$$V_B = \frac{R_2 V_{CC}}{R_2 + R_1} = \frac{10k(20)}{10k + 40k} = 4V$$

$$I_E = \frac{V_E}{R_E} = \frac{V_B - V_{BE}}{R_E} = \frac{4 - 0.7}{2k} = 1.65 mA$$

$$r_e = \frac{26mV}{I_E} = \frac{26mV}{1.65mA} \approx 15.76 \Omega$$

(11)

$$\beta_{re} = (100)(15.76) = 1576 = 1.576k\Omega$$

midband gain

$$A_v = \frac{V_o}{V_i} \approx \frac{-R_c \parallel R_L}{r_e} = \frac{(4k) \parallel (2.2k)}{15.76} \approx -90$$

The input impedance  $Z_i = R_i = R_1 \parallel R_2 \parallel \beta_{re} = 40k \parallel 10k \parallel 1.576k = 1.32k\Omega$ 

$$\text{overall gain} = \frac{V_o}{V_s} = \frac{V_o}{V_i} \cdot \frac{V_i}{V_s} = (-90) \left( \frac{R_i}{R_i + R_s} \right) = (-90)(0.569) \\ = -51.21$$

$$f_{L_s} = \frac{1}{2\pi (R_s + R_i) C_s} = \frac{1}{(6.28)(1k + 1.32k)(10\mu)} \approx 6.86 \text{ Hz}$$

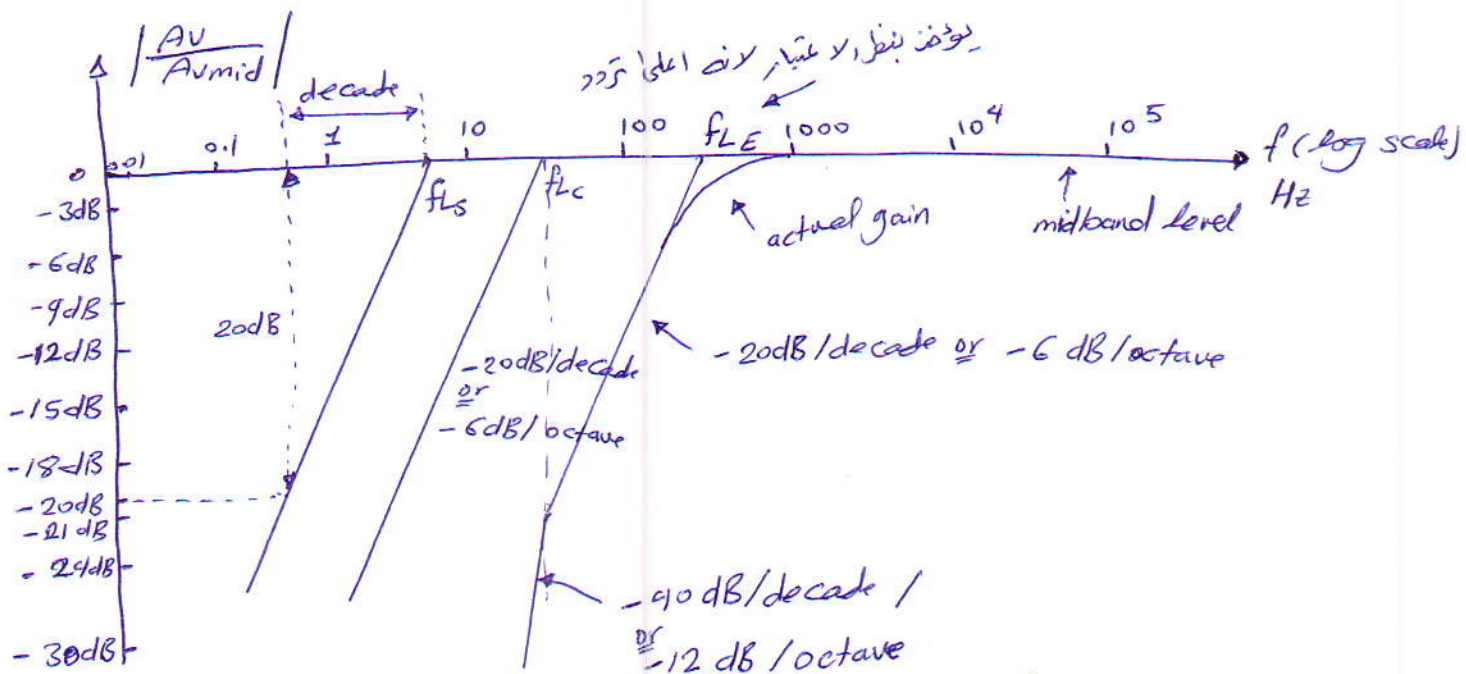
$$f_{L_c} = \frac{1}{2\pi (R_c + R_L) C_c} = \frac{1}{(6.28)(4k + 2.2k)(1\mu)} = 25.68 \text{ Hz}$$

$$R_s^- = R_s \parallel R_1 \parallel R_2 = 1k \parallel 40k \parallel 10k \approx 0.889k\Omega$$

$$R_e = R_E \parallel \left( \frac{R_s^-}{\beta} + r_e \right) = 2k \parallel \left( \frac{0.889k}{100} + 15.76 \right) \approx 24.35\Omega$$

$$\therefore f_{L_E} = \frac{1}{2\pi R_e C_E} = \frac{1}{(6.28)(24.35)(20\mu)} = 327 \text{ Hz}$$

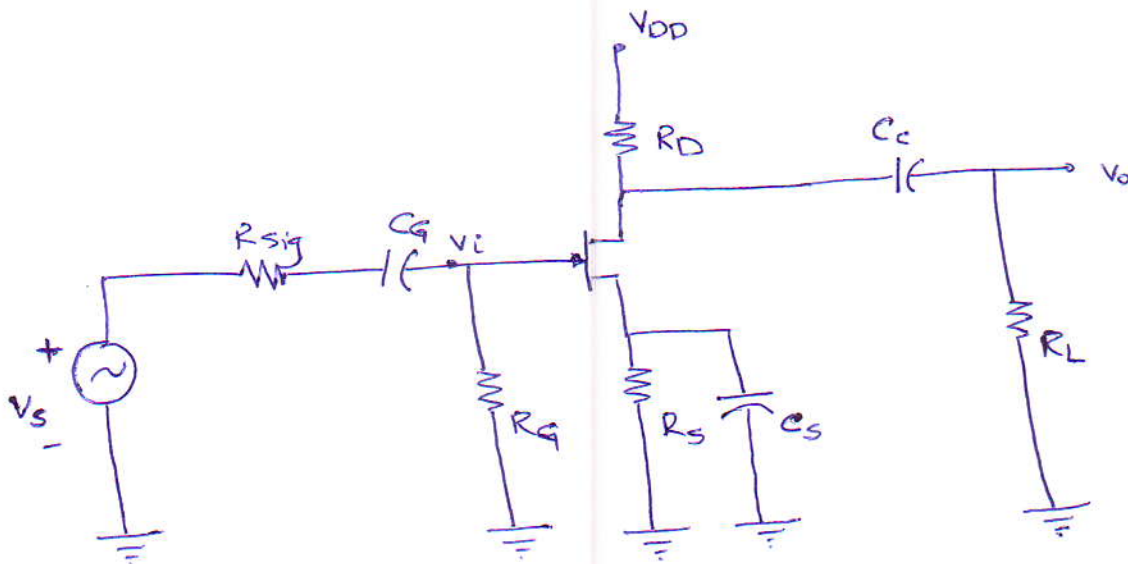
(b)



Fig(8): Low freq. response Plot.

## \* Low Frequency Response - FET Amplifier:

The analysis of the amplifier in the low freq. region will be quite similar to that of the BJT amplifier as follow:



Fig(9): FET amplifier Network.

$$f_L = \frac{1}{2\pi R_{th} C}$$

① Effect of  $C_G$ :

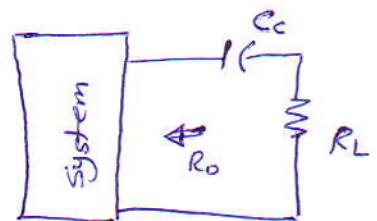
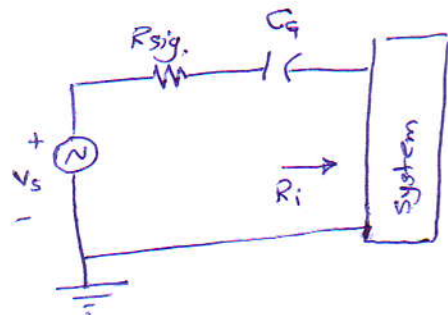
$$f_{LG} = \frac{1}{2\pi (R_{sig} + R_i) C_G}$$

$$R_i = R_G$$

② Effect of  $C_C$ :

$$f_{LC} = \frac{1}{2\pi (R_o + R_L) C_C}$$

$$R_o = R_D // r_d$$



③ Effect of  $C_s$ :

$$f_{Ls} = \frac{1}{2\pi R_{eq} C_s}$$

$$R_{eq} = \frac{R_s}{1 + R_s(1 + g_m r_d) / (r_d + R_D \parallel R_L)}$$

which for  $r_d \approx \infty \Omega$  becomes

$$R_{eq} = R_s \parallel \frac{1}{g_m}$$



Ex:-

(a) Determine the lower cutoff freq. for the network of fig(9) using the following Parameter

$$C_g = 0.01 \mu F, C_c = 0.5 \mu F, C_s = 2 \mu F$$

$$R_{sig} = 10 k\Omega, R_G = 1 M\Omega, R_D = 4.7 k\Omega, R_s = 1 k\Omega, R_L = 2.2 k\Omega$$

$$I_{DSS} = 8 mA, V_p = -4 V, r_d = \infty \Omega, V_{DD} = 20 V$$

(b) Sketch the freq. response using a Bode Plot.

Solution:-

① To find  $g_m$  value must be return to DC analysis

$$I_D = I_{DSS} \left(1 - \frac{V_{GS}}{V_p}\right)^2$$

to be continue.

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$$V_{GS} = V_G - V_S$$

$$= V_G - V_S$$

$$= -V_S \Rightarrow V_G = -I_D R_S$$

$$\text{for } I_D = 0 \Rightarrow V_{GS} = 0V$$

$$I_D = 2mA \Rightarrow V_{GS} = -2V$$

$$g_{m0} = \frac{2I_{DSS}}{|V_P|} = \frac{2(8mA)}{4} = 4mS$$

$$g_m = g_{m0} \left(1 - \frac{V_{GSQ}}{V_P}\right) = 4mS \left(1 - \frac{-2}{-4}\right) = 2mS$$

$$f_{L_G} = \frac{1}{2\pi(R_{sig} + R_i)C_G} = \frac{1}{(6.28)(10k + 1M)(0.01\mu)} \approx 15.8Hz$$

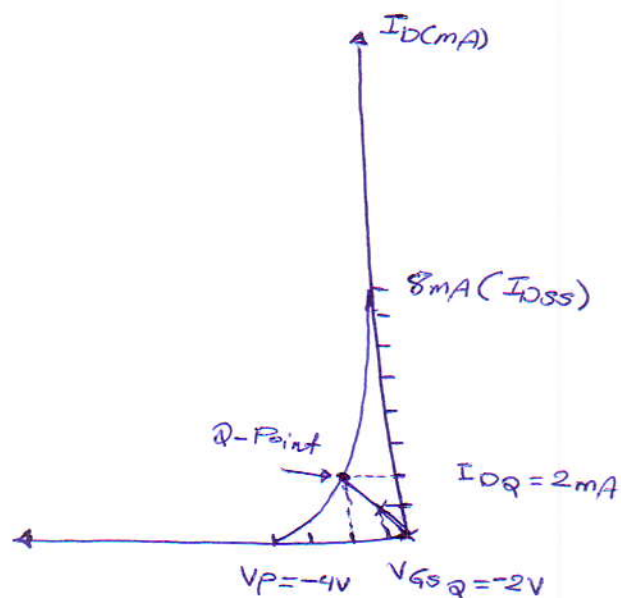
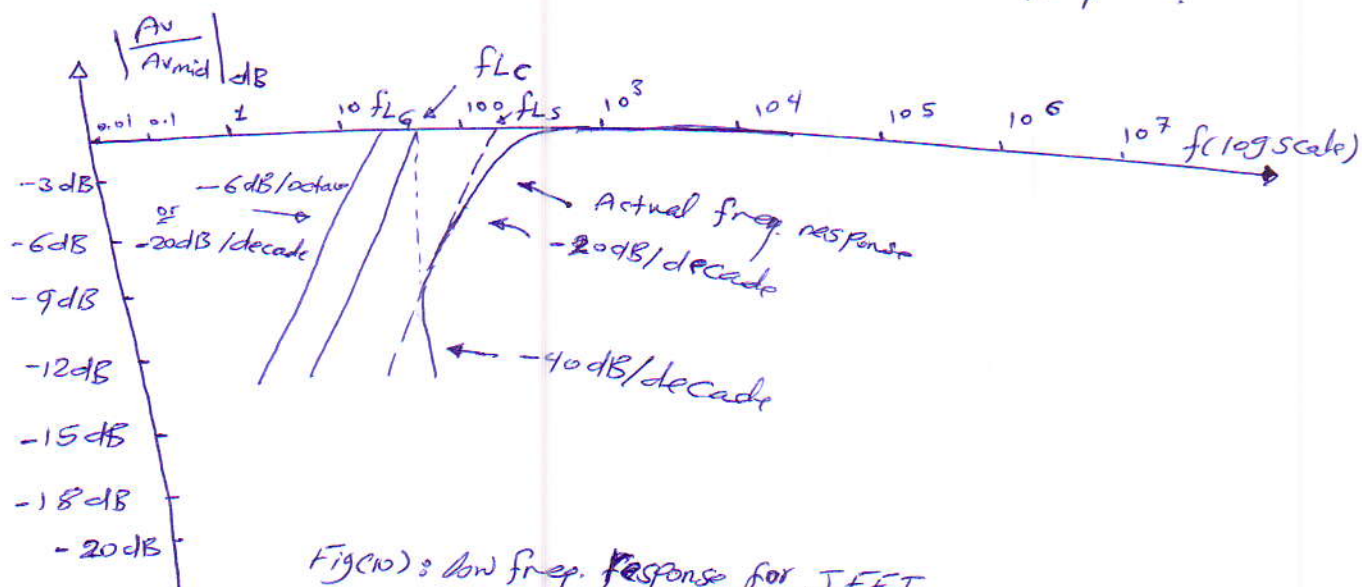
$$f_{L_C} = \frac{1}{2\pi(R_O + R_L)C_C} = \frac{1}{(6.28)(4.7k + 2.2k)(0.5\mu)} \approx 46.13Hz$$

$$R_{eq} = R_S \parallel \frac{1}{g_m} = 1k \parallel \frac{1}{2m} = 333.33\Omega$$

$$f_{L_S} = \frac{1}{2\pi R_{eq} C_S} = \frac{1}{(6.28)(333.33)(2\mu)} = 238.73Hz$$

(التردد المنخفض هو الذي يحدد)  
low freq. لا يحدد

(b)



## \* Miller Effect Capacitance :

At the high freq. of the i/p signal two factors will define the -3dB Point, the network capacitance (Parasitic of the P-N Junction and introduce wiring capacitance) to be considered as discrete components between the external lozets of the transistor or system.

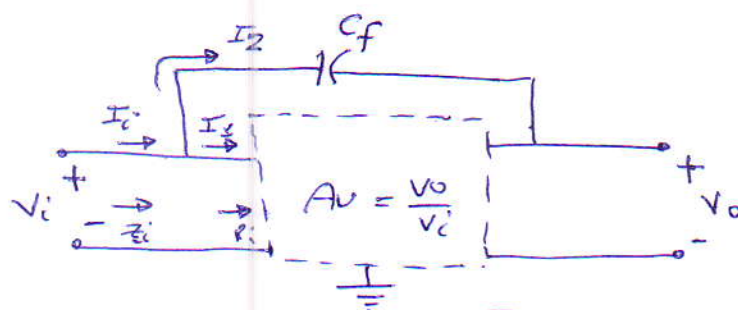


Fig (14): Network employed for the Miller input capacitance

$$C_{Mi} = (1 + |A_v|) C_f$$

$C_f$  : feedback capacitance

and can be represented by the network in fig (15)

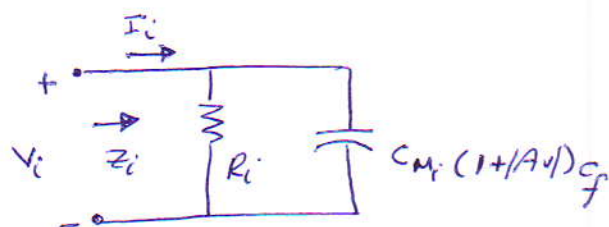


Fig (15)

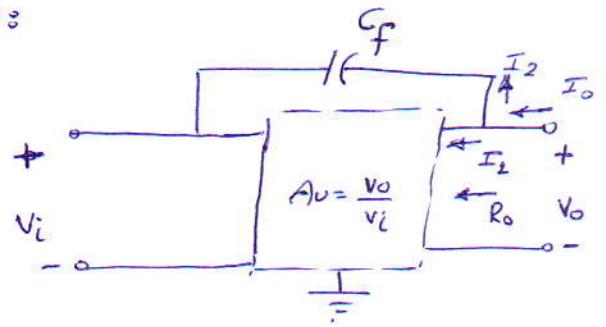
For any inverting amplifier, the input cap. will be increased by a Miller effect cap sensitive to the gain of the amplifier and Parasitic (electrode) capacitance between the i/p and o/p terminals of the active device.

The resistance  $R_o$  is usually sufficiently large and can be represented the Miller o/p capacitance as follow:

$$C_{M_o} = (1 + | \frac{1}{A_v} |) C_f$$

for  $A_v \gg 1$

$$\Rightarrow C_{M_o} = C_f$$

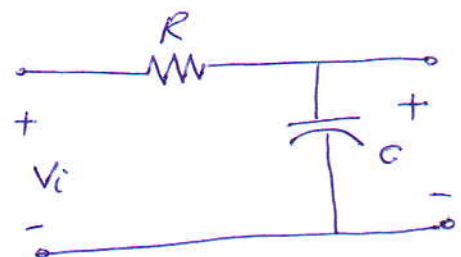
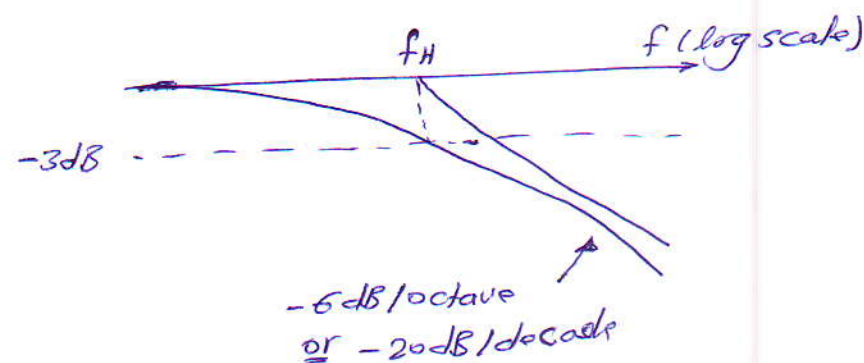


Fig(13): Network employed for the Miller output capacitance

### \* High frequency Response - BJT Amplifier:

At the high freq. end, there are two factors that define -3dB cutoff Point, the network cap. (Parasitic cap and introduce wiring cap), and the freq. dependent of  $h_{fe}(\beta)$ .

In the high freq. region, the RC network concern has the configuration appearing in fig (14):



Fig(14): RC combination that will define a high-cutoff freq.

\* when the i/p signal freq. increase, the reactance  $X_C$  decrease in magnitude, resulting in a short effect across the o/p and a decrease in gain.

where

$$V_o = V_i \frac{X_C}{X_C + R} \quad (\text{from fig(14)})$$

$$= V_i \frac{\frac{1}{j\omega C}}{\frac{1}{j\omega C} + R} = \frac{V_i \frac{1}{j\omega C}}{\frac{1 + j\omega R C}{j\omega C}} = V_i \frac{1}{1 + j\omega R C}$$

and at  $R = \frac{1}{2\pi f_H C}$  (special case)

we get:

$$A_v = \frac{V_o}{V_i} = \frac{1}{1 + j \frac{f}{f_H}}$$

and the magnitude  $|A_v| = \frac{1}{\sqrt{1 + \left(\frac{f}{f_H}\right)^2}}$

$$|A_v|_{dB} = -10 \log_{10} \left[ 1 + \left(\frac{f}{f_H}\right)^2 \right]$$

Actual gain value

or

$$|A_v|_{dB} \approx -20 \log_{10} \left( \frac{f}{f_H} \right)$$

Approximation gain value

The various Parasitic capacitances ( $C_{be}$ ,  $C_{bc}$ ,  $C_{ce}$ ) of the transistor in fig(15) are included with wiring cap. ( $C_{wi}$ ,  $C_{wo}$ ) introduced during construction, not the absence of the cap.  $C_s$ ,  $C_E$ , and  $C_c$  which are all assumed to be in the short circuit state at these frequencies.

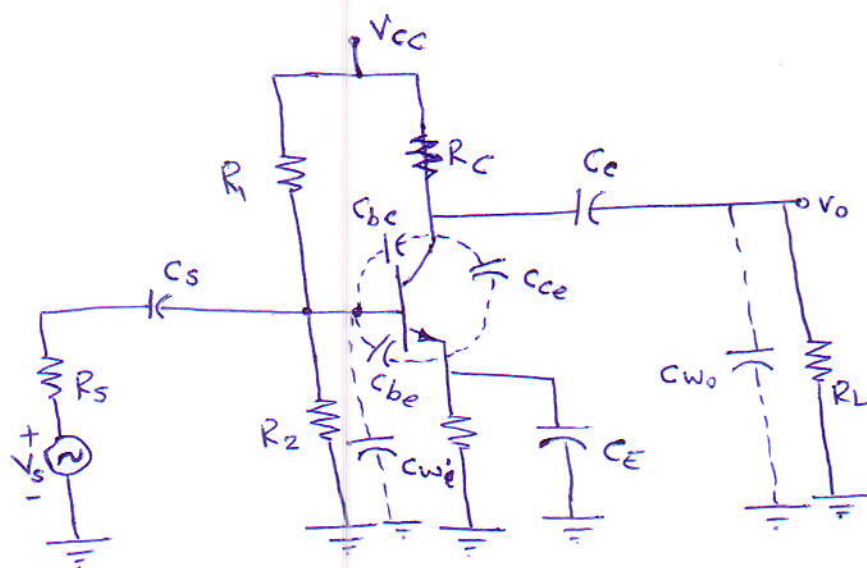
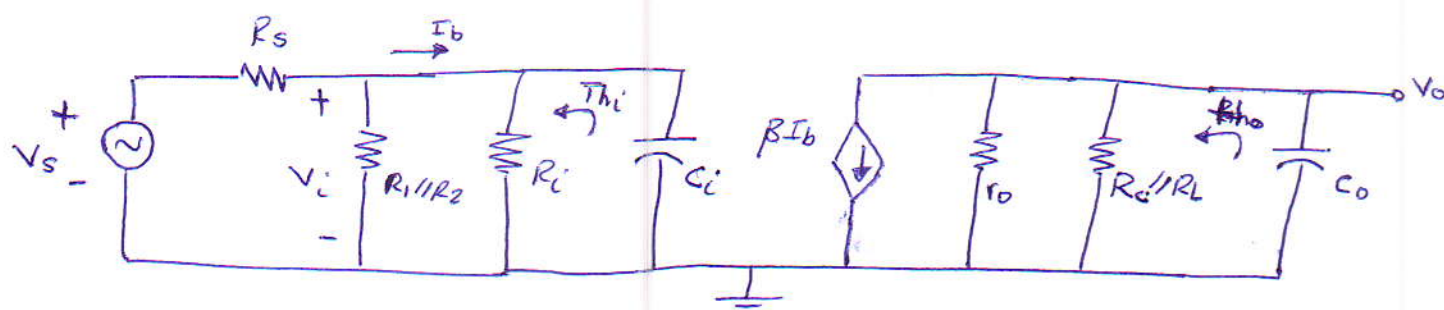


Fig (15): BJT network with capacitor that effect the high frequency response



High-freq. ac equivalent for network above.

$$C_i = C_{wi} + C_{be} + C_{mi}$$

$$C_o = C_{wo} + C_{ce} + C_{mo}$$

$$R_{thi} = R_s // R_1 // R_2 // R_i$$

$$R_{tho} = R_c // R_L // r_o$$

to be continue

$$\Rightarrow C_i = C_{wi} + C_{be} + C_{Mi} = \boxed{C_{wi} + C_{be} + (1 + |A_v|) C_{bc}}$$

At very high freq., the effect of  $C_i$  is to reduce the total impedance of the Parallel combination of  $R_1$ ,  $R_2$ ,  $R_i$  and  $C_i$ . The result is a reduced level of voltage across  $C_i$ , a reduction in  $I_b$  and a gain for the system.

$$\boxed{f_{H_o} = \frac{1}{2\pi R_{tho} C_o}} \quad \text{and} \quad \boxed{f_{Hi} = \frac{1}{2\pi R_{thi} C_i}}$$

$$\Rightarrow C_o = C_{wo} + C_{ce} + C_{Mo} = \boxed{C_{wo} + C_{ce} + (1 + |1/A_v|) C_{bc}}$$

for a large  $A_v$ :  $1 \gg \frac{1}{A_v}$

we get

$$\boxed{C_o \approx C_{wo} + C_{ce} + C_{bc}}$$

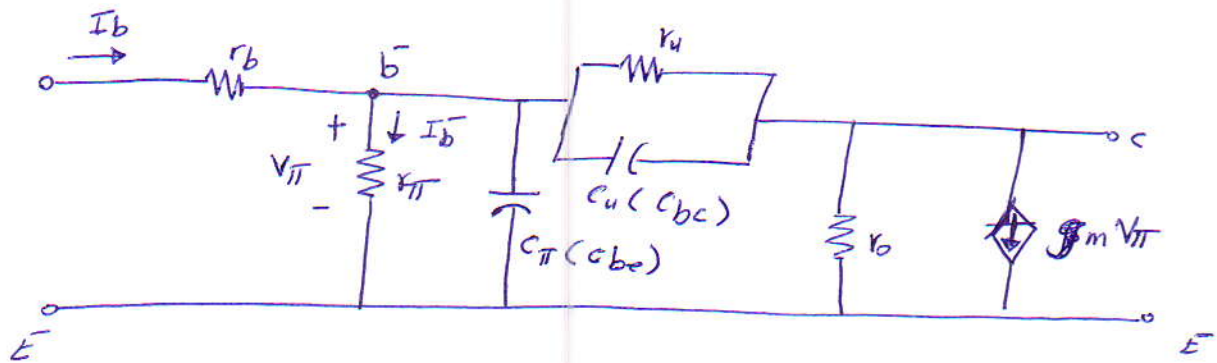
\* (يُوضَحُ لِنَبْطِزِ الإِعْتِبَارِ التَّرْدَدَ الْأَقْلَ فِيمَا دُرِجَاتِ التَّيَّ سَوَافَ تَسْتَنْجِعُ فِي السُّؤَالِ صِبْ أَمِ التَّرْدَدِ الْأَقْلَ هُوَ الْمَذْكُورُ تَأْثِيرًا عَلَى رَاسِخَاتِهِ).

### \* $h_{fe}$ or $\beta$ Variation :

The variation of  $h_{fe}$  (or  $\beta$ ) with frequency will approach, with some degree of accuracy, the following relationship:

$$h_{fe} = \frac{h_{fe \text{ mid}}}{1 + j \left( \frac{f}{f_{\beta}} \right)}$$

The fig(16) below will appear the variation parameters which are appearing in the high freq. effect on the  $h_{fe}$  or  $\beta$



Fig(16): High freq. transistor small-signal ac equivalent circuit.

$$g_m V_{\pi} = g_m (I_b r_{\pi}) = \frac{1}{r_e} (I_b \beta r_e) = \boxed{\beta I_b}$$

$r_b$ : includes the base contact, base bulk and base spreading resistance levels

$C_{\pi}$  is larger than  $C_u$

$r_{\pi}$ : is simply  $\beta r_e$  as introduced for the common emitter  $r_e$  model.

$r_u$ : is a very large resistance and provides a feedback path from the output to input in the equivalent model. (usually quite large  $\gg \beta r_o$ ).

$$r_{\pi} = \beta_{re} = h_{fe \text{ mid } re}$$

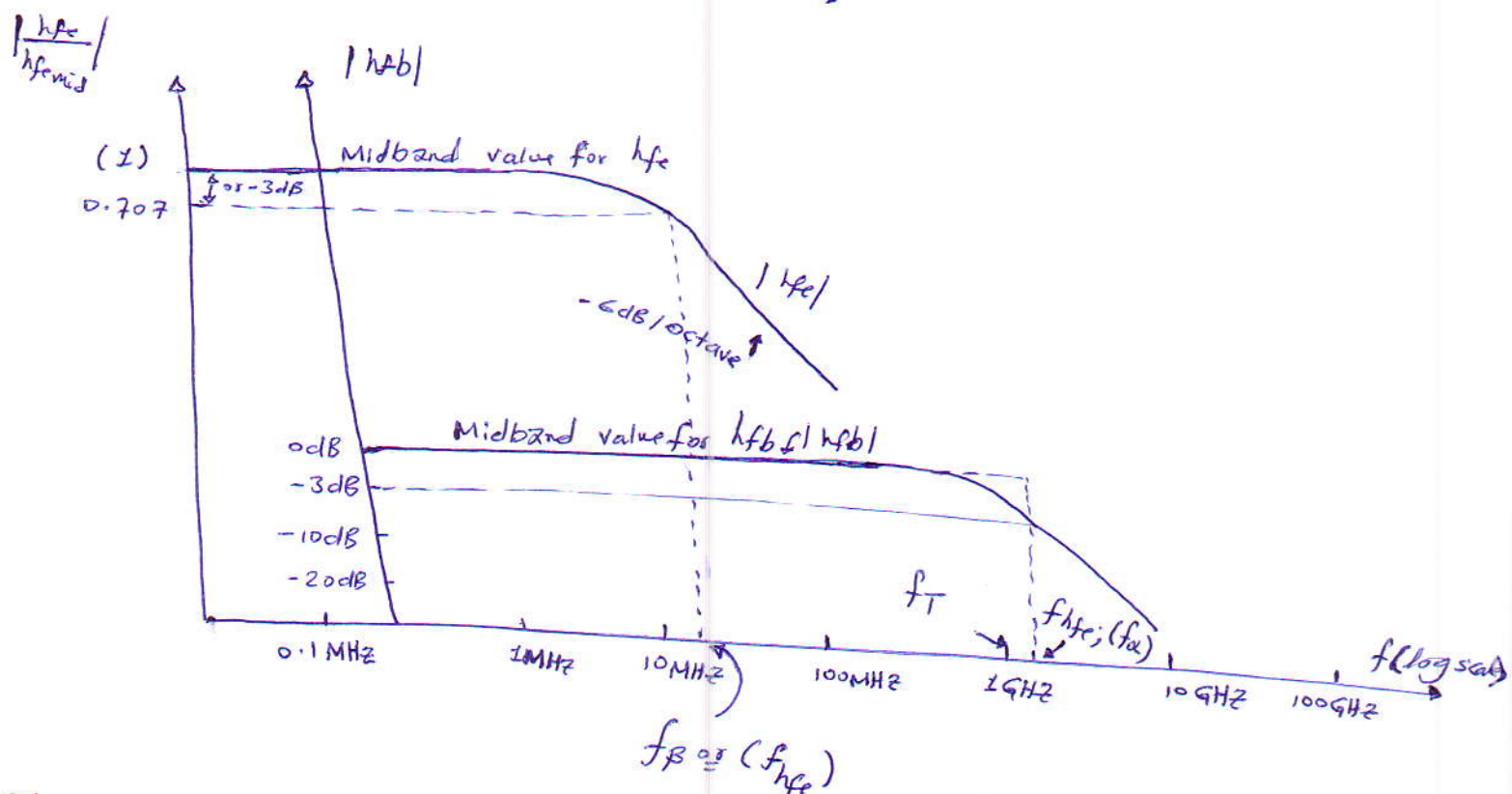
$$f_{\beta} \text{ (Sometimes appearing as } h_{fe}) = \frac{1}{2\pi r_{\pi} (C_{\pi} + C_{\mu})}$$

$$f_{\beta} = \frac{1}{h_{fe \text{ mid}}} \frac{1}{2\pi r_{e} (C_{\pi} + C_{\mu})}$$

$$\text{and } f_{\beta} \approx \frac{1}{2\pi \beta_{\text{mid } re} (C_{\pi} + C_{\mu})}$$

\* When we are comparing the  $h_{fe}$  values in the high freq. response with the  $h_{fb}$  (for common base configuration) or called ( $\alpha$ ). Note the small change in  $h_{fb}$  for the chosen freq. range and the CB configuration displays improved high-freq. chara. over the CE conf. and also the absence of the Miller effect cap due to the noninverting characteristics of the CB config. as shown in fig(17):

(نلاحظ أن  $h_{fb}$  في الترتيب المشترك القاعدة لا تتغير كثيراً مع التردد وهذا سيجعلنا نلاحظ أن  $h_{fb}$  في الترتيب المشترك القاعدة أفضل من  $h_{fe}$  في الترتيب المشترك الإصدار في الترددات العالية)



Fig(17):  $h_{fe}$  and  $h_{fb}$  versus frequency in the high-frequency region

The following equation permits a direct conversion for determining  $f_\beta$  if  $f_\alpha$  and  $\alpha$  are specified

$$f_\beta = f_\alpha (1 - \alpha)$$

عادة قيم  $\alpha$  (0.99) وبالتالي تقريباً  $f_\beta = 0.01 f_\alpha$   
ويمكن ملاحظة هنا لا مفر من (17) في المعادلة السابقة

~~~~~

A quantity called the gain-bandwidth Product is defined for the transistor by the condition

$$\left| \frac{h_{fe}(mid)}{1 + j \left( \frac{f}{f_\beta} \right)} \right| = 1$$

where

$$|h_{fe}|_{dB} = 20 \log_{10} \left| \frac{h_{fe}(mid)}{1 + j \left( \frac{f}{f_\beta} \right)} \right| = 20 \log_{10} 1 = 0 \text{ dB}$$

$$f_T \approx h_{fe}(mid) f_\beta$$

$f_\beta$  is approximate a bandwidth (BW) when we ignore a lower cutoff freq.

(gain-bandwidth Product)

وهو قيمته عند التردد المنخفض قريباً في حالة  $f_\beta$ ، لترانستور يعمل في حالة CB  
وتلك بيني آخر تردد يعمل فيه الترانزستور

$$\text{or } f_T = \beta_{mid} f_\beta$$

and

$$f_\beta = \frac{f_T}{\beta_{mid}}$$

عندها يكون الكسب (واحد)  $0 \text{ dB}$   
 $|h_{fe}| = 1$

$$\Rightarrow f_T = \beta_{mid} \frac{1}{2\pi \beta_{mid} r_e (C_\pi + C_\mu)}$$

$$\therefore f_T = \frac{1}{2\pi r_e (C_\pi + C_\mu)}$$

Ex: For the common emitter - voltage divider with the Parameter as follow:

$$R_s = 1k\Omega, R_1 = 40k\Omega, R_2 = 10k\Omega, R_E = 2k\Omega, R_C = 4k\Omega, R_L = 2.2k\Omega$$

$$C_s = 10\mu F, C_c = 1\mu F, C_E = 20\mu F, \beta = 100, r_o = \infty, V_{CC} = 20V$$

with the addition of

$$C_{\pi} (C_{be}) = 36PF, C_{\mu} (C_{bc}) = 4PF, C_{ce} = 1PF, C_{wi} = 6PF \text{ and } C_{wo} = 8PF.$$

② Determine  $f_{Hi}$  and  $f_{Ho}$ .

① Find  $f_B$  and  $f_T$

③ sketch the freq. response for the low and high freq. regions.

~~~~~

Solution: ①

$$R_i = 1.32k\Omega, A_{v_{mid}} = -90 \text{ and } R_{thi} = R_s // R_1 // R_2 // R_i$$

$$= 1k // 40k // 10k // 1.32k \approx 0.531k\Omega$$

$$\text{and } C_i = C_{wi} + C_{be} + (1 - A_v) C_{bc}$$

$$= 6p + 36p + (1 - (-90)) 4p = 406PF$$

$$f_{Hi} = \frac{1}{2\pi R_{thi} C_i} = \frac{1}{2\pi (0.531k)(406p)} = 738.24kHz$$

to be continue

(a)

(24)

$$R_{tho} = R_C // R_L = 4k // 2.2k = 1.419k\Omega$$

$$C_o = C_{w_o} + C_{ce} + C_{M_o} = 8p + 1p + \left(1 - \frac{1}{-90}\right) 4p = 13.04pF$$

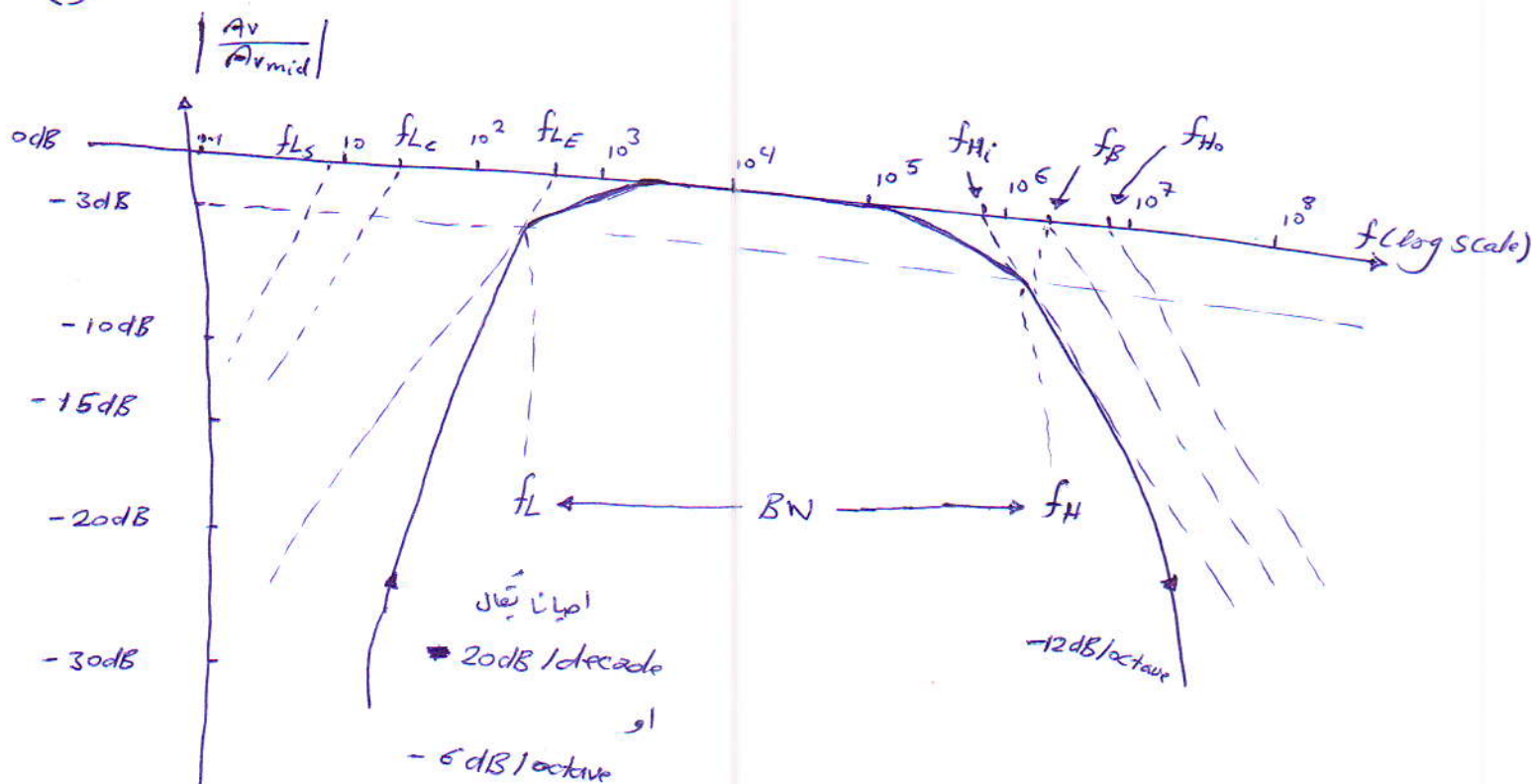
$$f_{H_o} = \frac{1}{2\pi R_{tho} C_o} = \frac{1}{2\pi (1.419k)(13.04p)} = 8.6MHz$$

(b)

$$f_\beta = \frac{1}{2\pi \beta_{mid} r_e (C_{be} + C_{bc})} = \frac{1}{2\pi (100)(15.76\Omega)(36p + 4p)} = 2.52MHz$$

$$f_T = \beta_{mid} f_\beta = (100)(2.52M) = 252MHz$$

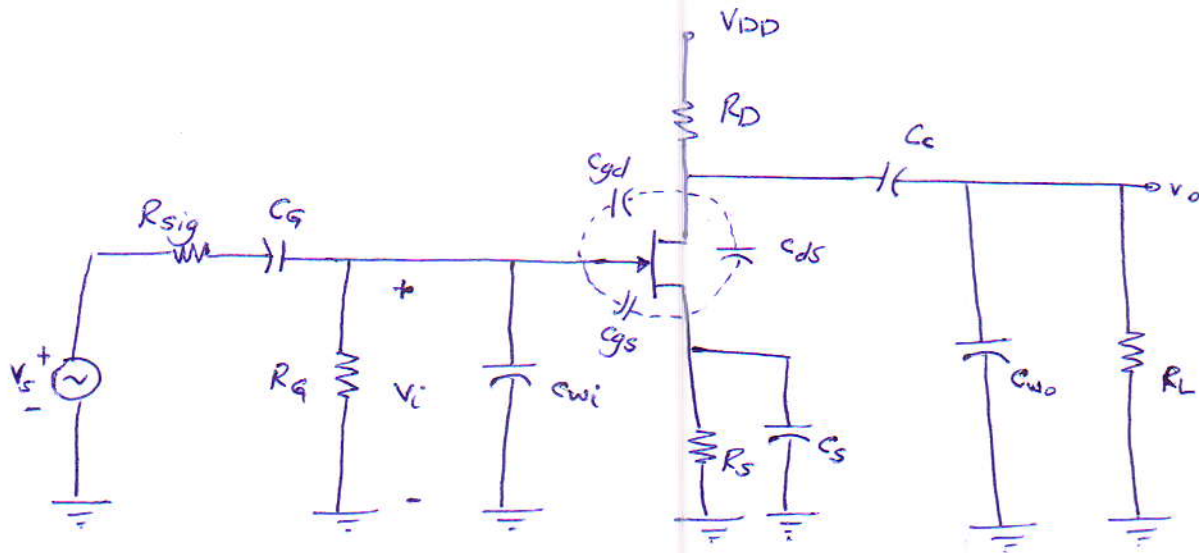
(c)



full frequency response for the CE config. network.

## \* High-Frequency Response - FET Amplifier:

The analysis of the high-freq. response of the FET amplifier will proceed in a very similar manner to that encountered for the BJT amplifier as shown in fig (18).



Fig(18): Capacitive elements that affect the high-freq. response of a JFET amplifier.

$$f_{Hi} = \frac{1}{2\pi R_{thi} C_i}$$

$$R_{thi} = R_{sig} \parallel R_G$$

$$C_i = C_{wi} + C_{gs} + C_{Mi}$$

$$C_{Mi} = (1 + |A_v|) C_{gd}$$

and for output circuit

$$f_{Ho} = \frac{1}{2\pi R_{tho} C_o}$$

$$R_{tho} = R_D \parallel R_L \parallel r_d$$

$$C_o = C_{wo} + C_{ds} + C_{Mo}$$

$$C_{Mo} = (1 + |1/A_v|) C_{gd}$$

(26)

Ex: Determine the high cutoff frequency with the following Parameter:

$$C_g = 0.01 \mu F, C_c = 0.5 \mu F, C_s = 2 \mu F, R_{sig} = 10 k\Omega, R_g = 1 M\Omega$$

$$R_D = 4.7 k\Omega, R_s = 1 k\Omega, R_L = 2.2 k\Omega, I_{DSS} = 8 mA, V_p = -4V, r_d = \infty \Omega$$

$$V_{DD} = 20V, C_{gd} = 2 pF, C_{gs} = 4 pF, C_{ds} = 0.5 pF, C_{wi} = 5 pF, C_{wo} = 6 pF$$

Solution:

$$R_{thi} = R_{sig} // R_g = 10 k // 1 M = 9.9 k\Omega$$

$$A_v = -3 \text{ From previous example }$$

$$C_i = C_{wi} + C_{gs} + (1 + |A_v|) C_{gd} = 5 pF + 4 pF + (1 + |-3|) 2 pF = 17 pF$$

$$f_{Hi} = \frac{1}{2\pi R_{thi} C_i} = \frac{1}{2\pi (9.9 k)(17 pF)} = 945.67 kHz$$

$$R_{tho} = R_D // R_L$$

$$= 4.7 k // 2.2 k \approx 1.5 k\Omega$$

$$C_o = C_{wo} + C_{ds} + C_{Ho} = 6 pF + 0.5 pF + (1 + \left| \frac{1}{-3} \right|) 2 pF = 9.17 pF$$

$$f_{Ho} = \frac{1}{2\pi (1.5 k)(9.17 pF)} = 11.57 MHz$$

### \* Multistage Frequency Effect :

when amplifier stages are cascaded to form a multistage amplifier, the dominant frequency response is determined by the responses of the individual stages. There are two cases to consider:

1. Each stage has a different lower critical freq. and a different upper cutoff frequency.

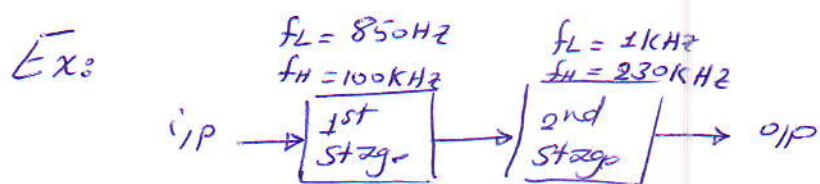
2. Each stage has the same lower cutoff freq. and the same upper cutoff frequency.

...

### \* Different cutoff frequency: (Nonidentical Stages)

when the lower cutoff freq. of each amplifier stage is different, the dominant  $f_L$  is equal to the highest freq. of stage.

when the upper cutoff freq. of each amplifier is different, the dominant  $f_H$  is equal to the lowest freq. of stage.



Determine the overall Bandwidth?

Solution:

$$f_L (\text{dominant}) = 1 \text{ kHz}$$

$$f_H (\text{dominant}) = 100 \text{ kHz} \quad \text{and} \quad BW = f_H - f_L$$

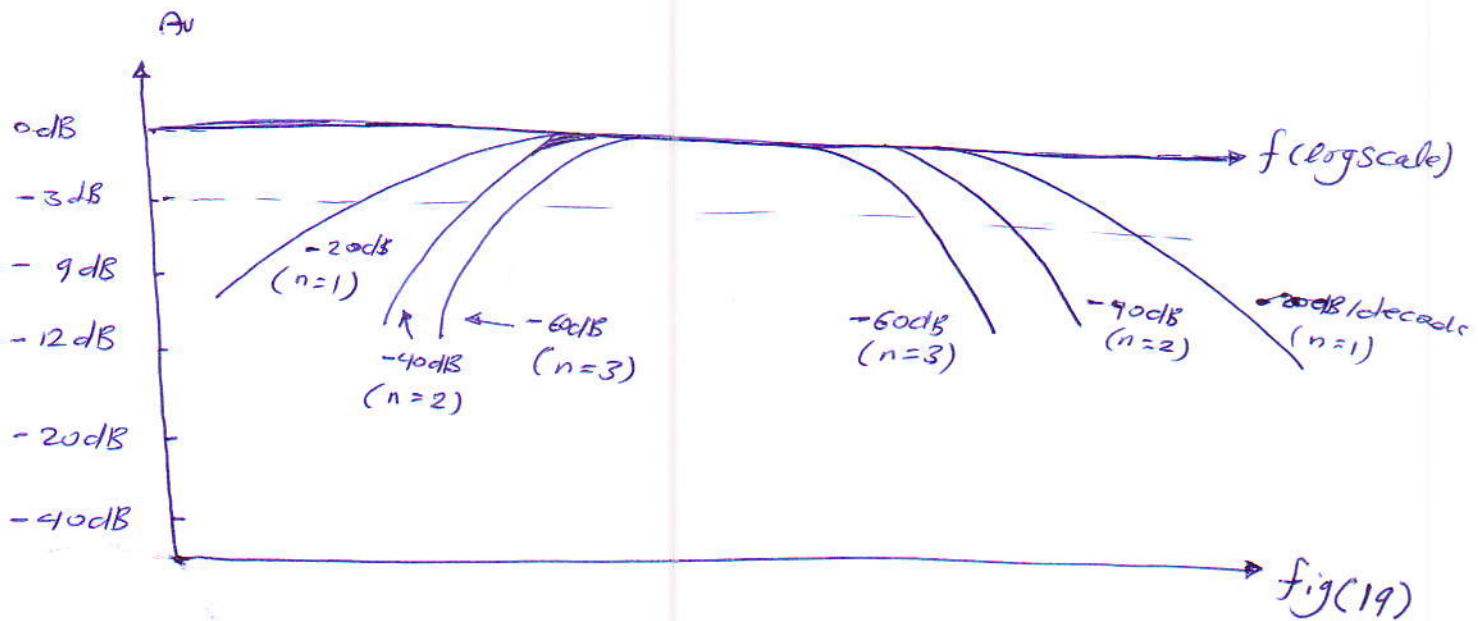
$$= 100 \text{ K} - 1 \text{ K} = 99 \text{ kHz}$$

\* Equal cutoff frequencies and Gain: (identical stages)

$$f_{L1} = f_{L2} = f_{Ln} ; f_{H1} = f_{H2} = f_{Hn} , A_{v1} = A_{v2} = A_{vn}$$

$$A_{v(\text{total or overall})} = A_{vT} = (A_m)^n \quad n: \text{number of stages}$$

\* For two identical stages cascade, the drop-off rate in the high and low frequency regions has increased to  $-12\text{dB/octave}$  or  $-40\text{dB/decade}$ . And for three stages increased to  $-18\text{dB/octave}$  or  $-60\text{dB/decade}$  as shown in fig below:



Effect of an increased number of stages on the cutoff frequencies and the Bandwidth.

$$\frac{A_{u_{low}}}{A_{u_{mid}}} (\text{overall}) = \left( \frac{A_{u_{low}}}{A_{u_{mid}}} \right)^n = \frac{1}{(1 - j \frac{f_L}{f})^n}$$

and the result equal to:

$$f_L^- = \frac{f_L}{\sqrt{2^{1/n} - 1}}$$

In a similar manner, it can be shown that for the high freq. region

$$f_H^- = (\sqrt{2^{1/n} - 1}) f_H$$

| ج, عدد Stages<br>(عدد المراحل) | ج, زيادة BW<br>زيادة النطاق الترددي | ج, $f_L^-$<br>gain | $n$ | $\frac{1}{\sqrt{2^{1/n} - 1}}$ |
|--------------------------------|-------------------------------------|--------------------|-----|--------------------------------|
|                                |                                     |                    | 2   | 0.64                           |
|                                |                                     |                    | 3   | 0.51                           |
|                                |                                     |                    | 4   | 0.43                           |
|                                |                                     |                    | 5   | 0.39                           |

Ex:  $A_{u(\text{overall})} = 4900$  for a multistage amplifier, find the number of stages, if the stage are identical and  $A_u$  for each stage is equal 70.

Solution:

$$A_{u(\text{overall})} = (A_u)^n$$

$$(4900) = (70)^n \Rightarrow \sqrt[n]{4900} = 70$$

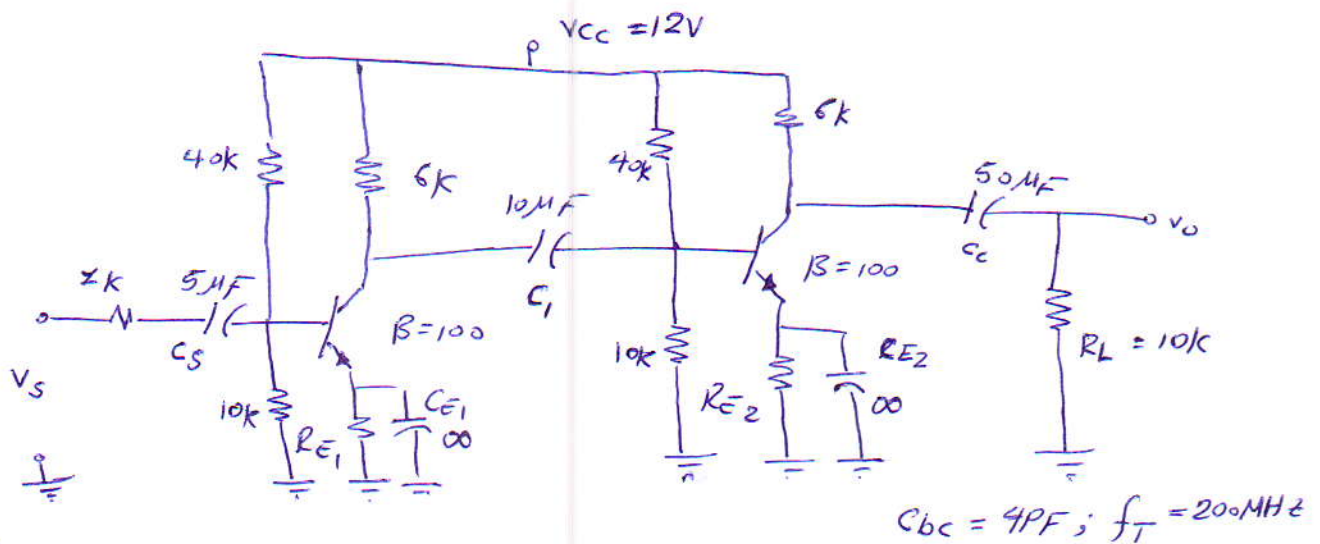
$$\Rightarrow n = \frac{\ln 4900}{\ln 70}$$

$$\therefore \boxed{n = 2}$$

$\therefore$  identical stage  
Integer - صحيح, عدد

Ex: For the circuit shown calculate:

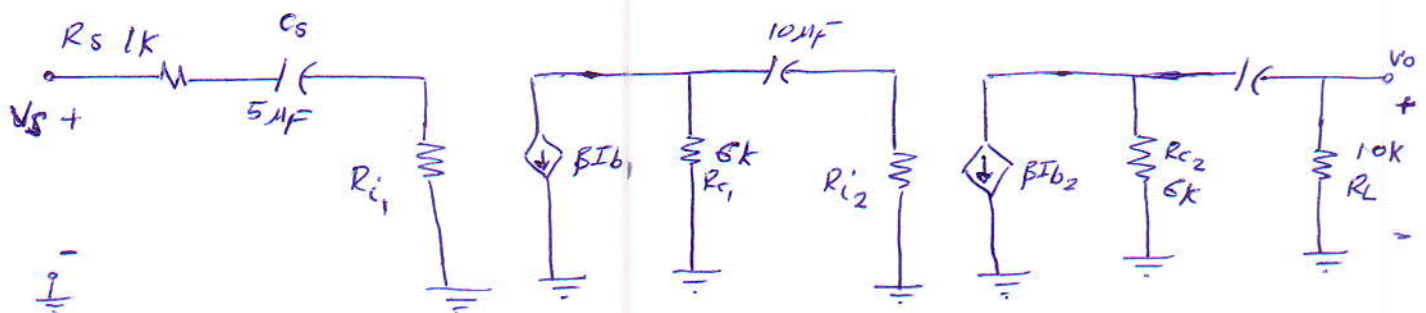
- ①  $R_{E1}$  and  $R_{E2}$  to obtain the emitter current  $0.5mA$  for each transistor
- ② The Bandwidth
- ③ The gain at  $1Hz$ ,  $1kHz$ ,  $10kHz$ ,  $1MHz$
- ④ How can you make the  $f_H$  (dominant) is equal to  $100kHz$



Solution:

\* Frequency Response at low freq: take the effect  $C_s$ ,  $C_c$  and  $C_1$  and ignore the effect of the  $(C_{E1}$  and  $C_{E2})$

ننظر على المصداق (D.C) ونغفل (A.C) (S.C)



$$R_{i1} = R_1 \parallel R_2 \parallel \beta r_e$$

$$R_{i2} = R_1 \parallel R_2 \parallel \beta r_e$$

to be continue

①

For approximation solution

③

$$V_B = \frac{12 \times 10k}{10k + 40k} = \boxed{2.4V} \quad \text{and} \quad V_E = V_B - V_{BE} = 2.4 - 0.7 = \boxed{1.7V}$$

$$R_{E1} = R_{E2} = \frac{V_E}{I_E} = \frac{1.7V}{0.5mA} = \boxed{3.4k\Omega}$$

$$\textcircled{2} \quad B.W = f_H - f_L$$

$$h_{ie1} = h_{ie2} = \beta r_e = 100 \times \frac{26mV}{0.5mA} = \boxed{5.2k\Omega} \quad r_e = 52\Omega$$

\* Take the effect of  $C_S$ :

$$f_{L_S} = \frac{1}{2\pi R_{th_S} C_S} \quad ; \quad R_{th_S} = R_i + R_S = R_S + (R_1 // R_2 // \beta r_e)$$

$$= 1k + (10k // 40k // 5.2k) = \boxed{4.15k}$$

$$= \frac{1}{2\pi (4.15k) (5\mu F)} = \boxed{7.67Hz} \quad (\text{dominant freq.})$$

\* Take the effect of  $C_1$ :

$$f_{L_{C_1}} = \frac{1}{2\pi R_{th_1} C_1} \quad ; \quad R_{th_1} = R_{C_1} + (R_2 // R_2 // h_{ie2})$$

$$= 6k + (10k // 40k // 5.2k) = \boxed{9.15k\Omega}$$

$$f_{L_{C_1}} = \frac{1}{2\pi R_{th_1} C_1} = \frac{1}{2\pi (9.15k) (10\mu F)} = \boxed{1.7Hz}$$

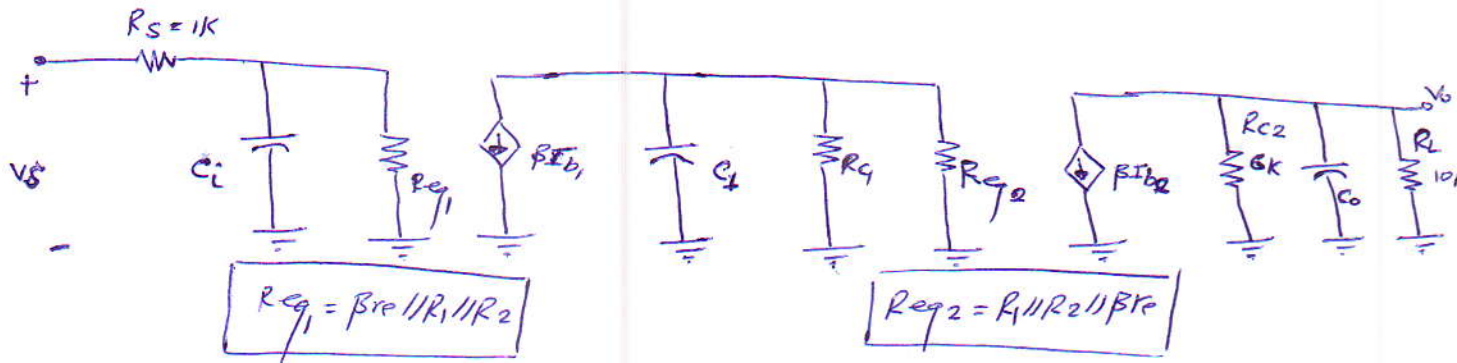
\* Take the effect of  $C_c$ :

$$f_{L_{C_c}} = \frac{1}{2\pi R_{th_c} C_c} \quad ; \quad R_{th_c} = R_{C_2} + R_L = 6k + 10k = \boxed{16k}$$

$$= \frac{1}{2\pi (16k) (50\mu F)} = \boxed{0.199Hz}$$

to be continue.

\* Frequency Response at high frequency (Parasitic Capacitances):



$$C_i = C_{wi} + C_{be1} + C_{bc1} (1 + |A_{v1}|)$$

$$C_4 = C_{w4} + C_{ce1} + C_{bc1} (1 + |1/A_{v1}|) + C_{be2} + C_{bc2} (1 + |A_{v2}|)$$

$$C_o = C_{wo} + C_{ce2} + C_{bc2} (1 + |1/A_{v2}|)$$

\* Take the effect of  $C_i$ :

$$f_{Hi} = \frac{1}{2\pi R_{thi} C_i} ; R_{thi} = R_s || R_{eq1} = 1k || (40 || 10)k || 5.2k$$

$$= \boxed{0.76k\Omega}$$

\* نحتاج إلى إيجاد  $C_i$ ،  $C_4$ ، و  $C_o$  في  $C_{be}$  و  $C_{bc}$  و  $C_{ce}$  و  $C_{wi}$  و  $C_{wo}$

$$C_i = C_{wi} + C_{be1} + C_{Mi}$$

$$C_{Mi} = C_{bc1} (1 + |A_{v1}|)$$

$$= 4p (1 + |A_{v1}|)$$

$$C_{bc} = 4pF$$

$$A_{v1} = \frac{-R'_L}{r_e} ; R'_L = \beta r_{e2} || R_1 || R_2 || R_{C1} = (5.2k) || 10k || 140k || 6k$$

$$= \frac{-2.066}{52} \approx \boxed{-40}$$

to be continue

$$\Rightarrow C_{M1} = 4P(1 + |-40|) = 164PF$$

$$f_T = \frac{1}{2\pi r_e (C_{be1} + C_{bC})} \Rightarrow 200MHz = \frac{1}{2\pi (52)(4PF + C_{be1})}$$

$$\Rightarrow (4PF + C_{be1}) \approx 15PF \quad \therefore C_{be1} = \boxed{11PF} = C_{be2}$$

$$\therefore f_{Hi} = \frac{1}{2\pi [(11P) + (164P)] (0.76K)} = \boxed{1.197MHz}$$

\* Take the effect of  $C_L$ :

$$f_{HC1} = \frac{1}{2\pi R_{th1} C_L} ; R_{th1} = R_C // R_1 // R_2 // \beta r_e$$

$$= 6K // 10K // 40K // 5.2K = \boxed{2.066K\Omega}$$

$$C_L = \cancel{C_{w1}} + \cancel{C_{ce1}} + \underbrace{C_{bC1} \left(1 + \left|\frac{1}{A_{v1}}\right|\right)}_{C_{M0}} + C_{be2} + \underbrace{C_{bc2} (1 + |A_{v2}|)}_{C_{M1}}$$

$$A_{v2} = \frac{-R_L}{r_e} = \frac{-6K // 10K}{52} \approx \boxed{-72}$$

$$\Rightarrow C_L = 11P + 4P(1 + \left|\frac{1}{-40}\right|) + 4P(1 + |-72|) \approx \boxed{307PF}$$

$$\therefore f_{HC1} = \frac{1}{2\pi (307P)(2.066K)} = \boxed{0.251MHz} \text{ (dominant freq.)}$$

\* Take the effect of  $C_0$ :

$$f_{H0} = \frac{1}{2\pi R_{th0} C_0} ; R_{th0} = R_C // R_L = \boxed{3.75K\Omega}$$

$$C_0 = \cancel{C_{w0}} + \cancel{C_{ce2}} + C_{bc2} (1 + |A_{v2}|)$$

to be continue.

$$C_o = 4P \left( 1 + \left| \frac{1}{-72} \right| \right) = \boxed{4.05 PF}$$

$$\Rightarrow f_{H_o} = \frac{1}{2\pi (4.05P)(3.75K)} = \boxed{10.484 MHz}$$

$$\therefore BW = f_H - f_L = 0.251M - 7.67 \approx \boxed{0.251 MHz}$$

③

$$A_{VT}(\text{midband}) = A_{V_1} \cdot A_{V_2} = (-90)(-72) = \boxed{2880}$$

\* at  $\pm Hz$  (low freq.)

$$\frac{A_v}{A_{mid}} = \frac{1}{\sqrt{1 + \left(\frac{f_L}{f}\right)^2}} \Rightarrow A_v = \frac{2880}{\sqrt{1 + \left(\frac{7.67}{1}\right)^2}} \approx \boxed{372}$$

\* at  $\pm kHz$  and  $10kHz$  the gain is equal to gain midband

\* at  $\pm MHz$  (high freq.)

$$\frac{A_v}{A_{mid}} = \frac{1}{\sqrt{1 + \left(\frac{f}{f_H}\right)^2}} \Rightarrow A_v = \frac{2880}{\sqrt{1 + \left(\frac{1M}{0.251M}\right)^2}} \approx \boxed{701}$$

$$\textcircled{4} f_{H_c} = \frac{1}{2\pi C_1 R_{th_1}} ; \boxed{R_{th_1} = 2.066 K\Omega}$$

$$100 kHz = \frac{1}{2\pi (2.066K)(307P + \bar{C})} \Rightarrow 307P + \bar{C} \approx 770P$$

$$\therefore \boxed{\bar{C} = 463 PF}$$

وهي قيمة المكثفات التي يجب ان تضاف  
واظية انشاء القطع لتجبل  
يكون قيمته  $100kHz$

H.W: For the common emitter amplifier circuit with the following <sup>(35)</sup> Parameter:

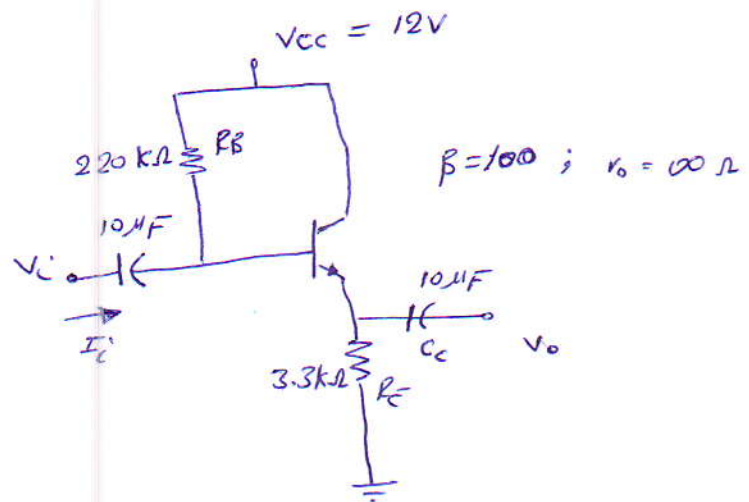
$C_{bc} = 2\text{PF}$ ;  $C_{be} = 100\text{PF}$ ;  $C_{ce} = 5\text{PF}$  and  $R_1 = 40\text{k}\Omega$ ,  $R_2 = 10\text{k}\Omega$ ,  
 $R_S = 400\Omega$ ,  $R_C = 3\text{k}\Omega$ ,  $R_L = 6\text{k}\Omega$ ,  $R_E = 0.5\text{k}\Omega$ ,  $C_S = 1\mu\text{F}$ ,  
 $C_C = 1.8\mu\text{F}$  and  $C_E = 10\mu\text{F}$ ,  $\beta = 100$ ,  $V_{CC} = 12\text{V}$

Assume the wiring capacitors at i/p is  $4\text{PF}$  and at o/p is  $6\text{PF}$

- 1-  $A_{mid}$  and  $f_L$
- 2-  $f_H$  and Bandwidth
- 3- Sketch the frequency Response using Bode Plot
- 4- Calculate the voltage gain at  $20\text{Hz}$ ,  $10\text{kHz}$  and  $5\text{MHz}$
- 5- Calculate the frequency at which the gain drops to 60% of its maximum value
- 6- If we add another capacitor  $\bar{C}$  Parallel with  $C_S$ , is the BW will effect? Explain (Assume  $\bar{C} = 1\mu\text{F}$ )

EX: For the emitter follower network below Determine

- ① The gain at midband frequency.
- ② Lower cutoff frequencies.



Solution:

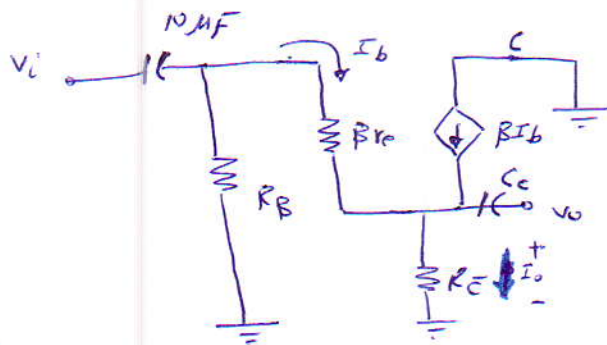
At first, we obtain the ac equivalent circuit at low frequency

①

$$V_o = I_o R_E$$

$$= (1 + \beta) I_b R_E$$

$$I_b = \frac{V_i}{Z_b} = \frac{V_i}{R_B + (1 + \beta) R_E}$$



$$\therefore \frac{V_o}{V_i} = A_v = \frac{(1 + \beta) R_E}{R_B + (1 + \beta) R_E} \approx \frac{\beta R_E}{\beta (r_e + R_E)} = \boxed{\frac{R_E}{r_e + R_E}}$$

to find  $r_e$ :

$$V_{CC} - I_B R_B - V_{BE} - I_E R_E = 0 \quad \Rightarrow \quad V_{CC} - I_B R_B - V_{BE} - (\beta I_B + I_B) R_E = 0$$

$$\Rightarrow I_B = \frac{V_{CC} - V_{BE}}{R_B + (1 + \beta) R_E} = \frac{12 - 0.7}{220k + (1 + 100) 3.3k} = \boxed{20.42 \mu A}$$

to be continue.

$$I_E = (1+\beta)I_B = (1+100)20.42\mu = \boxed{2.062\text{mA}}$$

$$\therefore r_e = \frac{26\text{mV}}{2.062\text{mA}} = 12.61\Omega$$

$$\Rightarrow A_v = \frac{3.3\text{k}}{3.3\text{k} + 12.61} = \boxed{0.996 \approx 1}$$

(2)

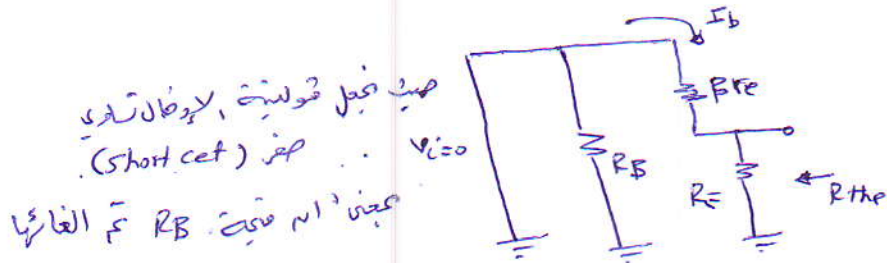
$$f_{Ls} = \frac{1}{2\pi R_{th}s C_s} \quad ; \quad R_{th}s = R_B \parallel Z_b$$

$$= \boxed{R_B \parallel [\beta r_e + (1+\beta)R_E]}$$

$$f_{Lc} = \frac{1}{2\pi R_{thc} C_c}$$

$$; \quad R_{thc} = R_E \parallel r_e$$

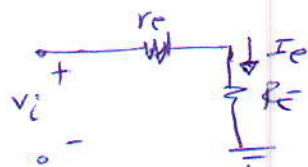
وهنا في نموذجنا، لدينا دقيقتان  
 $f_{Lc}$  و  $f_{Ls}$  ولكن للتوضيح أكثر  
 نفضل كتابة حساب  $R_{thc}$



$$I_E = (1+\beta)I_B \quad ; \quad I_B = \frac{V_i}{Z_b}$$

$$\Rightarrow \left[ I_B = \frac{V_i}{h_{ie} + (1+\beta)R_E} \right] \quad * (1+\beta) \text{ دقيقتان}$$

$$\frac{(1+\beta)I_B}{I_E} = \frac{V_i (1+\beta)}{\beta r_e + (1+\beta)R_E} \Rightarrow I_E = \frac{V_i}{\frac{\beta r_e}{1+\beta} + R_E} = \frac{V_i}{r_e + R_E}$$



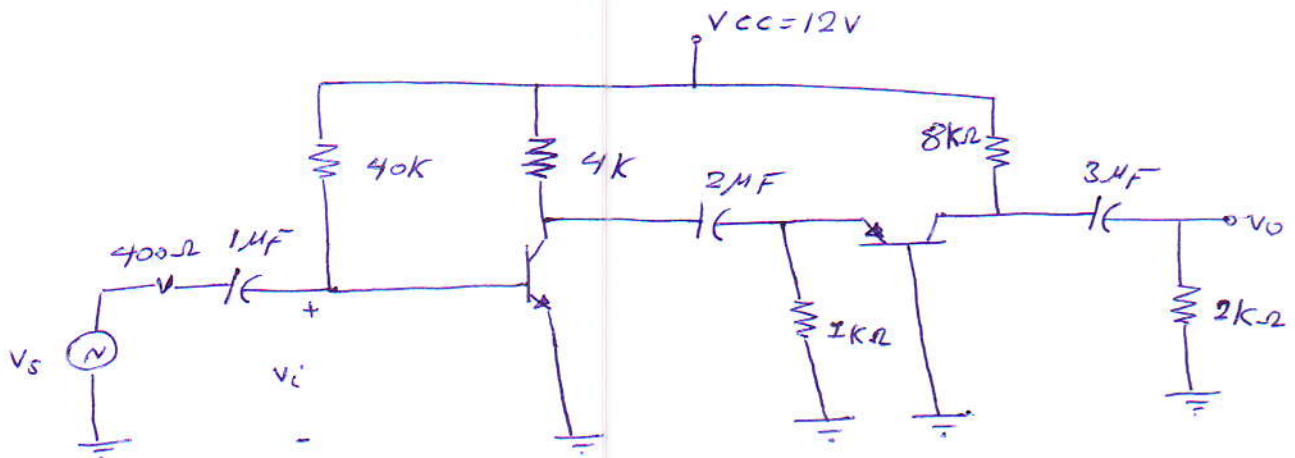
لغني ذلك، اننا فيجب علينا إيجاد  $I_E$   
 هي عبارة عن مقاومة  $V_i$   
 على مقاومتي على التوالي  $(r_e + R_E)$   
 ولكن يجب علينا  $V_{i=0}$  (Short cut)  
 تصبح هنا المقاومة المكافئة

$$\boxed{R_E \parallel r_e}$$

H.W.:

For the Cascode amplifier shown in figure below:

- 1- calculate midband voltage gain,  $f_L$  and  $f_H$ : Assuming that  $f_H$  is due to the stray capacitance of the C.E stage
- 2- Sketch the Bode Plot response
- 3- what is the advantage of this connection



$$C_{be} = 200 \text{ pF}$$

$$C_{bc} = C_{ce} = 5 \text{ pF}$$

$$h_{ie} = 2 \text{ k}\Omega$$

$$h_{fe} = 100$$

## Feedback Amplifier:

is one in which a fraction of the amplifier output is fed back to the inputs to control the output and consist of two parts an amplifier and a F.B connection.

$x_s$ : external signal

$x_o$ : output signal

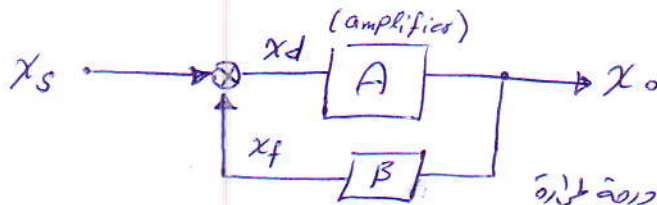
$x_f$ : F.B signal

$A_f$ : close loop gain (gain with F.B)

$x_d$ : Difference signal  $\Rightarrow x_d = x_s \mp x_f$

$A$ : gain of the basic amplifier (open loop gain)

$\beta$ : F.B ratio,  $\beta = \frac{x_f}{x_o}$



يتمثل الأنسب للكثير بتغيير درجة الحرارة  
وتغيير توليد القدرة المقرة وتقدم على المكونات  
وتغير معالج الدوائر عند احتياجه لذلك  
نبدأ إلى المقذبة العكسية للحصول على استقرار  
أفضل

1- If  $x_f$  is in phase with  $x_s$ : +ve F.B,  $x_d = x_s + x_f$  and this is Principle oscillators.

2- If  $x_f$  is out of Phase with  $x_s$ : -ve F.B, then  $x_d = x_s - x_f$

## Effect of -ve F.B:

- ① Reduce the gain ; ② Extend the BW
- ③ Increase gain stability against impedances Parameters variations.
- ④ Reduce Noise and Nonlinear distortion
- ⑤ control the I/P and O/P impedances

→ to be continue.

for the F.B. amplifier

(40)

$$A = \frac{x_o}{x_i} ; x_i = x_d \Rightarrow x_i = x_s - x_f$$

$$\therefore x_o = A x_i \quad \therefore x_o = A (x_s - x_f) \dots \textcircled{1}$$

$$x_f = \beta x_o \dots \textcircled{2} \text{ Subs. } \textcircled{1} \text{ in } \textcircled{2} \text{ and we get:}$$

$$x_o = A (x_s - \beta x_o) = A x_s - A \beta x_o \Rightarrow \boxed{\frac{x_o}{x_s} = \frac{A}{1 + A\beta} = A_f}$$

the equation above show that the gain with F.B. reduces by the factor  $\boxed{(1 + A\beta)}$

### Effect of Negative F.B. on amplifier:

#### ① Reduction in frequency distortion:

when  $\beta A \gg 1 \Rightarrow$  gain with feedback is  $A_f \approx \frac{1}{\beta}$  (Purely Resistive)

ب: هي عبارة عن قيم صارية ولا تتغير قيمتها على تردد الإدخال لذلك لا تتأثر بالتردد الداخل  
أيضا في المكبر الإيجابي مع غير F.B. فانه الكسب (A) يتأثر بالتردد الداخل بصورة  
مباشرة وبالتالي فانه -ve F.B. يقل من التلويح بسبب زيادة التردد أو نقصانه

## ② Reduction in Noise and Nonlinear Distortion:

### \* Nonlinear Distortion:

this distortion is due to the non-linear relation between i/p voltage and current in transistor

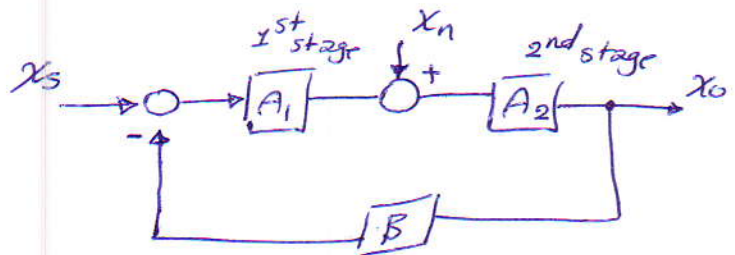
Assuming distortion without F.B. is "D", with F.B. it will be

$$D_f = \frac{D}{1 + A\beta}$$

صوت قبل التغذية الراجعة  $D$  في  
يُقسم على  $(1 + A\beta)$

### \* Noise:

-ve F.B reduces the internal noise, consider the system shown in fig. below, where  $x_n$  is an internal noise (generated by  $A_1$ )



without F.B.

$$\begin{aligned} x_o &= (x_s A_1 + x_n) A_2 \\ &= x_s A_1 A_2 + x_n A_2 \end{aligned}$$

with F.B

$$x_o = \frac{A_1 A_2}{1 + A\beta} x_s + \frac{A_2}{1 + A\beta} x_n$$

نلاحظ ان صوت التشويش (noise) قد قُسم على  $(1 + A\beta)$  لأن

كانت نسبة كسره

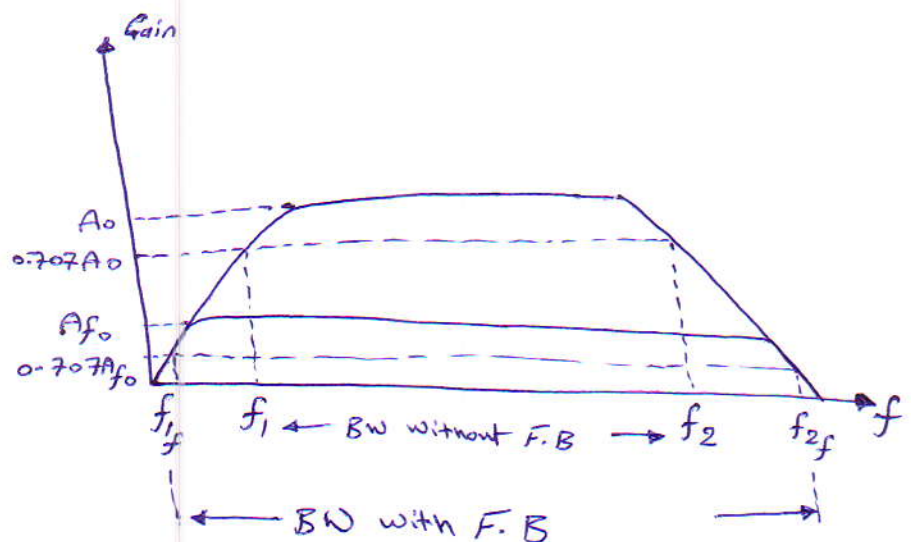
∴ -ve F.B reduce the effect of internal noise.   
 أي أنه كلما زاد  $A\beta$  قل التشويش الداخلي

### ③ Effect of -ve feedback on Gain and Bandwidth:

The overall gain with -ve F.B

$$A_f = \frac{A}{1 + A\beta} \approx \frac{A}{A\beta} \approx \frac{1}{\beta} \text{ for } A\beta \gg 1$$

عملية تأثير كسب المستطاع المربوط على التوالي في الترانزستور في حالة الترددات، لواطت اما في الترددات العالية فانه الكسب يتأثر بالمستطاع، لذلك (Parasitic) - اما في حالة ربط الترددات المنخفضة فانه الكسب تقريباً يساوي  $\frac{1}{\beta}$  لذلك فانه متغير، الاحتمال لتأثير بالمستطاع مطلقاً لذلك فانه متغير عادة لذلك لا يقل الكسب مباشرة عند تغيير قيمته الى A ولكن بعد تغيير كبير لقيمة A لذلك يزداد BW كما هو موضح في الرسم ادناه



The -ve F.B. extends the B.W of the amplifier where it reduces  $f_L$  and increases  $f_H$  resulting increasing the B.W of the amp.

حيث بانخفاض الكسب، يزداد عرض النطاق الترددي

$$A_{f_L} = \frac{A_m}{1 - j \frac{f_L}{f}} \quad \text{--- (1)}$$

when the -ve F.B is applied the gain will be reduced to:

$$A_f = \frac{A}{1 + A\beta} \quad \text{--- (2) substituting (1) in (2) and we get:}$$

$$\Rightarrow (A_{Lf})_F = \frac{\frac{A_m}{1 - \frac{f_L}{f}}}{1 + \left( \frac{AB}{1 - j \frac{f_L}{f}} \right)} = \frac{A_m}{1 - j \frac{f_L}{f} + AB} = \frac{A_m}{f(1+AB) - j f_L}$$

نقسيه بسا  
مالحاق على  
(1+AB)  
كه

$$\Rightarrow (A_{Lf})_F = \frac{\left[ \frac{A_m}{1+AB} \right] \leftarrow \text{F.B gain}}{1 - j \left[ \frac{f_L}{f(1+AB)} \right] \leftarrow \text{F.B } f_L} = \frac{A_{mf}}{1 - j \frac{(f_L)_F}{f}}$$

$$\Rightarrow (f_L)_F = \frac{f_L}{1+AB} \quad \text{and in the same way we can show that}$$

$$(f_H)_F = f_H (1+AB)$$

وبالتالي قلت  $f_L$  وزادت  $f_H$  لذلك ازادت BW

#### ④ Gain stability with Feedback:

$$A_f = \frac{A}{1+AB}$$

$$\Rightarrow \left| \frac{dA_f}{A_f} \right| = \frac{1}{|1+AB|} \left| \frac{dA}{A} \right|$$

where  $AB \gg 1$

$$\Rightarrow \left| \frac{dA_f}{A_f} \right| \approx \left| \frac{1}{AB} \right| \left| \frac{dA}{A} \right|$$

في حالة ربط النظام بالتغذية العكسية  
فانه تغير الكسب لا يؤثر مباشرة  
على الكسب الكلي ~~نظرا~~ كثيرا  
لذلك تزداد استقرارية الكسب  
وبالتالي ناه اي تغير بسبب  
في رصبة، طمارة او ضربة  
المكونات طانه لا يؤثر  
على استقرارية الكسب

حيث ان ضربة تغير كسب التغذية العكسية  
تم قعطيلته بمعامل  $\left| \frac{1}{AB} \right|$  بينما الكسب من دون  
التغذية العكسية يتغير صلبة  $\left| \frac{dA}{A} \right|$

Ex: If an amplifier gain of  $-1000$  and F.B of  $\beta = -0.1$  has a gain change of  $20\%$  due to temperature, calculate the change in gain of the F.B amplifier.

Solution:

$$\left| \frac{dA_f}{A_f} \right| \approx \left| \frac{1}{A\beta} \right| \left| \frac{dA}{A} \right| = \left| \frac{1}{(-0.1)(1000)} \right| * \left| \frac{20}{100} \right| = 0.2\%$$

نلاحظ ان نسبة الاستقرار في الكسب في الـ F.B اعظم منه في الـ A، لأن الكسب في الـ F.B اعظم رتبة من الـ A، لذلك فـ F.B اعظم رتبة من الـ A.

### ⑤ Effect of -ve F.B. on the I/P and o/p impedances:

This effect depends on the F.B. signal is sampled and added to the input, i.e depend on the "topology"

For series input connection, the I/P impedance increase and for shunt connection the input impedance decrease, the same effect is for the output impedance. as shown in table below:

| Parameter     | Voltage series | Voltage shunt | Current series | Current shunt |
|---------------|----------------|---------------|----------------|---------------|
| I/P impedance | Increase       | decrease      | increase       | decrease      |
| o/p impedance | decrease       | decrease      | increase       | increase      |

Effect of -ve F.B. on I/P and o/p impedance

دراسة خصائص التوصيل

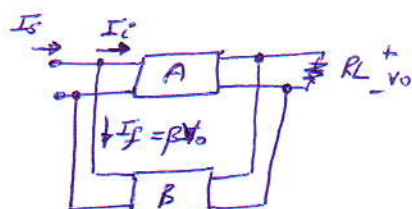
# \* F.B Connection Types (Topologies):

- ① Voltage series F.B.
- ② Voltage shunt F.B.
- ③ Current series F.B.
- ④ Current shunt F.B.

اعتماداً على ربط الإدخال، فإن مخرجاته إما  
الإخراج يسوق دائرة التغذية، والعكس  
لجعل الإدخال بسيطاً منطوقه دقيقة على  
مخرجات الإدخال

~ ~ ~ ~ ~

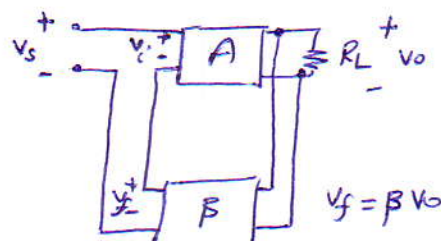
## ① Voltage shunt:



(transresistance amplifier)

يسير في ال digital ameter  
مقاومة الإدخال وإخراج قليلة

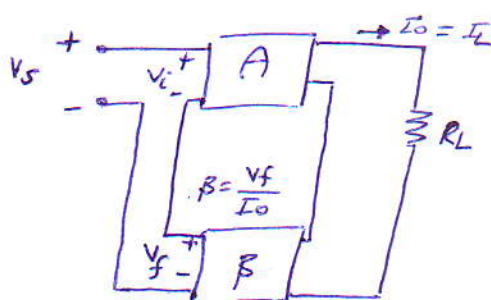
## ② Voltage series:



(voltage amplifier)

with  $Z_i$  is increased and o/p ( $Z_o$ ) is decreased

## ③ Current Series:



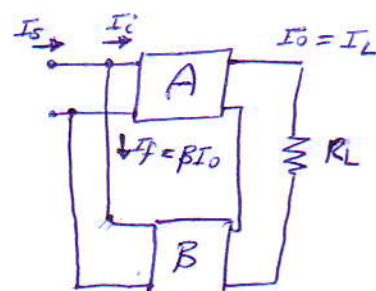
(transconductance amplifier)

I/p and o/p impedances are increased

يصلح لقياس ال Digital Voltmeter والى

تكون مقاومة الإدخال ب MΩ

## ④ current shunt:



(current amplifier)

with  $Z_i$  is decreased and  $Z_o$  is increased

# Procedures summary of analysis F.B. amplifier

| Topology<br>characteristics  | Voltage<br>Series       | Voltage<br>Shunt        | Current<br>Series       | Current<br>shunt        |
|------------------------------|-------------------------|-------------------------|-------------------------|-------------------------|
| 1- To find i/p loop          | Set $V_o = 0$           | $V_o = 0$               | $I_o = 0$               | $I_o = 0$               |
| 2- To find o/p loop          | Set $I_i = 0$           | $V_i = 0$               | $I_i = 0$               | $V_i = 0$               |
| 3- Signal Source             | Thevenin                | Norton                  | Thevenin                | Norton                  |
| 4- $\beta = \frac{x_f}{x_o}$ | $\frac{V_f}{V_o}$       | $\frac{I_f}{V_o}$       | $\frac{V_f}{I_o}$       | $\frac{I_f}{I_o}$       |
| 5- $A = \frac{x_o}{x_i}$     | $A_v = \frac{V_o}{V_i}$ | $R_M = \frac{V_o}{I_i}$ | $G_M = \frac{I_o}{V_i}$ | $A_i = \frac{I_o}{I_i}$ |
| 6- $D = 1 + A\beta$          | $1 + \beta A_v$         | $1 + \beta R_M$         | $1 + \beta G_M$         | $1 + \beta A_i$         |
| 7- $A_f$                     | $\frac{A_v}{D}$         | $\frac{R_M}{D}$         | $\frac{G_M}{D}$         | $\frac{A_i}{D}$         |
| 8- $R_{if}$                  | $R_i \cdot D$           | $\frac{R_i}{D}$         | $R_i \cdot D$           | $\frac{R_i}{D}$         |
| 9- $R_{of}$                  | $\frac{R_o}{D}$         | $\frac{R_o}{D}$         | $R_o \cdot D$           | $R_o \cdot D$           |

## Method Analysis of F.B. amplifier:

a- To find the I/P circuit:

نفساً يُدْرَأُ لِيُظَاهَرَ بِجِبِلِّ الْإِخْرَاجِ بِأَرْبَعِ صَفْحَاتٍ الْإِخْرَاجِ أَمَّا يُدْرَأُ أَوْ تَوَلَّى

- 1- Set the output voltage ( $V_o = 0$ ) short o/p (for voltage sampling).
- 2- Set the output current ( $I_o = 0$ ) open o/p (for current sampling)

b- To find the o/p circuit:

نفساً يُدْرَأُ لِيُظَاهَرَ بِجِبِلِّ الْإِخْرَاجِ بِأَرْبَعِ صَفْحَاتٍ الْإِخْرَاجِ أَمَّا يُدْرَأُ أَوْ تَوَلَّى

- 1- Set  $V_i = 0$  for shunt comparison (short circuit to i/p).
- 2- Set  $I_i = 0$  for series comparison (open circuit to i/p).

To complete the analysis: follow the steps below:

- 1- Identify the F.B. Topology
- 2- Draw the basic amplifier circuit without F.B.
- 3- Replace each active device by Proper model.
- .....

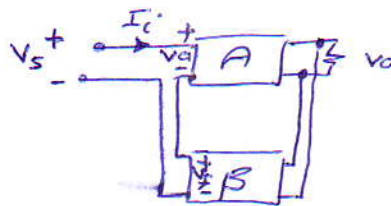
Ex: Prove that  $Z_{if} = Z_i (1 + \beta A)$  for the voltage series F.B. connection?

Solution:

$$V_s = V_a + V_f$$

$$V_f = \beta V_o \text{ and } V_o = A V_a$$

$$\Rightarrow V_s = V_a + \beta V_o = V_a + A\beta V_a$$



$$\therefore V_s = V_a (1 + A\beta)$$

$$\therefore V_s = Z_{if} \cdot I_i$$

$Z_{if}$  (i/p impedance with F.B)

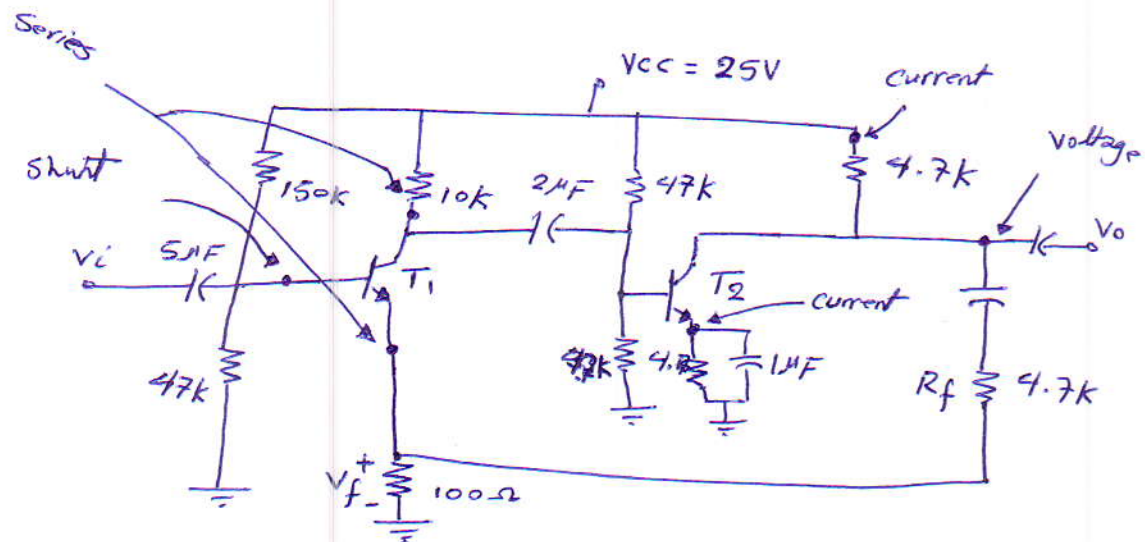
$$\Rightarrow \frac{V_s}{I_i} = \frac{V_a}{I_i} (1 + A\beta)$$

$$\therefore \boxed{Z_{if} = Z_i (1 + A\beta)}$$

$Z_i$  (i/p impedance without F.B)

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Ex: For the F.B amplifier shown below  $T_1$  and  $T_2$  are Identical transistors with:  $h_{fe} = 50$ ,  $h_{ie} = 1.1k\Omega$ ; calculate the overall gain, the i/p and o/p impedance ( $Z_i$  and  $Z_o$ ) before and after F.B?

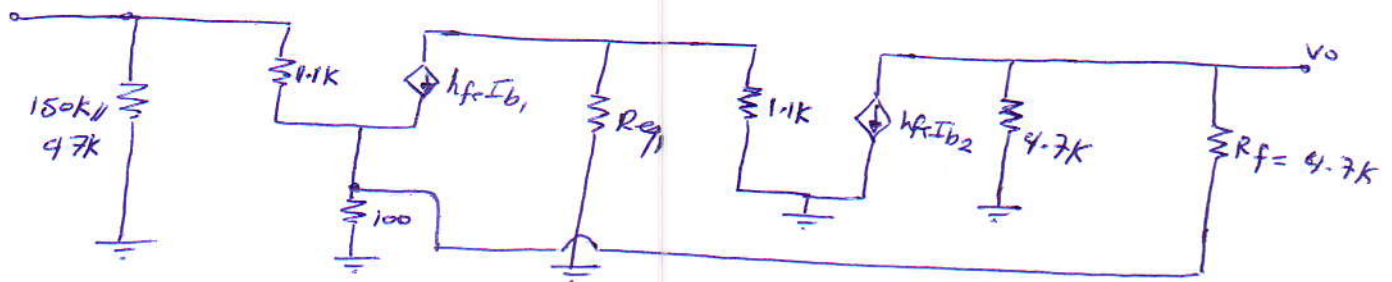


Solution:

Step ①

① Topology type is Voltage-Series

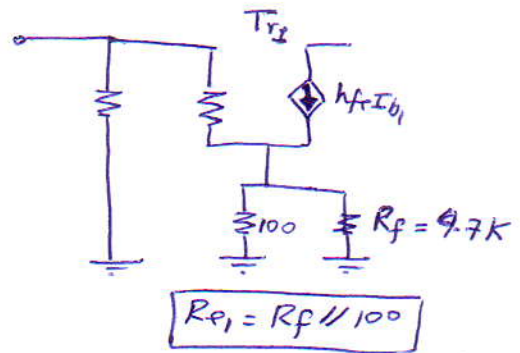
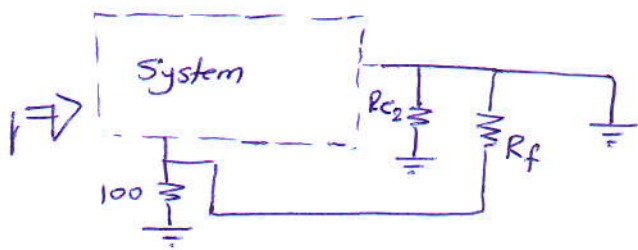
Step ② to find the input set  $V_o = 0$  because (o/p is voltage)



$$R_{eq1} = R_{C1} \parallel R_{B1} \parallel R_{B2}$$

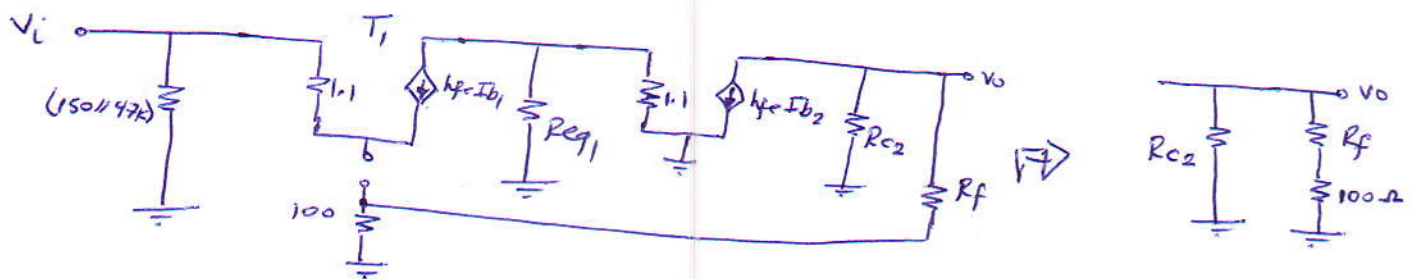
to be continue

(49)

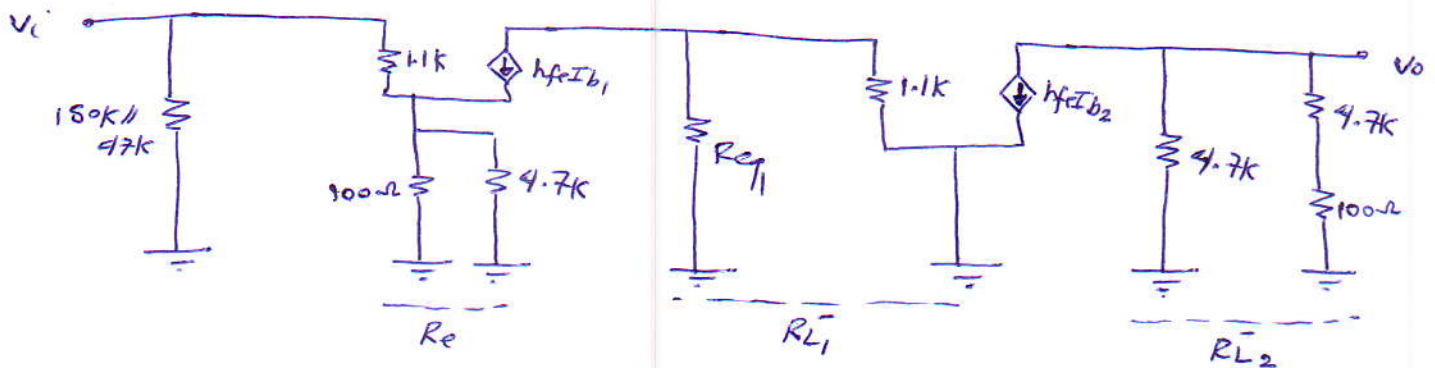


Step ③ to find the output circuit:

Set ( $I_i = 0$  because input series)



Step ④ Basic amplifier set without F.B



$$R_{L1} = R_{C1} \parallel R_{B1} \parallel R_{B2} \parallel h_{ie2} = 10k \parallel 47k \parallel 33k \parallel 1.1k = 942 \Omega$$

$$R_{L2} = (4.7k + 100) \parallel 4.7k = 2.37k \Omega$$

$$R_e = 100 \parallel 4.7k = 98 \Omega$$

→

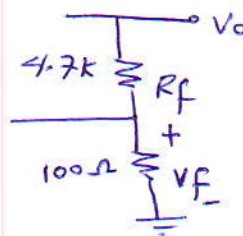
$$A_{v1} = \frac{-h_{fe} R_{L1}}{h_{ie1} + (1+\beta) R_e} = \frac{-50 * 942}{1.1k + (1+50) 98} = \boxed{-7.72}$$

$$A_{v2} = \frac{-h_{fe} R_{L2}}{h_{ie}} = \frac{-50 * 2.37k}{1.1k} = \boxed{-108}$$

$$\text{overall gain } (A_{VT}) = A_{v1} \cdot A_{v2} = (-7.72)(-108) = \boxed{834}$$

To find  $\beta$  value?

$$V_f = \frac{V_o * 100}{100 + 4.7k}$$



$$\therefore \beta = \frac{V_f}{V_o} \quad \therefore \beta = \frac{100}{100 + 4.7} = \boxed{\frac{1}{48}}$$

$$\Rightarrow D = 1 + \beta A_{VT} = 1 + \left(\frac{1}{48}\right)(834) = \boxed{18.4}$$

$$\Rightarrow A_{vf} = \frac{A_{VT}}{D} = \frac{834}{18.4} \approx \boxed{45.4}$$

① ملاحظه: انخفاض الكسب من 834 إلى 45.4  
② كسب  $A_{vf} \approx \frac{1}{\beta}$  أي تقريباً يساوي  $\frac{1}{48}$

$$A_f = \frac{A}{1+\beta A} \approx \frac{1}{\beta} \quad \text{لأن}$$

$$Z_{if} = Z_i (1 + \beta A) = Z_i (18.4)$$

$$Z_i = h_{ie1} + (1 + \beta) R_e$$

$$= 1.1k + (1 + 50) 98 \approx 6.1k \Omega \Rightarrow Z_{if} = 6.1k * 18.4 = \boxed{112.24k \Omega} \quad \text{تزداد}$$

$$Z_{of} = \frac{Z_o}{D} = \frac{R_{C2} \parallel R_{L2}}{D} = \frac{4.7k \parallel 4.8k}{18.4} = \boxed{129 \Omega} \quad \text{تقل}$$

ملاحظة: يتم احتساب  $Z_i$  للترانزستور بعد مقاومة  $R_B$  لحساب قيمته  $Z_i$  مع غير اوضاع قيم المقاربات المتوسطة لاحقاً. اما في حالة عدم توافر السؤال فيتم الاخذ بنظر الاعتبار مكان تحديد  $Z_i$

Ex: For the circuit shown; calculate  $A_{vf}$ ,  $Z_{if}$  and  $Z_{of}$ ?

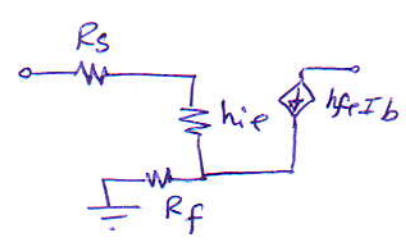
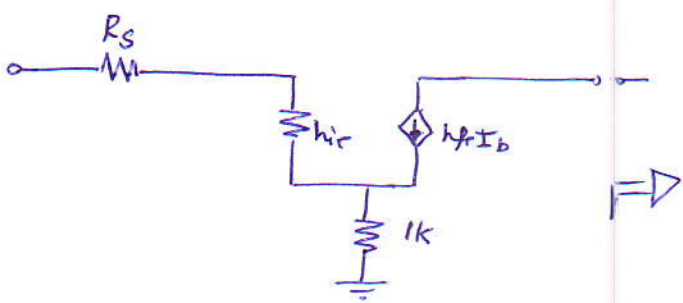
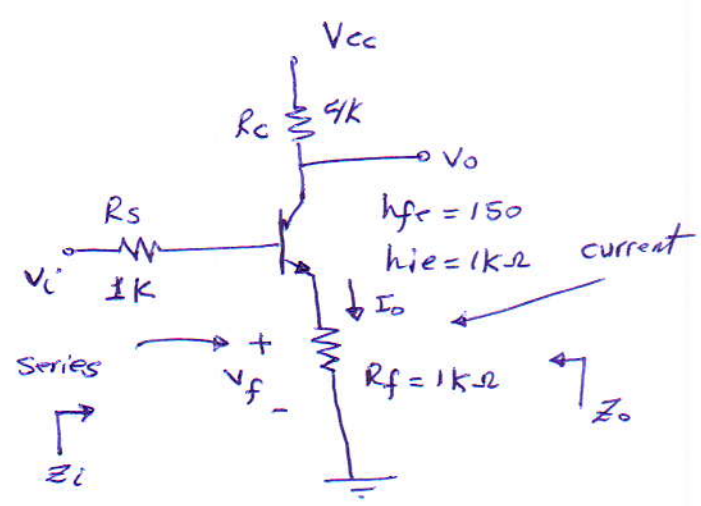
Solution:

Step ①:

Topology type is current-series

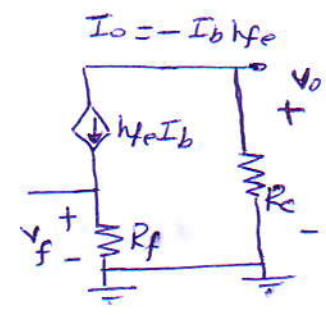
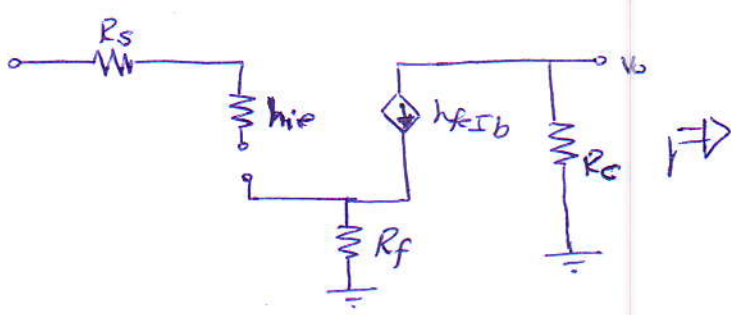
Step ②:

To find the input circuit  $I_o = 0$

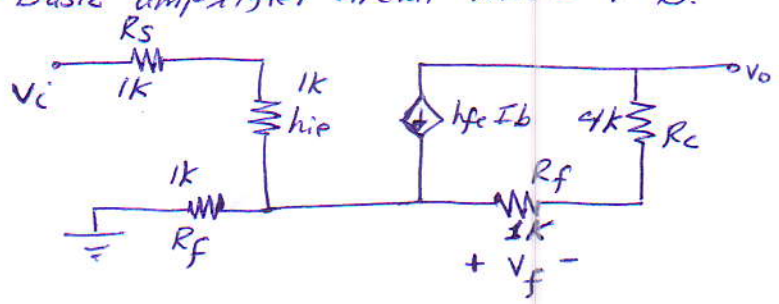


Step ③:

To find the output circuit  $I_i = 0$



Step ④: Basic amplifier circuit without F.B.



to be continue.

$$\beta = \frac{V_f}{I_o} ; V_f = -I_o R_f \Rightarrow \beta = -R_f = \boxed{-1k\Omega}$$

$$A_f \text{ (gain with feedback)} = \frac{I_o}{V_i} = \frac{A}{1 + \beta A}$$

$$G_M = \frac{I_o}{V_i} = \frac{-h_{fe} I_b}{I_b (R_s + h_{ie} + R_f)} = \frac{-150}{(1k + 1k + 1k)} = \boxed{-50mA/V}$$

$$D = 1 + \beta G_M = 1 + (-1000)(-50 \times 10^{-3}) = \boxed{51}$$

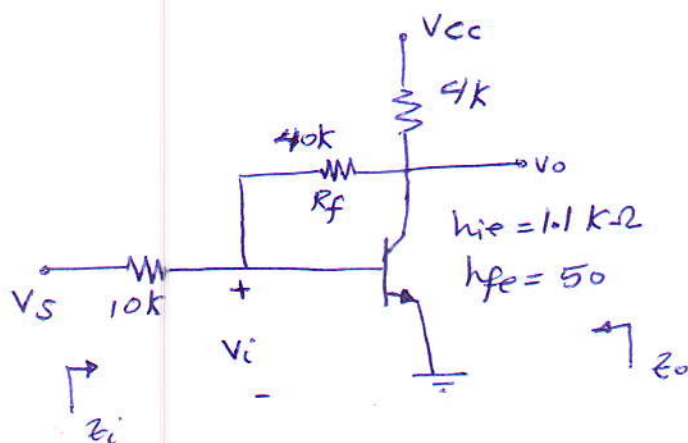
$$A_f \text{ or } G_{Mf} = \frac{A}{1 + \beta \beta} = \frac{G_M}{D} = \frac{-50mA/V}{51} \approx \boxed{-1mA/V}$$

$$A_{vf} = \frac{V_o}{V_i} = \left[ \frac{-I_o R_c}{V_i} \right] = -1 \times 10^{-3} \times 4k = \boxed{-4}$$

$$Z_{if} = (R_s + R_f + h_{ie}) D = (3k)(51) = \boxed{153k\Omega}$$

$$Z_{of} = R_c \times D = 4k \times 51 = \boxed{204k\Omega}$$

Ex: For the circuit shown below, find  $A_{vf}$ ,  $Z_{if}$  and  $Z_{of}$ ?

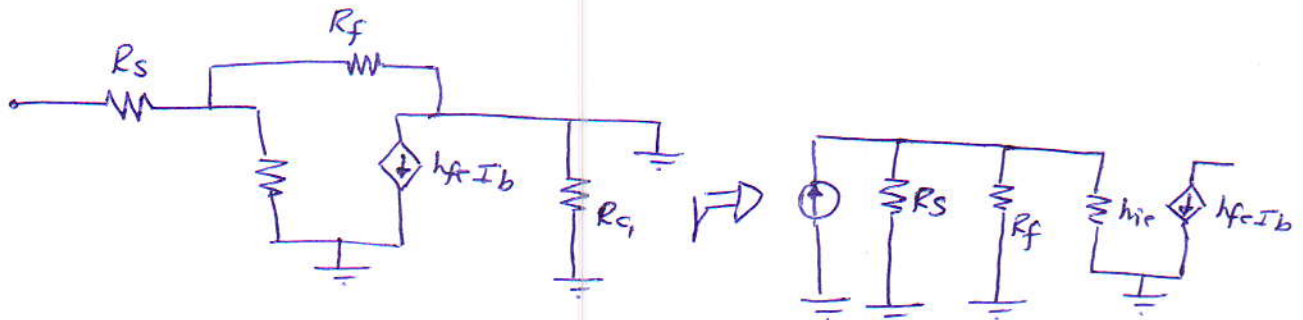


to be continue.

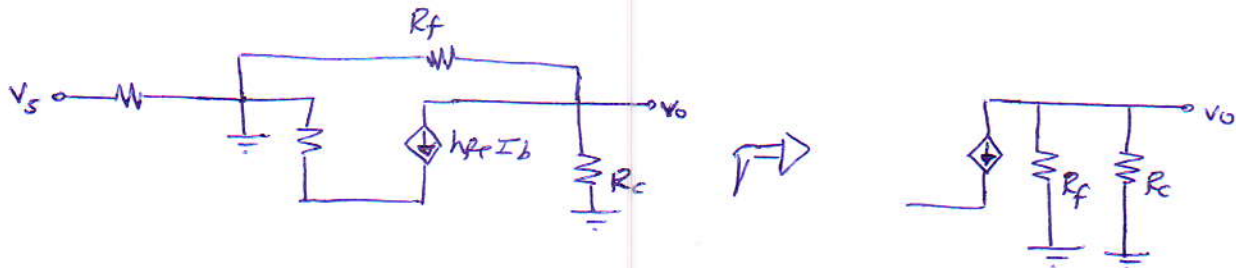
Solution:

Step ①: Topology type is Voltage-Shunt

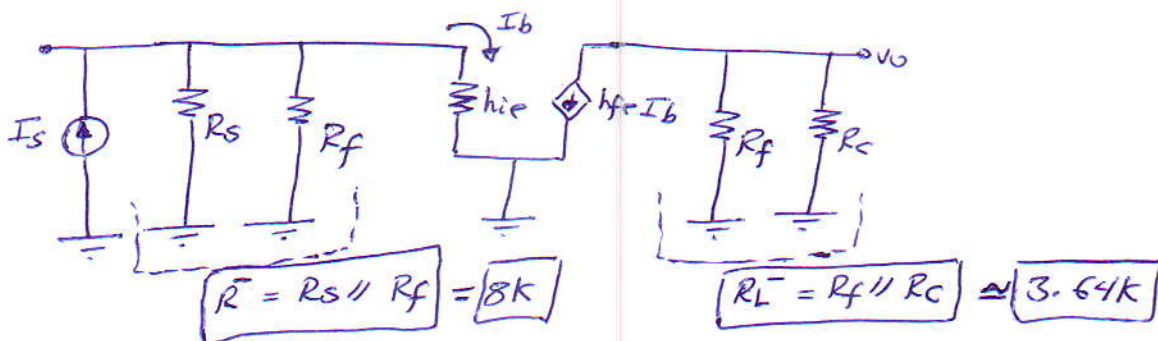
Step ②: To find input circuit ( $V_o = 0$ )



Step ③: To find output circuit ( $V_i = 0$ )



Step ④: Basic amplifier circuit without F.B.



$$R_M = \frac{V_o}{I_s} = \frac{-I_o R_L}{I_s} = \frac{-I_b h_{fe} R_L}{I_s} = \frac{-h_{fe} R_L}{I_s} * I_s * \frac{(R_s \parallel R_f)}{(R_s \parallel R_f) + h_{ie}}$$

$$\Rightarrow R_M = \frac{-50 * 3.64k * 8k}{8k + 1.1k} = -160k\Omega$$

to be continue

$$\beta = \frac{I_f}{V_o} = \frac{1}{V_o} \cdot \frac{V_c - V_o}{R_f} = \frac{-1}{R_f} = \frac{-1}{40} = \boxed{-0.025 \text{ mA/V}}$$

$$D = 1 + \beta R_M = 1 + (-0.025 \times 10^{-3})(-160 \times 10^3) = \boxed{5}$$

$$R_{Mf} = \frac{R_M}{D} = \frac{-160 \text{ k}}{5} = \boxed{-32 \text{ k}} = A_f$$

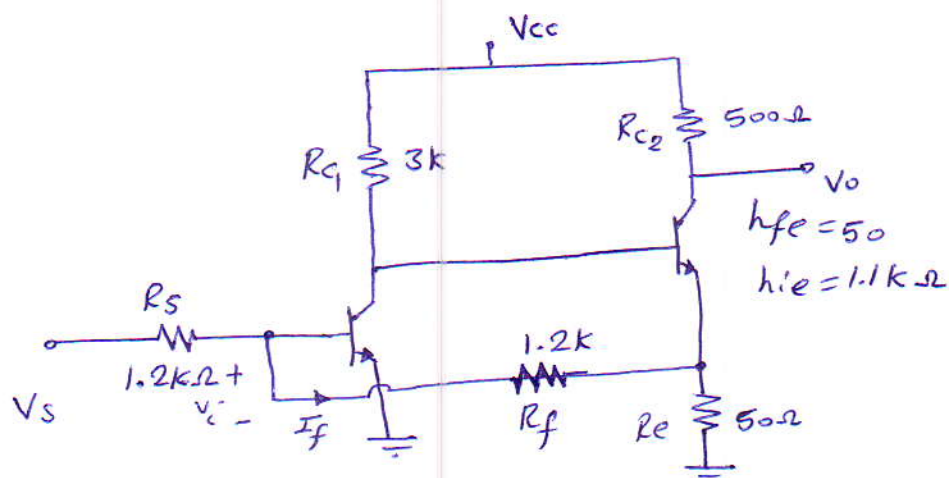
$$A_{vf} = \frac{V_o}{V_s} = \frac{V_o}{I_s R_s} = \frac{R_{Mf}}{R_s} = \frac{-32 \text{ k}}{10 \text{ k}} = \boxed{-3.2}$$

$$Z_{if} = Z_i / D = \frac{R_s \parallel R_f \parallel h_{ie}}{5} = \frac{968}{5} \approx \boxed{193 \Omega}$$

$$Z_{of} = \frac{Z_o}{D} = \frac{R_c \parallel R_f}{5} = \frac{3.64 \text{ k}}{5} = \boxed{728 \Omega}$$

~ ~ ~ ~ ~

Ex: For the circuit shown; Determine  $A_{vf}$ ,  $Z_{if}$  and  $Z_{of}$



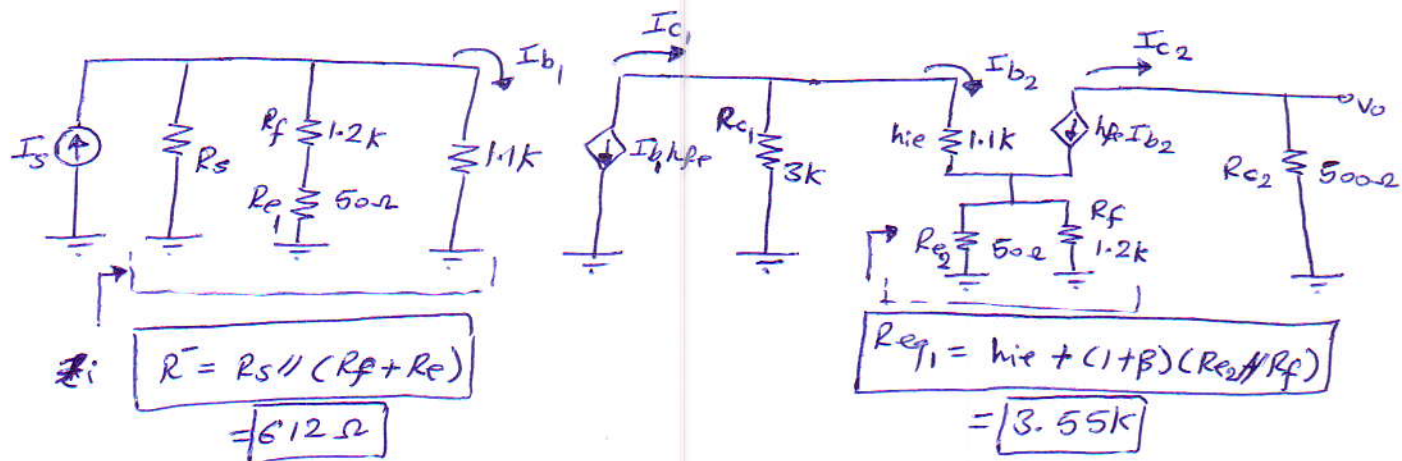
Solution:

step ①: F.B type is current-shunt

Steps ② and ③ will be appear in step ④

→  $Z_{if}$

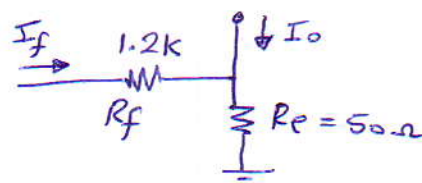
step 4: Basic amplifier circuit without F.B.



$$\beta = \frac{I_f}{I_o}$$

$$I_f = I_o \times \frac{R_e}{R_e + R_f} \Rightarrow \beta = \frac{I_f}{I_o} = \frac{R_e}{R_e + R_f}$$

$$\beta = \frac{50}{50 + 1.2k} = 0.04$$



$$A_T = \frac{I_{c2}}{I_s} = \frac{I_{c2}}{I_{b2}} \cdot \frac{I_{b2}}{I_{c1}} \cdot \frac{I_{c1}}{I_{b1}} \cdot \frac{I_{b1}}{I_s}$$

$$I_{c2} = -h_{fe} I_{b2} \Rightarrow \frac{I_{c2}}{I_{b2}} = -50$$

$$I_{c1} = -I_{b1} h_{fe} \Rightarrow \frac{I_{c1}}{I_{b1}} = -50$$

$$I_{b2} = +I_{c1} \times \frac{3k}{3k + 3.55k} \Rightarrow \frac{I_{b2}}{I_{c1}} = +0.458$$

$$I_{b1} = I_s \times \frac{612}{612 + 1.1k} \Rightarrow \frac{I_{b1}}{I_s} = 0.357$$

نتیجه

(56)

$$A_{I_T} = (-50)(-50)(0.458)(0.357) = \boxed{408}$$

$$D = 1 + \beta A_{I_T} = 1 + (0.04)(408) = \boxed{17.32}$$

$$A_{V_f} = \frac{V_o}{V_s} = \frac{-I_{C2} R_{C2}}{I_S R_S} = A_{I_f} * \frac{R_{C2}}{R_S}$$

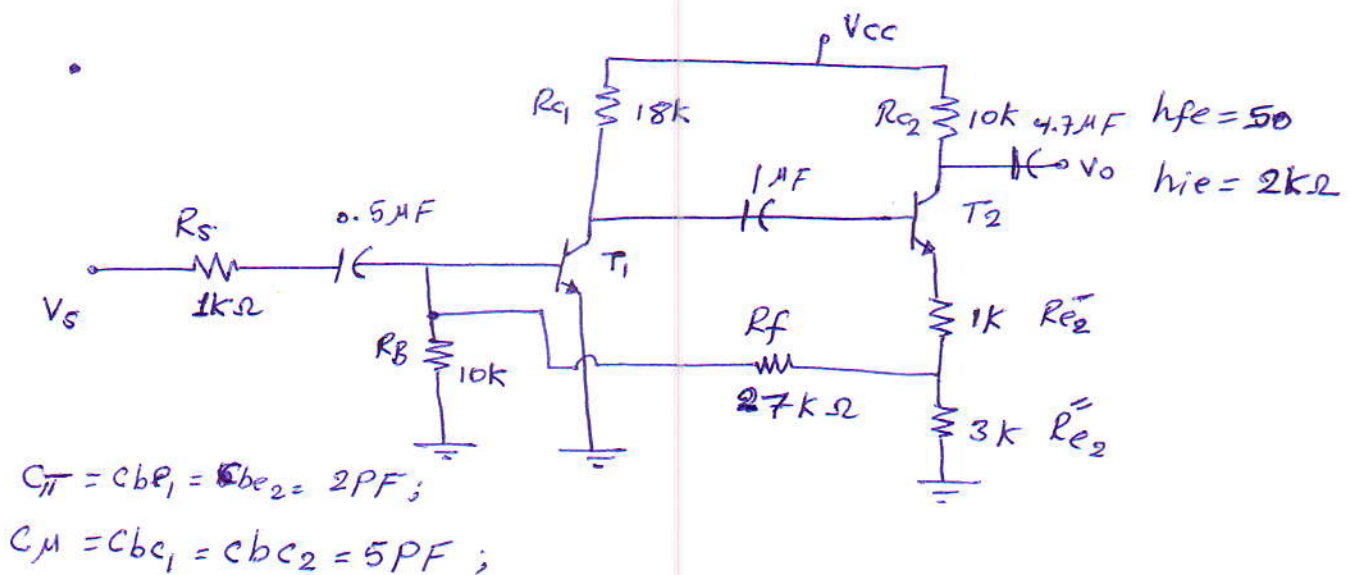
$$A_{I_f} = \frac{408}{17.32} \approx \boxed{23.6} \Rightarrow A_{V_f} = 23.6 * \frac{500}{1.2k} = \boxed{9.83}$$

$$R_i = R \parallel R_{ie} = 612 \parallel 1.1k = \boxed{394 \Omega} \Rightarrow Z_{if} = \frac{394}{17.32} \approx \boxed{23 \Omega}$$

$$Z_{of} = R_{C2} * D = 500 * 17.32 = \boxed{8.6 k\Omega}$$

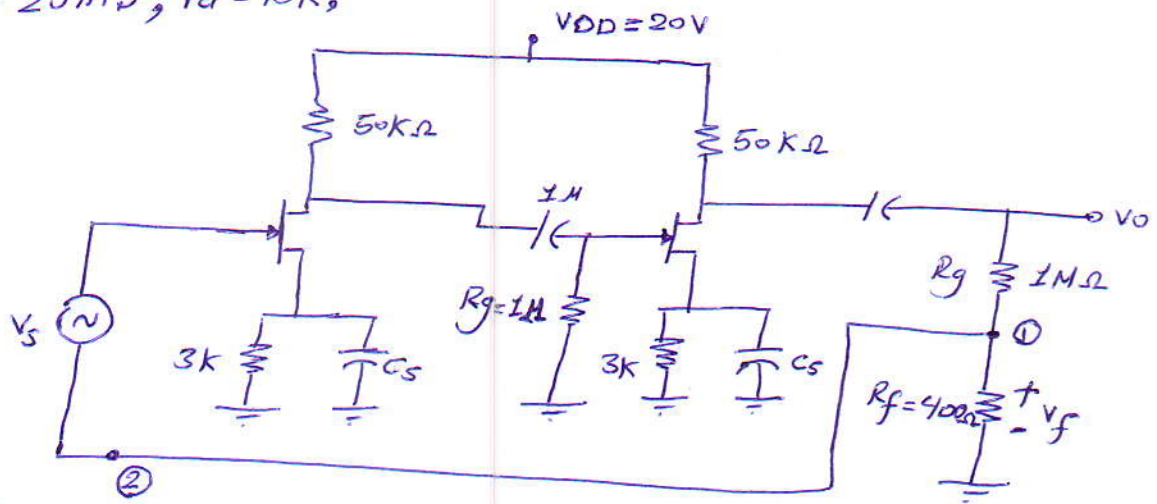
H.w1: Prove that  $Z_{if} = Z_i (1 + A\beta)$  and  $Z_{of} = Z_o (1 + A\beta)$  for the current-series connection?

H.w2: For the ckt shown below; Determine  $A_{V_f}$ ,  $Z_{if}$  and  $Z_{of}$ ?  
After that calculate the upper cutoff freq. and the lower cutoff freq. after and before F.B?



Ex: For the circuit shown below; find  $A_{vf}$  and  $Z_{of}$  given that

$g_m = 20 \text{ mS}$ ,  $r_d = 10 \text{ k}\Omega$ ,



Solution:

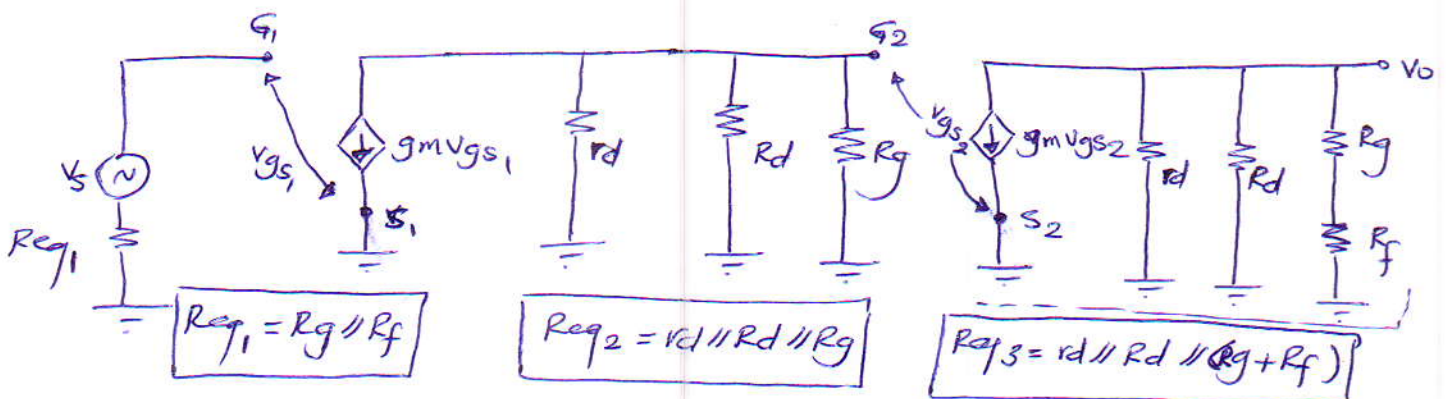
Step 1 F.B type is voltage-series (voltage amplifier)

نلاحظ من الشكل اننا باين النقطة رقم 1 تم اضافته فولتية الدخل في voltage اما نقطة رقم 2 فانه مقاومته  $R_f$  تكون على فولتية  $(V_f)$  يتم سارتها مع فولتية المصدر  $(V_s)$  وبالتالي هي series

Step 2 To find  $i_p$  circuit ( $V_o = 0$ )

Step 3 To find  $o_p$  circuit ( $I_i = 0$ )

Steps 2 and 3 will be appear in step 4



$$R_{eq1} = 1M // 400\Omega \approx \boxed{400\Omega}, \quad R_{eq2} = 10k // 50k // 1M = \boxed{8.26k\Omega}$$

$$R_{eq3} = r_d // R_d // (R_g + R_f) = 10k // 50k // (1M + 400) \approx \boxed{8.26k\Omega}$$

$$V_{gs1} = V_{g1} - V_{s1} \stackrel{\text{D.O.}}{=} V_s$$

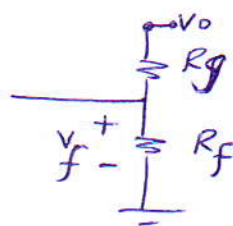
$$\frac{V_{o1}}{V_s} = A_{v1} \Rightarrow A_{v1} = -g_m R_{eq2} = A_{v2}$$

$$\Rightarrow A_{v1} = -20 \times 10^{-3} \times 8.26 \times 10^3 = \boxed{-165.2} = A_{v2}$$

$$\therefore A_{vT} = A_{v1} \cdot A_{v2} = (-165.2)(-165.2) = \boxed{27291}$$

$$D = 1 + \beta A; \quad \beta = \frac{V_f}{V_o}$$

$$V_f = V_o \times \frac{R_f}{R_f + R_g}$$



$$\Rightarrow \beta = \frac{V_f}{V_o} = \frac{400}{400 + 10^6} = \boxed{4 \times 10^{-4}}$$

$$\therefore D = 1 + \beta A_{vT} = 1 + (4 \times 10^{-4})(27291) \approx \boxed{12}$$

$$\Rightarrow A_{vf} = \frac{A_{vT}}{D} = \frac{27291}{12} = \boxed{2274.25}$$

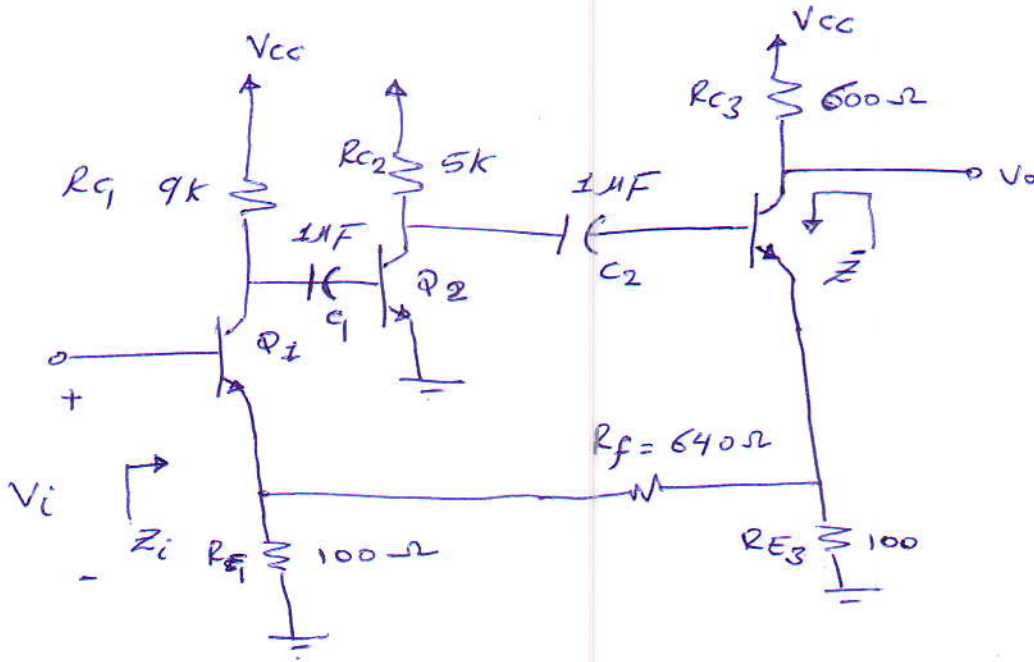
$$Z_{of} = Z_o / (1 + \beta A_{vT}) = (R_{eq3}) / (12)$$

$$\therefore Z_{of} = \frac{8.26k}{12} = \boxed{688\Omega} \quad \text{decrease due to voltage sampling}$$

①

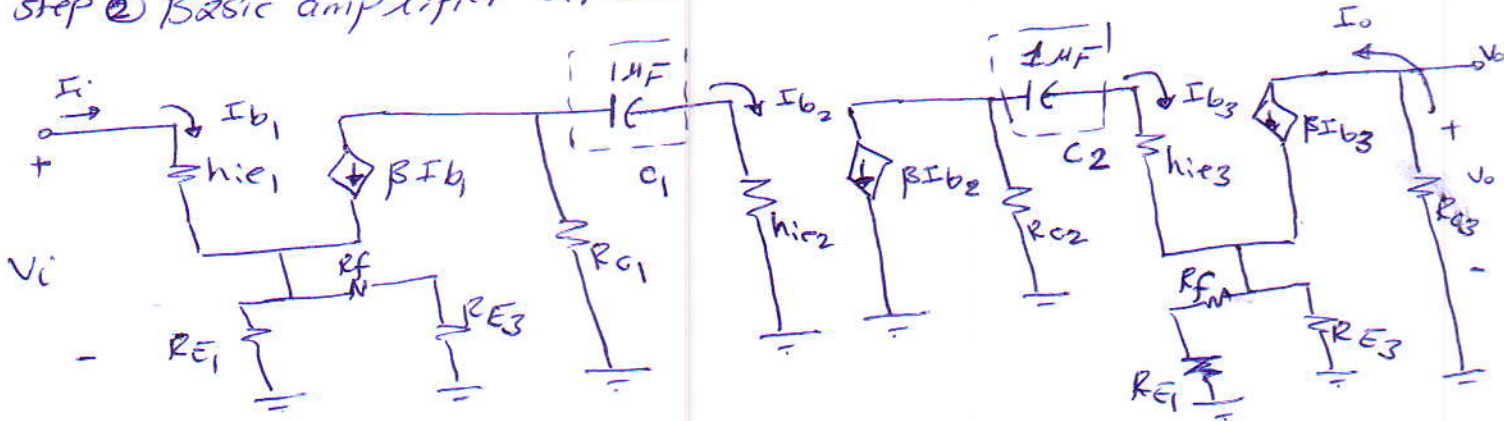
Ex: For the circuit shown below, determine  $A_{vf}$ ,  $Z_{if}$ ,  $Z_{of}$ ,  $Z_i$  and  $f_L$  (After and before feedback)?

$I_{C1} = 0.6 \text{ mA}$ ,  $I_{C2} = 1 \text{ mA}$ ,  $I_{C3} = 4 \text{ mA}$ ,  $h_{fe} = 100$



Solution:

Step 1 F.B type is current-series  
Step 2 Basic amplifier circuit without F.B



ملاحظة: هذه الـ ac equivalent لا يجب ان توضع المتغيرات ولكن وضعت لغرض التوضيح  
ومن ثم تم تبسيطها كيف يتم احتساب قيم المقاربات ( $R_{th}$ ) لكل مرحلة

(2)

∴ F.B type is current-series &  $A = \frac{I_o}{V_i}$  (transconductance amplifier)

$$A = \frac{I_o}{V_i} \quad ; \quad V_i = I_i Z_b = I_{b1} Z_b = I_{b1} (h_{ie1} + (1+\beta)(R_{E1} \parallel (R_f + R_{E3}))$$

$$r_{e1} = 41.7 \Omega$$

$$r_{e2} = 25 \Omega$$

$$r_{e3} = 6.25 \Omega$$

$$\therefore V_i = I_{b1} (13067.62) \quad \leftarrow \text{بعد تعويض القيم}$$

$$I_o = \beta I_{b3} = \boxed{100 I_{b3}}$$

$$I_{b3} = \frac{-\beta I_{b2} R_{C2}}{R_{C2} + h_{ie3} + (1+\beta)(R_{E3} \parallel R_f + R_{E1})} = \boxed{-34.43 I_{b2}}$$

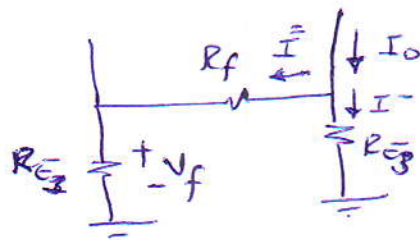
$$I_{b2} = \frac{-\beta I_{b1} R_{C1}}{R_{C1} + h_{ie2}} = \boxed{-78.26 I_{b1}}$$

$$\therefore A = \frac{(-78.26)(-34.43)(100) I_{b1}}{I_{b1}(13067.62)} = \boxed{20.7} \text{ A/V}$$

$$\beta = \frac{V_f}{I_o}$$

$$V_f = I^- R_{E1}$$

$$= \frac{I_o * R_{E3}}{R_{E3} + R_f + R_{E1}} * R_{E1} \quad \text{FD} \quad \beta = \boxed{11.9 \Omega}$$



3

$$D = 1 + \beta A = 1 + (11.9)(20.7) = \boxed{247.33}$$

$$A_f = \frac{A}{D} = \frac{20.7}{247.33} \approx \boxed{83.7 \text{ mA/V}}$$

$$Z_{if} = D Z_i = D (h_{ie1} + (1 + \beta)(R_{E1} \parallel R_f + R_{E3})) \approx \boxed{3.24 \text{ M}\Omega}$$

$$\bar{Z} = \frac{R_{C2} + h_{ie3}}{\beta_3 + 1} + (R_{E3} \parallel R_f + R_{E1}) = \boxed{143.8 \Omega}$$

$$Z_{of} = D \bar{Z} = 247.33 \times 143.8 \approx \boxed{35.6 \text{ k}\Omega}$$

$$f_{Lc1} = \frac{1}{2\pi R_{th1} C_1} \quad ; \quad R_{th1} = h_{ie2} + R_{C1} = 2.5 \text{ k} + 9 \text{ k} = \boxed{11.5 \text{ k}\Omega}$$

$$\Rightarrow f_{Lc1} = \frac{1}{2\pi (11.5 \text{ k})(1 \mu)} = \boxed{13.84 \text{ Hz}} \text{ before F.B}$$

$$\text{After F.B } (f_{Lc1})_F = \frac{f_{Lc1}}{D} = \frac{13.84}{247.33} = \boxed{0.056 \text{ Hz}} \quad \begin{array}{l} \text{تقریباً صف} \\ \text{بعد اضماعه ال F.B} \end{array}$$

$$f_{Lc2} = \frac{1}{2\pi R_{th2} C_2} \quad ; \quad R_{th2} = R_{C2} + h_{ie3} + (1 + \beta)(R_{E3} \parallel R_f + R_{E1}) = \boxed{14.5 \text{ k}\Omega}$$

$$\Rightarrow f_{Lc2} \approx \boxed{11 \text{ Hz}} \text{ before F.B}$$

$$\text{After F.B } (f_{Lc2})_F = \frac{11}{247.33} = \boxed{0.044 \text{ Hz}}$$

**Q1:** The circuit shown in figure (1) has  $\beta=120$ ,  $V_{CE}=4.47V$ ,  $C_{be}=40pF$ ,  
 $C_{bc}=1.5pF$ ,  $C_{ce}=5pF$ ,  $C_{wi}=4pF$  and  $C_{wo}=8pF$ .

1. Find the bandwidth, if cutoff frequency of  $C_c$  is 2.895Hz?
  2. Sketch the frequency response using Bode plot?
  3. Calculate the frequency and  $(A_v/A_{v_{mid}})dB$  at which the gain drops to 50% of its maximum value?
- 40 Mark**

**Q2:**

- a) For the circuit shown in figure (2) has  $\beta_1=200$ ,  $\beta_2=150$ ,  $h_{ie1}=20k\Omega$ ,  
 $h_{ie2}=7.5k\Omega$ .
1. Find  $A_{vf}$  and  $Z_{if}$ ?
  2. If the first stage adds 1V as a noise voltage before F.B, determine the noise value for two stages before and after F.B?
- b) What are the effect of negative feedback on gain and bandwidth?  
 Confirm your answer by drawing and equations.
- 10 Mark**

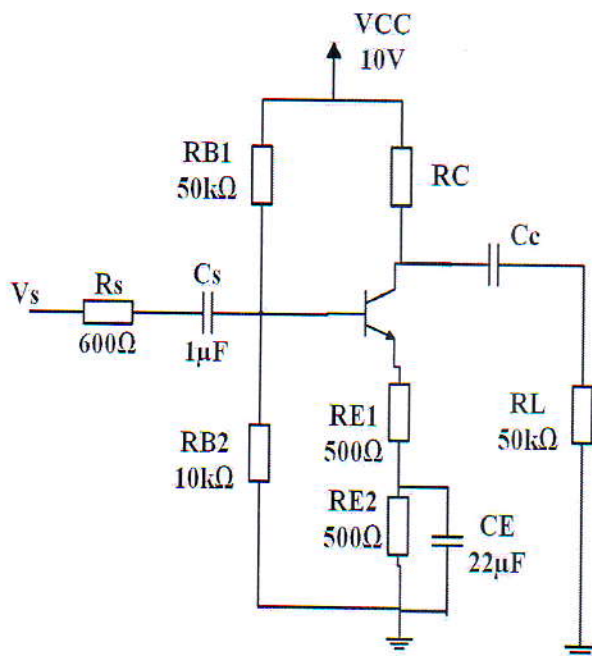


Fig (1)

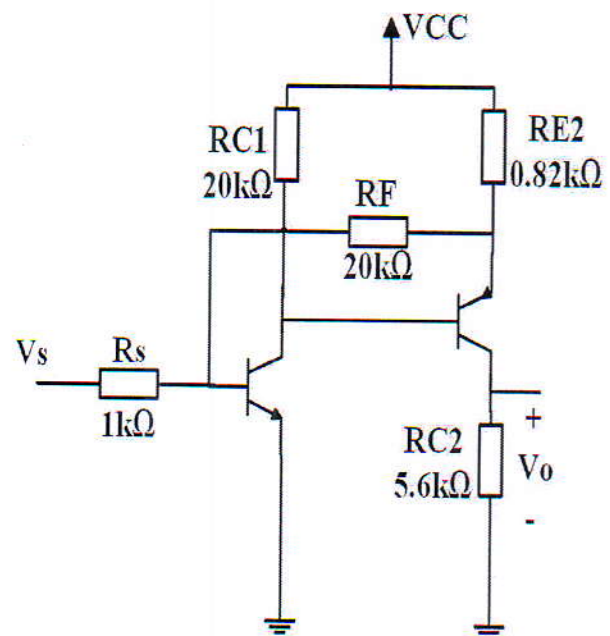


Fig (2)

**Q1:** The circuit shown in figure (1) has  $\beta=120$ ,  $V_{CE}=4.47V$ ,  $C_{be}=40pF$ ,  $C_{bc}=1.5pF$ ,  $C_{ce}=5pF$ ,  $C_{wi}=4pF$  and  $C_{wo}=8pF$ .

1. Find the bandwidth, if cutoff frequency of  $C_c$  is 2.895Hz?
  2. Sketch the frequency response using Bode plot?
  3. Calculate the frequency and  $(A_v/A_{v_{mid}})dB$  at which the gain drops to 50% of its maximum value?
- 40 Mark**

**Q2:**

a) For the circuit shown in figure (2) has  $\beta_1=200$ ,  $\beta_2=150$ ,  $h_{ie1}=20k\Omega$ ,  $h_{ie2}=7.5k\Omega$ .

**50 Mark**

1. Find  $A_{vf}$  and  $Z_{if}$ ?
  2. If the first stage adds 1V as a noise voltage before F.B, determine the noise value for two stages before and after F.B?
- b) What are the effect of negative feedback on gain and bandwidth?  
Confirm your answer by drawing and equations.
- 10 Mark**

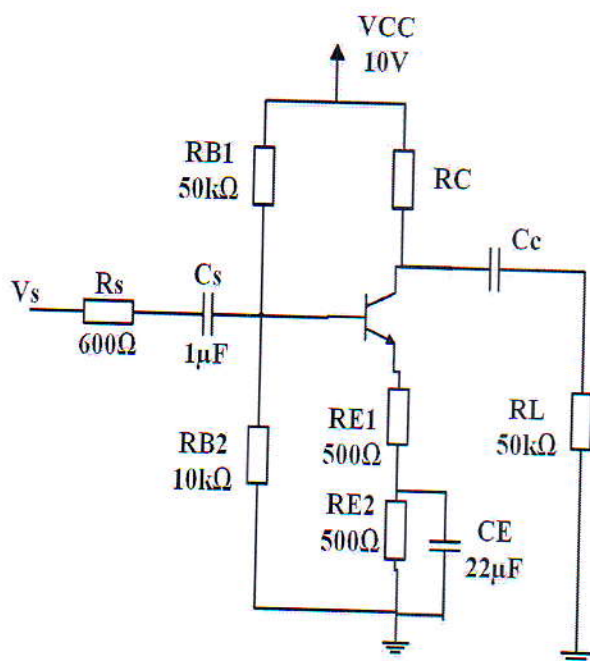


Fig (1)

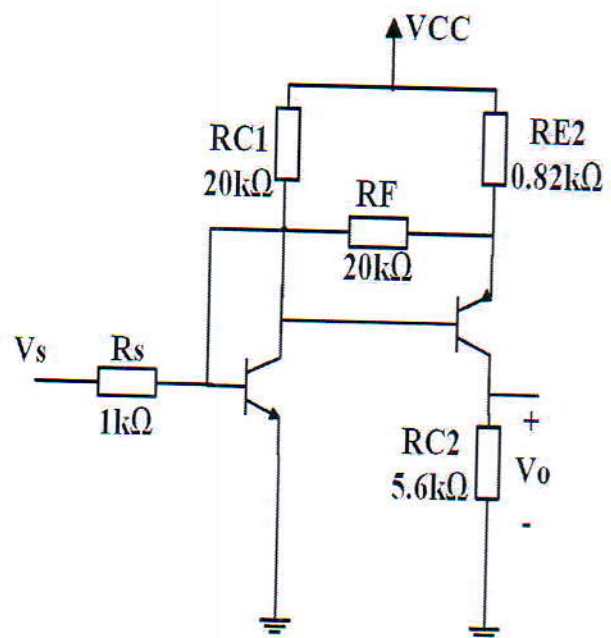
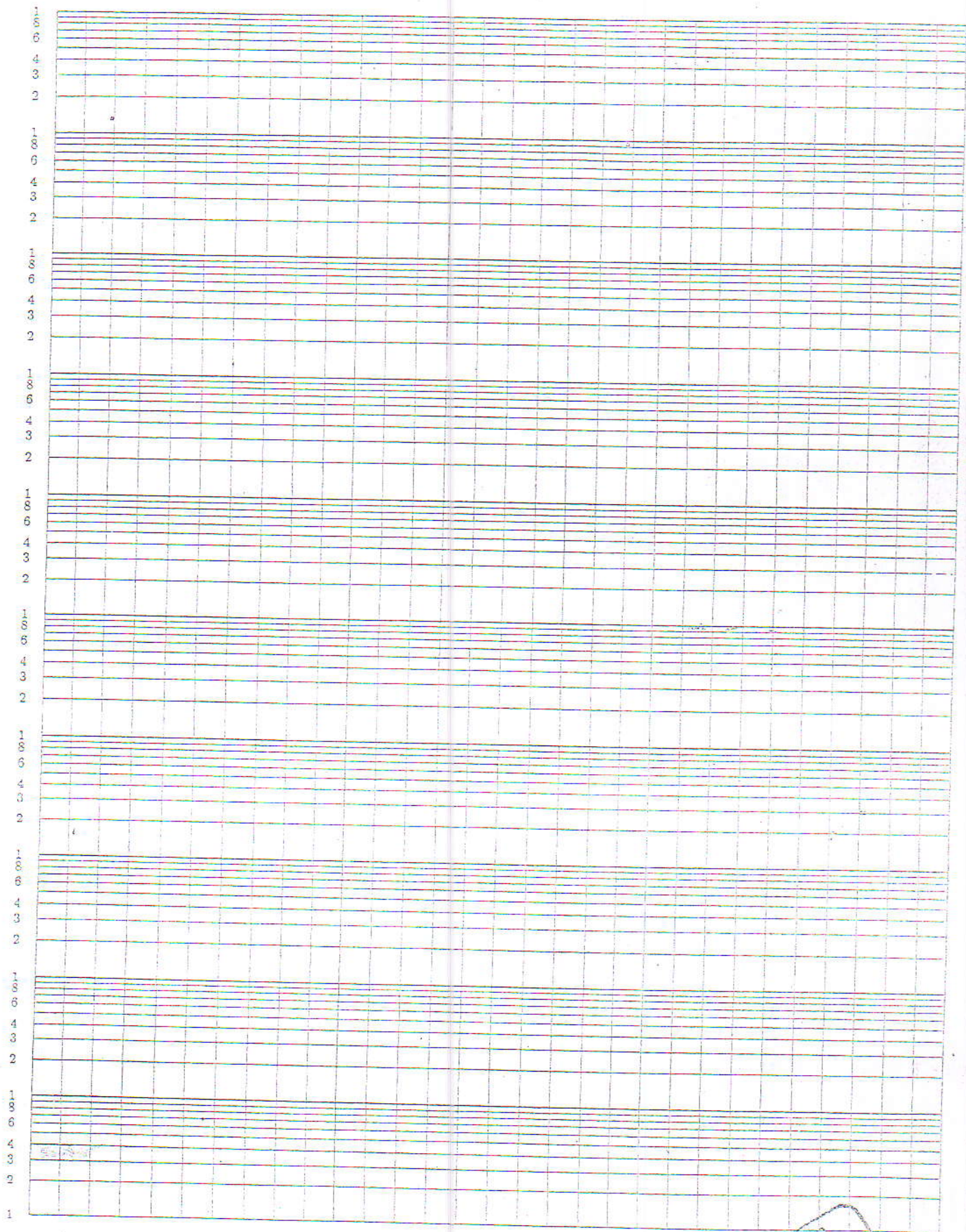


Fig (2)

Lecturer

Good Luck

Saad Gazai Muttalak



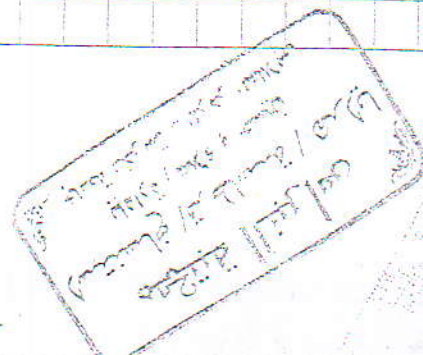
10

10

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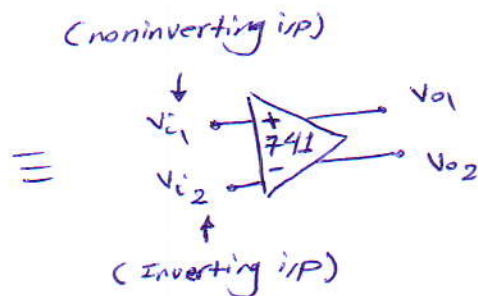
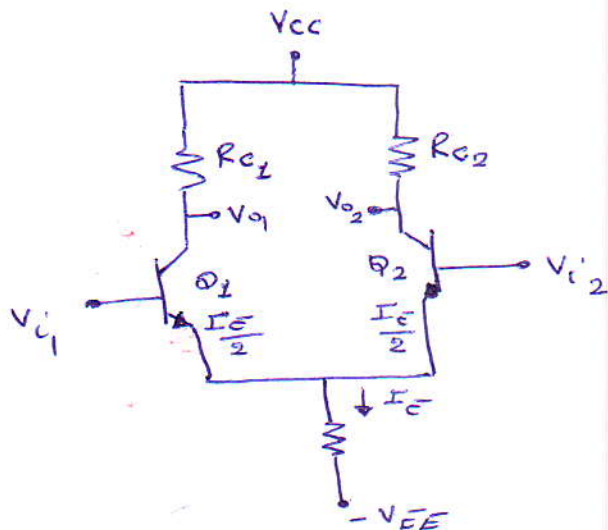
10-11-12



# Differential and Operational Amplifier :

Differential Amplifier circuit: is an arrangement of transistors which allow the difference between two signal sources to be amplified and the output is proportional to the difference between these two inputs as shown in figure below.

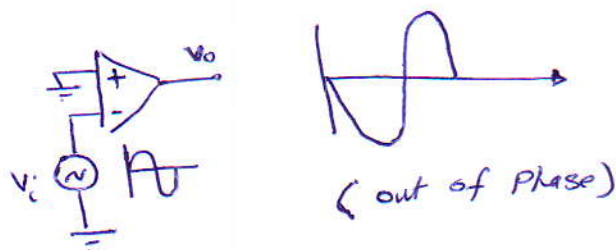
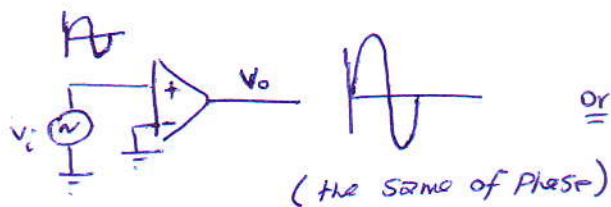
المرحلة الأولى (Differential Amp) هي عبارة عن زوج من الترانزستورات المتطابقة (IC) كمرحلة إدخال (Input stage) حيث أن (IC 741) يتولى بواجب على 24 ترانزستور وبتقنية الجاوس IC مع مرادف حيث أن المرادف عبارة عن (Diff. Amp)



\* يجب أن يكون كلا الترانزستورين  $Q_1$  و  $Q_2$  متطابقين (match) لأن أي اختلاف بينهما يؤدي إلى اختلاف المرادف، ليأثر به الآخر.

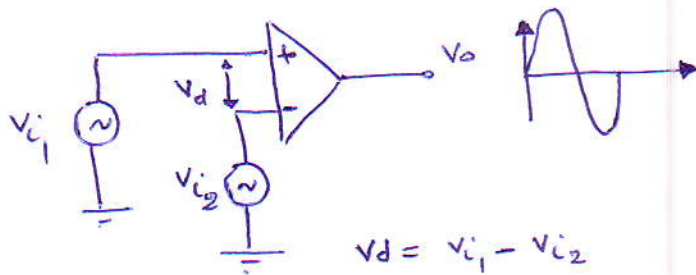
## ① Single-Ended Input:

Single ended i/p operation results when the i/p signal is connected to one i/p with the other i/p connected to ground as shown below.



## ② Double-Ended (Differential) Input :

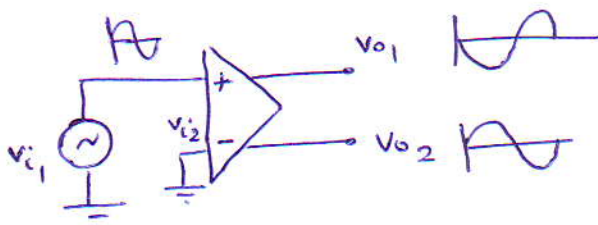
من المحتمل ان كلا الطرفين تطبق عليهما موجتين وبالتالي فان نتيجة الاخراج تكون بنفس طور نتيجة طرح الموجتين وكما موضح في الشكل ادناه، حيث اذا كانت نتيجة الطرح موجبة فان الاخراج يكون كذلك موجب والعكس بالعكس



Double-Ended (Differential) operation

## ③ Double-Ended Output :

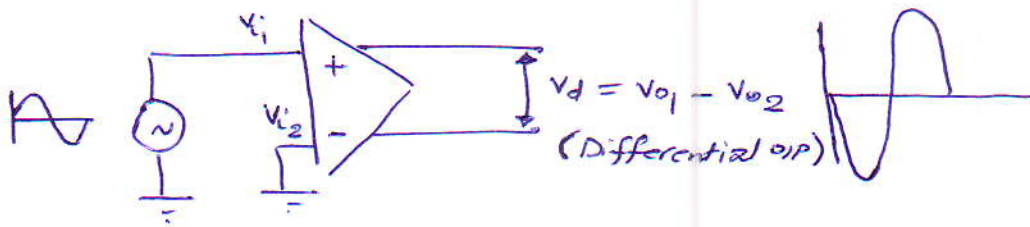
\* The signal applied to the Plus i/p results in two amplified outputs of opposite Polarity as shown below.



\* يكون  $V_{o1}$  عكس قطبية  $V_{o2}$  الاشارة  $V_i1$   
لان الاخراج يكون من CE ترانزستور  
وهو يعطي  $180^\circ$  فرق طور .

\* The 2nd case is the same operation with single o/p measured between output terminals (not with respect to ground).

تابع

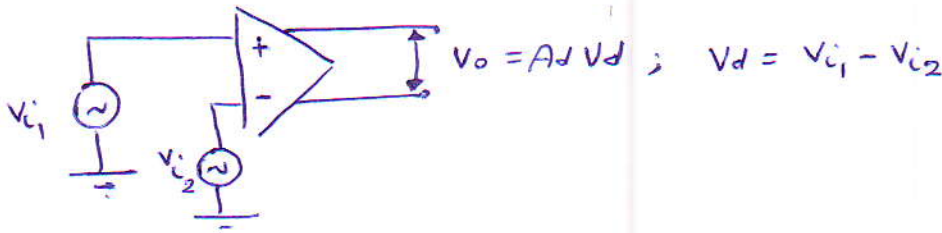


For example  $v_{o1} = -10$  and  $v_{o2} = 10 \Rightarrow v_d = -10 - (10) = \boxed{-20}$   
and can be called floating output signal

\* Notes:

\* مخرج الـ أ.م.ف.ج. يكون طرئياً بين  $v_{o1}$  و  $v_{o2}$  ولا يكون مربوط على (ground)

\* The figure shown below is called differential i/p, differential o/p operation (fully differential operation)



#### ④ Common-Mode operation:

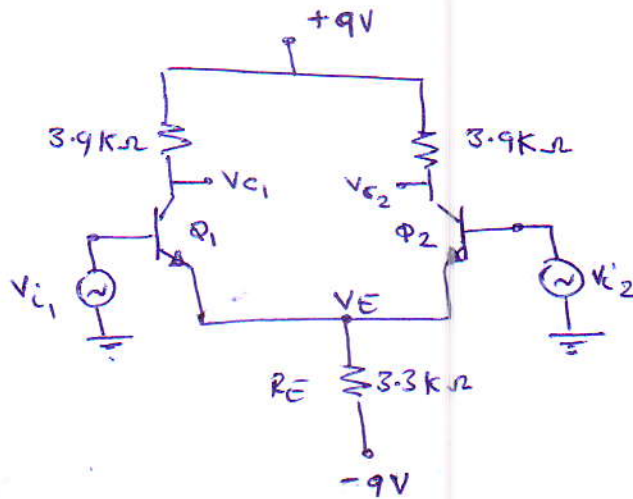
عندما يتم ادخال نفس قيمة المولدة عند طرفي الازدواج فانه المخرج يكون من (Differential i/p)

$$v_{i1} = v_{i2}$$

وذلك لان قيمة  $v_d = v_{i1} - v_{i2} = 0$ . حيث اذا كان المخرج يساوي صفراً فانه قيمة الـ Signal of Noise  
تم رفضها وتسمى هذه الحالة Common mode rejection ولكن في الحقيقة لا يكون المخرج  
يساوي صفراً بل انه يكون قيمة صفراً لذلك يتم استخدام D.C. offset

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Ex: Determine  $I_E$ ,  $I_{C1}$ ,  $I_{C2}$ ,  $V_{C1}$  and  $V_{C2}$  in the circuit below?



Solution:

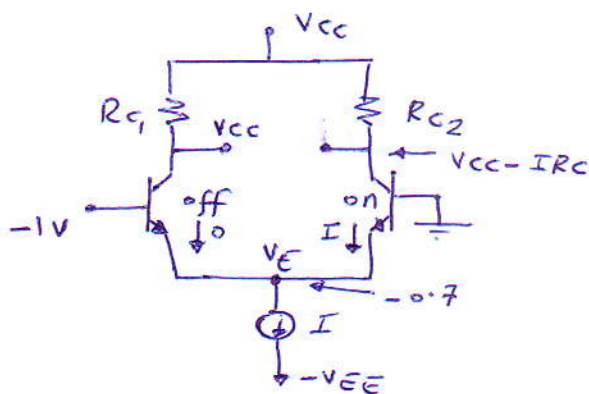
$$I_E = \frac{-V_{BE} + V_{EE}}{R_E} = \frac{9 - 0.7}{3.3 \text{ k}\Omega} = \boxed{2.5 \text{ mA}}$$

$$I_{C1} = I_{C2} = \frac{I_E}{2} = \frac{2.5 \text{ mA}}{2} = \boxed{1.25 \text{ mA}}$$

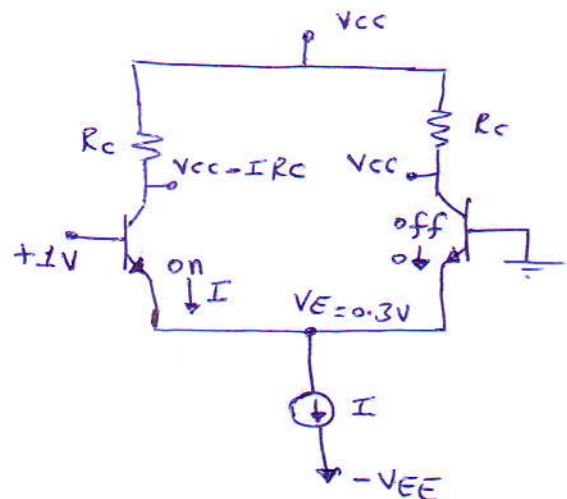
$$V_{C1} = V_{C2} = V_{CC} - I_C R_C = 9 - (1.25 \times 10^{-3})(3.9 \times 10^3) = \boxed{4.125 \text{ V}}$$

~ ~ ~ ~ ~

Basic Operations: To see how the BJT differential pair works, can be obtained two cases below.



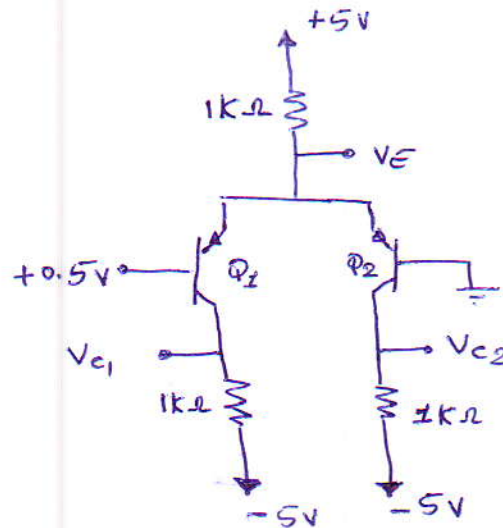
Case 1



Case 2

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EX: Find  $V_E$ ,  $V_{C1}$  and  $V_{C2}$  in the circuit below? Assume  $V_{BE} = 0.7$   
 $\alpha \approx 1$



Solution:

$Q_1$  is off and  $Q_2$  is on

$$V_E = V_{BE2} = 0.7V$$

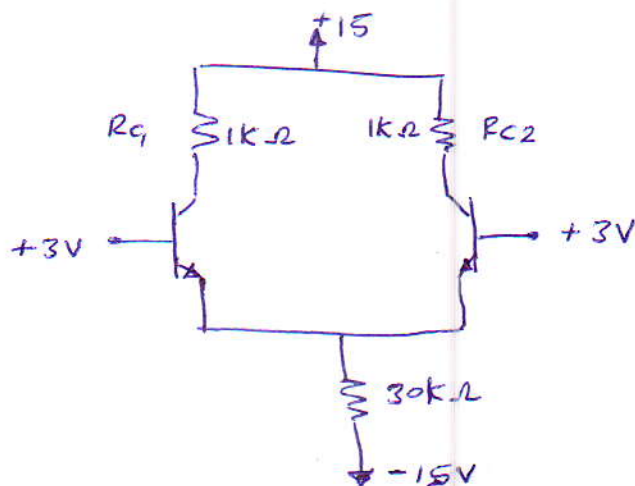
$$I_E = \frac{V_{EE} - V_E}{R_E} = \frac{5 - 0.7}{1k} = 4.3mA \approx I_{C2} \text{ because } I_{C1} = 0$$

$$V_{C2} = I_{C2} R_C - V_{CC} = (4.3mA)(1k) - 5 = -0.7V$$

$$V_{C1} = -5V \text{ because } Q_1 \text{ is off, thus } I_{C1} = 0$$

~~~~~

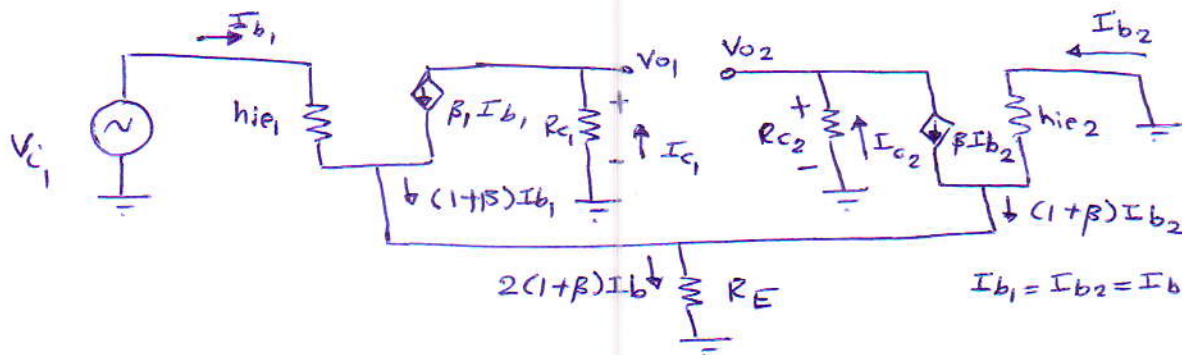
H.w: Determine  $V_E$ ,  $V_{C1}$  and  $V_{C2}$  in the circuit below?



## Ac Operation of Circuit:

### ① Single-Ended Ac voltage gain:

To calculate the Single-ended voltage gain ( $\frac{V_o}{V_i}$ ), apply signal to one input with the other connected to ground as shown below in ac equivalent circuit.



Assume two transistors are well matched, then

$$I_{b1} = I_{b2} = I_b$$

$$r_{i1} = r_{i2} = r_i = h_{ie} = \beta r_e$$

$R_E$  (very large) ideally infinite.

$$\Rightarrow I_b = \frac{V_i}{2r_i} = \frac{V_i}{2\beta r_e} \quad \text{--- ①}$$

$$V_o = -I_c R_c = -\beta I_b R_c \quad \text{--- ②} \quad \text{substitute equation ① in ② and we get:}$$

$$V_o = -\beta \left( \frac{V_i}{2\beta r_e} \right) R_c \Rightarrow \boxed{\frac{V_o}{V_i} = -\frac{R_c}{2r_e}}$$

ملاحظة: في الحقيقة ان مقاومة  $R_E$  هي توازي  $h_{ie2}$  ولكن جعل قسمة  $R_E$  كبيره لغرض جعل قيمه المقام قليله وبالتالي زياده الكسب ولكن هناك محدودات وهي انكم زياده  $R_E$  بتسبب فيه مشاكل لانه التيار يقل وبالتالي فان الترانزستور يتأثر بسبب تأثير الـ Biasing لذلك نلجأ الى current source

## ② Double-Ended Ac Voltage gains

In this case the signals applied to both inputs, the differential voltage gain is:

$$A_d = \frac{V_o}{V_d} = -\frac{R_c}{r_e}$$

$$V_d = V_{i1} - V_{i2}$$

## ③ Common- Mode operation of circuit:

It should also provide as small an amplification of the signal common to both inputs.

From the previous ac equivalent circuit in Page 64 we can write:

$$V_i - I_b r_i - 2(\beta + 1) I_b R_E = 0$$

$$\Rightarrow I_b (r_i + 2(\beta + 1) R_E) = V_i \quad \therefore I_b = \frac{V_i}{r_i + 2(1 + \beta) R_E} \quad \dots \textcircled{1}$$

$$\therefore V_o = -\beta I_b R_c \quad \dots \textcircled{2} \text{ subs. } \textcircled{1} \text{ in } \textcircled{2} \text{ and we get:}$$

$$\boxed{\frac{V_o}{V_i} = \frac{-\beta R_c}{r_i + 2(1 + \beta) R_E}} = A_c$$

نلاحظ ان قيمة الكسب المنخفضة  
(في حالة ادخال مؤلفتين متساويتين، طائفتي  
ال Diff Amp) يكون قليل حيث ان  
قيمة هذا الكسب تمثل علاقة عكسية  
مع noise rejection

## Constant current source :

لغرض جعل المقاومة المتغيرة في الـ Emitter  
للـ Differential Amplifier هي عالية وليس الوقت قيمة  
التيار غير قليلة هي بالإستعانة بـ Active load  
وهو مصدر تيار مع ترانستورات ومقاومات  
حيث يعطي قيمة تيار ثابتة وكذلك مقاومة  
عالية.

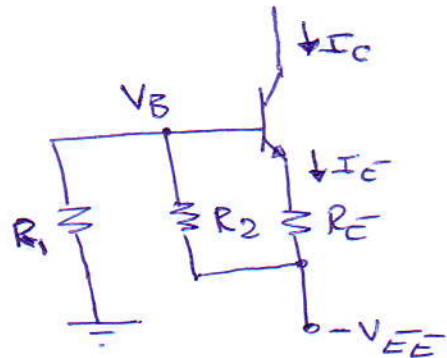
### ① Bipolar Transistor constant current source :

$I_E$  is desired constant current source shown in figure below  
and it's set by Resistor  $R_1$  and ( $R_2, R_E$ ) and also  $V_{EE}$

$$V_B = \frac{(-V_{EE}) R_1}{R_1 + R_2}$$

$$V_E = V_B - 0.7V$$

$$I_E \approx I_C = \frac{V_E - (-V_{EE})}{R_E}$$



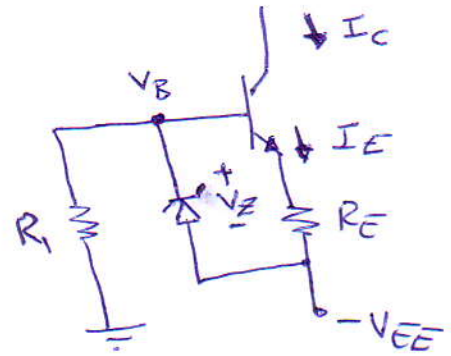
\* نلاحظ من الدائرة انه يتم تثبيت تيار  $I_C$  لانتقار مطلقاً على Differential circuit  
التي تكون عادة عند الـ collector

### ② Transistor - Zener constant current source :

يتم استبدال المقاومة  $R_2$  بـ Zener diode لزيادة استقرارية الدائرة حيث عند زيادة  
درجة الحرارة تقل  $V_{BE}$  وبالتالي يزداد تيار الـ  $I_E$  وتزداد فولتية  $V_E$   
وبالتالي يتغير قيمة تيار  $I_C$  لذلك نستخدم الـ Zener لغرض الاستقرارية لـ  $I_C$   
وكما موضح في الشكل  
يتبع

$$I_C \approx I_E = \frac{V_Z - V_{BE}}{R_E}$$

\* نلاحظ ان العلاقة اعلاه بين تيار  $I_C$   
لا تتغير مطلقاً على  $V_{EE}$  ولا على  $V_{BE}$  (زاد)  
استقرار تيار  $(I_C)$



constant current source/using Zener diode

### ③ MOSFET constant Source :

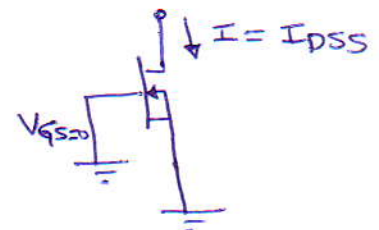
The MOSFET transistor provides an excellent constant current source. If the MOSFET device is biased at  $V_{GS} = 0$ , the constant current is set at  $I_{DSS}$ .

$$I_D = I_{DSS} \left(1 - \frac{V_{GS}}{V_P}\right)^2$$

where  $V_{GS} = 0$

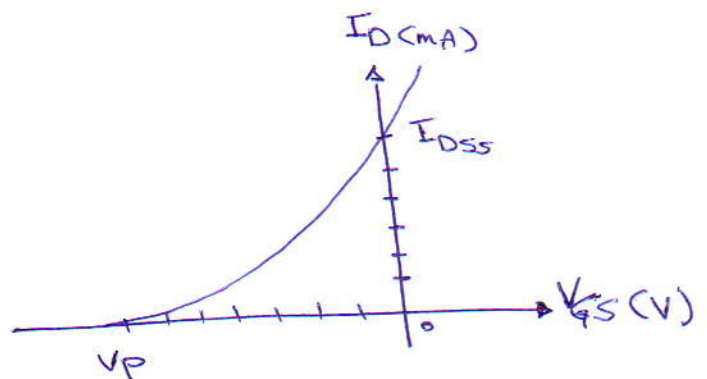
$$\Rightarrow I_D = I_{DSS} \text{ (constant current)}$$

and high input impedance



Depletion MOSFET

\* نلاحظ ان العلاقة اعلاه بين تيار  $I_D$   
لا تتغير مطلقاً على  $V_{GS}$  ولا على  $V_{DS}$  (زاد)  
استقرار تيار  $(I_D)$

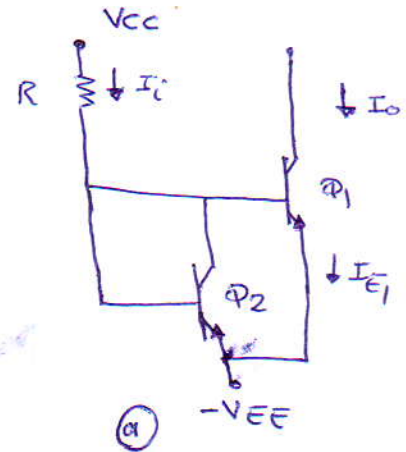


#### 4) Current Mirror constant current source:

##### a) current mirror for low current values:

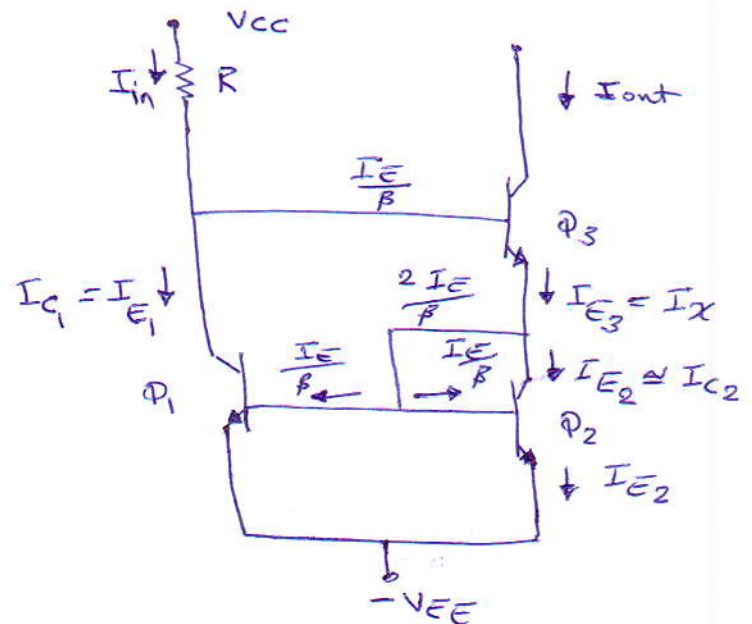
The current source ( $I_o$ ) will remain at the constant value set by  $V_{CC}$  and  $R$

\* نريد ان قيمة تيار  $(I_o)$  تكون قليلة لا تبالوي  
علاوة  $(\beta I_{E1})$



##### b) Current mirror with higher current and o/p impedance:

\* لنقوم بتصميم current mirror في الدوائر المتكاملة حيث يتم صنع الترانزستورات بنفس الوقت لغاية ان يكونوا متطابقين (matched or identical) حيث يكون تيار  $(I_E)$  لـ  $Q_1$  و  $Q_2$  نفس التيار وبالتالي فان تيار المار بـ  $Q_1$  و  $Q_2$  هو  $V_{CC}$  يكون نفس تيار لـ  $Q_2$  وانها مآه تكون المعبره لذلك نسمي current mirror.



$$I_{C1} \approx I_{E1} \approx I_X$$

(b) current source with higher o/p impedance

\* matched or identical لغاية ان قيمة  $V_{BE}$  متساوية للتأثيرات المتفرقة، ونضع  $\beta$

## Analysis of current mirror circuit:

$$I_B = \frac{I_E}{1 + \beta} \approx \frac{I_E}{\beta}$$

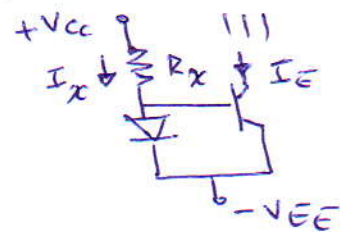
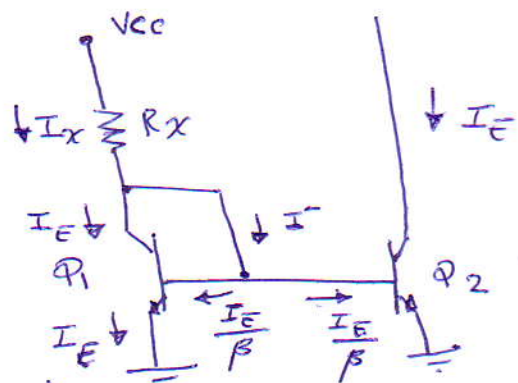
and  $I_C \approx I_E$

$I_E$  (for both transistor is the same)

$$I^- = \frac{I_E}{\beta} + \frac{I_E}{\beta} = \frac{2 I_E}{\beta}$$

$$I_X = I_E + I^- = I_E + \frac{2 I_E}{\beta} = \frac{(\beta + 2)}{\beta} I_E \approx \boxed{I_E}$$

$$I_X = \frac{V_{CC} - V_{BE}}{R_X}$$



في دارة المرآة،  $I_X$  يساوي تقريباً  $I_E$  في  $Q_2$  (current mirror)

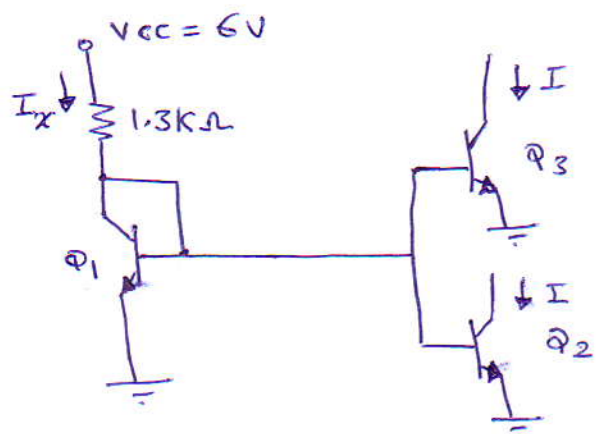
Ex: Calculate the current  $I$  through each of transistor  $Q_2$  and  $Q_3$  in the circuit below?

Solution:

$$\begin{aligned} I_X &= I_E + \frac{3 I_E}{\beta} \\ &= \left( \frac{\beta + 3}{\beta} \right) I_E \approx I_E \end{aligned}$$

$$I \approx I_X = \frac{V_{CC} - V_{BE}}{R_X} = \frac{6 - 0.7}{1.3 \text{ k}\Omega}$$

$$\Rightarrow \boxed{I = 4.08 \text{ mA}}$$



Ex: Design a current mirror source for a differential amplifier with current  $1\text{mA}$  for each transistor if  $V_{CC}=12\text{V}$  and  $V_{EE}=-6\text{V}$ .

Solution:

$$I_{E1} = I_{E2} = 1\text{mA} \text{ (given)}$$

$$\Rightarrow I_O = I_{E1} + I_{E2} = \boxed{2\text{mA}}$$

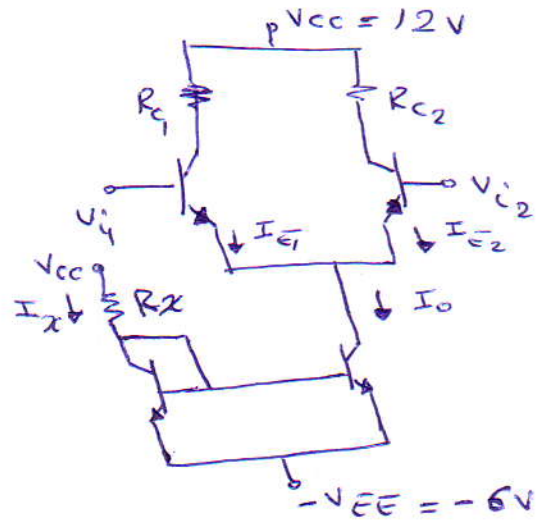
∴ Active load is a current mirror

$$\therefore I_O = I_X = \boxed{2\text{mA}}$$

$$\Rightarrow R_X = \frac{V_{CC} + V_{EE} - V_{BE}}{I_X}$$

$$= \frac{12 + 6 - 0.7}{2\text{m}} = \boxed{8.65\text{K}\Omega}$$

\* ملاحظة: رسم برآءه هو جند صطل وهو غير مظهر في السوال



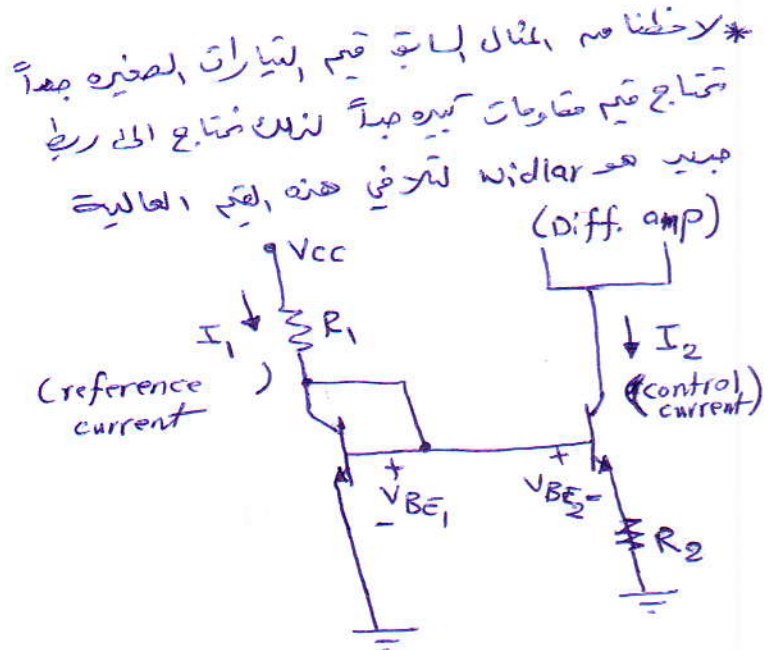
\* ملاحظة: اذا كانت قيمة تيار  $I_X$  تساوي  $20\mu\text{A}$  فانه قيمة المقاومة  $R_X$  تصبح  $(865\text{K})$  وهذه القيمة كبيرة يعجب او قد يكون مستحيل تصنيعها داخل  $\downarrow$   $(I_C)$  لذلك يجب ان تكون قيم التيارات منطوية وبالتالي تكون قيم المقاومات منطوية! بالاضافة الى ذلك فانه قيم التيارات العالية نسبياً تفهم ان كلا الترانزستورين غير متوازن (Diff) لها قيمة (biasing) جيدة.

### ⑤ Widlar current source :

for the current mirror example we see : a small reference current implies a large reference resistor, which is not always possible with conventional Integrated Circuit technology.

$$I_2 = \frac{KT}{R_2} \ln \left( \frac{I_1}{I_2} \right)$$

$KT$ : thermal voltage  
(26mV at 300K)



EX: Determine the value of resistor required for the Widlar current source, if the reference current is 1mA and the control current is 10μA ( $I_2$ ).

Solution:

$$R_2 = \frac{KT}{I_2} \ln \left( \frac{I_1}{I_2} \right)$$

$$\Rightarrow R_2 = \frac{26\text{mV}}{10\mu\text{A}} \ln \left( \frac{1\text{mA}}{10\mu\text{A}} \right) = \boxed{12\text{k}\Omega}$$

\* نلاحظ مع قيمة تيار صغيرة لـ  $I_2$  وهي (10μ) فإن قيمة المقاومة مقبولة وهي (12k) وبإمكاننا تصنيعها داخل الـ IC.

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Ex: Design widlar current mirror source to obtain the current at each transistor for differential amplifier equal to  $10\mu A$  and the reference is  $1mA$ . ( $V_{CC} = 12V$  and  $V_{EE} = -6V$ )

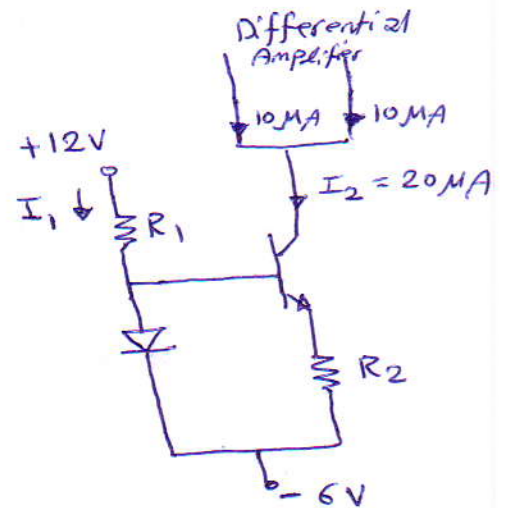
Solution:

$$R_1 = \frac{V_{CC} + V_{EE} - V_{diode}}{I_1 \text{ (reference)}}$$

$$= \frac{12 + 6 - 0.7}{1mA} = \boxed{17.3 K\Omega}$$

$$R_2 = \frac{kT}{I_2} \ln\left(\frac{I_1}{I_2}\right)$$

$$= \frac{26mV}{20\mu A} \ln\left(\frac{1mA}{20\mu A}\right) = \boxed{4.9 K\Omega}$$



Ex: Calculate the Source circuit currents for the figure shown below?

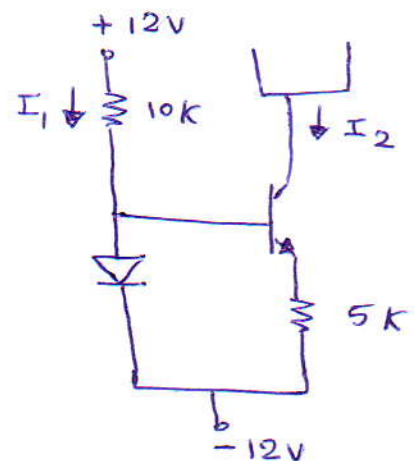
Solution:

$$I_1 = \frac{12 + 12 - 0.7}{10K} = \boxed{2.33 mA}$$

$$I_2 = \frac{kT}{R_2} \ln\left(\frac{I_1}{I_2}\right)$$

$$\Rightarrow I_2 = \frac{26mV}{5K} \left( \ln\left[ \frac{2.33 \times 10^{-3}}{I_2} \right] \right)$$

H-w: Try and error to find  $I_2$  value.



Input Resistance :

For differential amplifier with two inputs, there are two values of  $R_{in}$  (input resistance).

1-  $R_{in}(\text{diff})$  : difference mode resistance, which exist between two inputs.

2-  $R_{in}(\text{cm})$  : common mode resistance, which exist between each input and ground

$$* R_{in}(\text{diff}) = 2h_{ie} = 2\beta r_e$$

$$* R_{in}(\text{cm}) = 2\beta R_E \quad (R_E \text{ is the emitter resistance; if } R_E \text{ is replaced with current mirror source, the opp resistance associated with the current source})$$

EX: For the circuit shown below, determine the differential and common mode input resistances. The early voltage is 90V and  $\beta$  is 200. Assume that the Area of  $Q_1$  is one to fifth that of  $Q_3$ .

→ to be continue

(74)

Solution:

$$I_1 = I_{\text{reference}} = \frac{V_{CC} + V_{EE} - V_{BE}}{R_x}$$

$$= \frac{12 + 12 - 0.7}{30k} = \boxed{776 \mu A}$$

$$\therefore I_2 = \frac{I_1}{5} \text{ (because of emitter area)}$$

\* كل كات مضاعف 5 (emitter) أي كل 5 أيار  $I_1$  trans.  $I_2$   
 وبالمثل كل 5 أيار  $I_2$  مضاعف 5 أيار  $I_1$

$$\Rightarrow I_2 = \frac{776}{5} = \boxed{155 \mu A}$$

$$I_{E1} = I_{E2} = \frac{I_2}{2} = \frac{155 \mu}{2} = \boxed{77.5 \mu A}$$

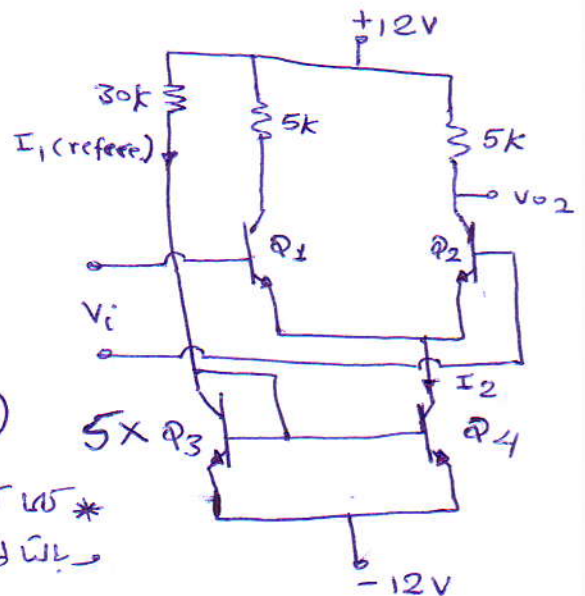
$$r_e = \frac{26mV}{77.5 \mu} = \boxed{335 \Omega} = r_{e1} = r_{e2}$$

$$R_{in}(\text{diff.}) = 2h_{ie} = 2\beta r_e = 2(200)(335) = \boxed{134 k\Omega}$$

$$R_{in}(cm) = 2\beta R_E \quad R_E: (\text{associated with current source})$$

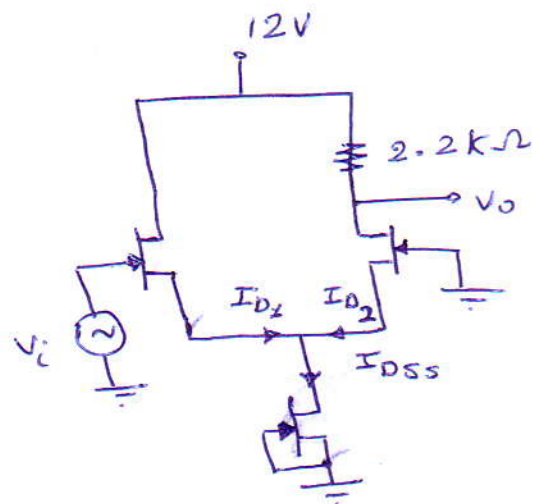
$$R_o(Q_4) = \frac{\text{early voltage}}{I_2} = \frac{90}{155 \mu} = \boxed{580 k\Omega} \text{ that equivalent to } R_E$$

$$\Rightarrow R_{in}(cm) = 2\beta R_E = 2(200)(580k) = \boxed{232 M\Omega}$$



Ex: For the circuit shown below, determine the gain, assume  $g_{m0} = 10 \text{ mS}$ .

Solution:



$$A_v = \frac{1}{2} g_m R_L = \frac{1}{2} g_m R_D$$

$$g_m = g_{m0} \left(1 - \frac{V_{GS}}{V_P}\right)$$

$$I_D = I_{DSS} \left(1 - \frac{V_{GS}}{V_P}\right)^2$$

for the FET current source, when  $V_{GS} = 0 \Rightarrow I_D = I_{DSS}$

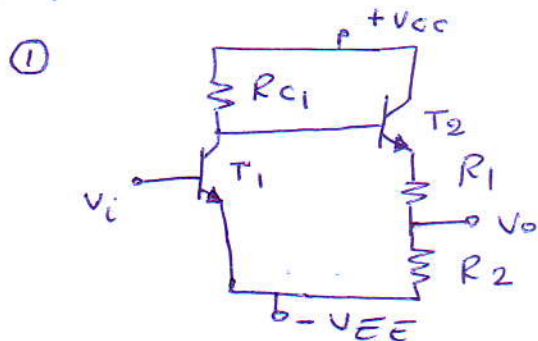
$$\therefore I_{D2} = \frac{I_{DSS}}{2}$$

$$\Rightarrow \frac{I_{DSS}}{2} = I_{DSS} \left(1 - \frac{V_{GS}}{V_P}\right)^2 \Rightarrow \frac{V_{GS}}{V_P} = 0.293$$

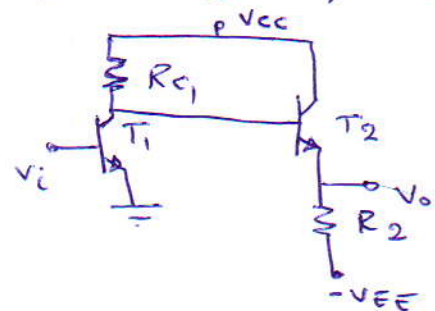
$$\therefore g_m = 10 \text{ m} (1 - 0.293) = 7.07 \text{ mS}$$

$$\therefore A_v = \frac{1}{2} (7.07 \text{ m}) (2.2 \text{ k}) = 7.7$$

Ex: For the circuits shown below, calculate the o/p impedance.



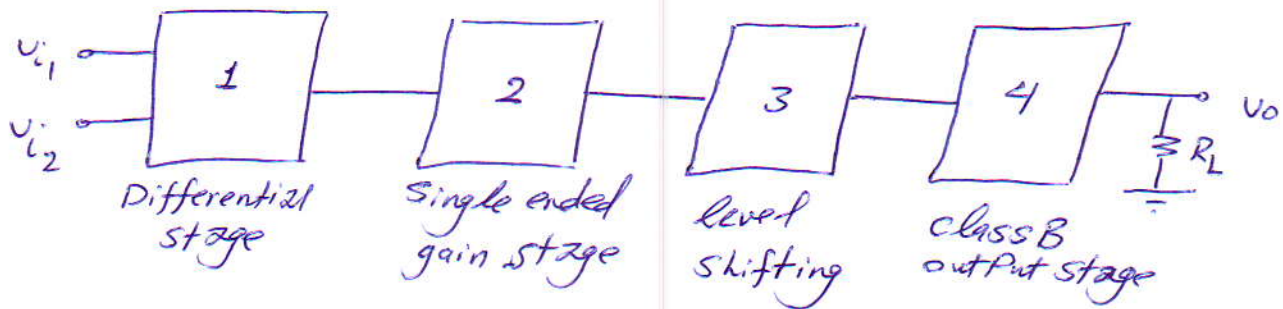
$$R_o = R_2 \parallel \left(R_1 + \frac{h_{ie2} + R_{c1}}{\beta_2}\right)$$



$$R_o = R_2 \parallel \left(\frac{h_{ie2} + R_{c1}}{\beta_2}\right)$$

## Operational Amplifier Schematic :

A simplified schematic of an complete op-Amp is shown in fig. below.



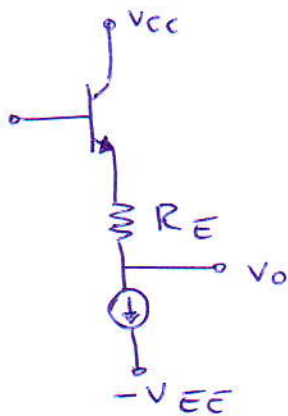
$$① A_{d1} = -\frac{R_c}{r_e}$$

\* المرحلة الأولى (Diff. stage) هي المكسب اما المرحلة الثانية

$$② A_{d2} = -\frac{R_c}{2r_e}$$

وهي زيادة المكسب كذلك وصعب القانون في الموضع ثانياً

### ③ D.C level shifting :



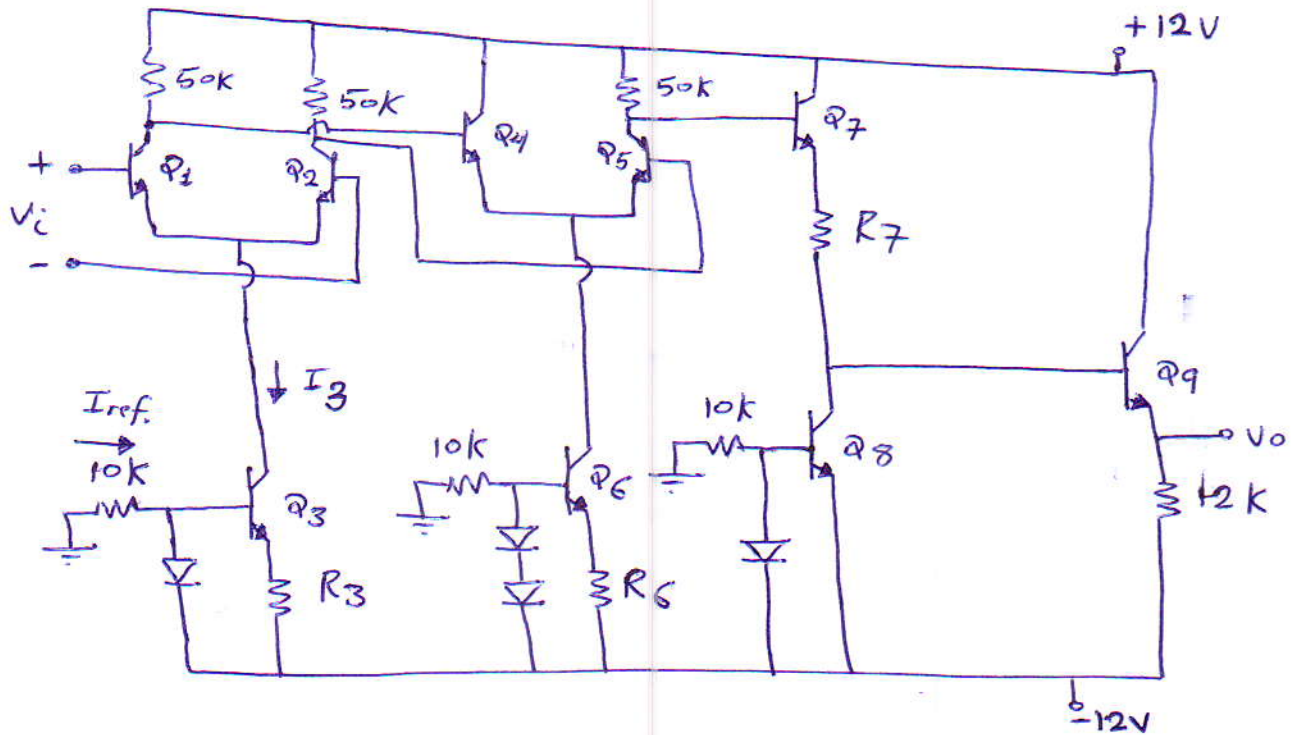
\* المرحلة الثالثة وظفتها هي لجعل D.C في الإدخال صحت  
ان المستوية صحت، لتصبح  $v_{in}$  ل  $I_C$  لذلك نلجأ إلى  
مرحلة ثالثة تقوم بقطع D.C وهي عبارة عن  
emitter follower trans. وهي تقوم بجعل D.C voltage  
من  $V_{CC}$  (+ve) في الإدخال إلى تقريباً  $-V_{EE} - (-V_{EE})$   
في الإخراج وبالتالي طرح القيمة وتكون النتيجة الإدخال  
تساوي  $v_{in}$  عند D.C وكانها صحت مربوطة قبل  $(v_o)$

### ④ class B output stage :

\* وهو عبارة عن مرحلة تسمح ان تكون مقارعة الإخراج قليلة وكذلك تكون دائرة سوق  
تيار (current driver) بحيث تعطي قيم تيارات عالية ويستخدم فيها مكبر من نوع  
class B power amplifier

Ex: For the circuit shown below calculate:

- ①  $R_3$  and  $R_6$  to obtain the current in  $Q_1$  and  $Q_2$  equal to  $100 \mu A$ .
- ②  $R_7$  to obtain the output voltage swing to zero.
- ③  $R_{in}$  and  $R_o$
- ④ Gain, if  $(\beta = 100)$ .
- ⑤ Is the level shifting stage prevents the D.C voltage in output?



Solution:

① 
$$I_{ref} = \frac{V_{EE} - V_{diode}}{R_x} = \frac{12 - 0.7}{10k} = 1.13 mA \quad \therefore I_1 \text{ and } I_2 \text{ are equal to } 100 \mu A$$

$$\Rightarrow I_3 = I_1 + I_2 = 200 \mu A$$

$$\therefore R_3 = \frac{KT}{I_3} \ln \left( \frac{I_{ref}}{I_3} \right) \quad \text{Widlar current source}$$

$$= \frac{25 mV}{200 \mu A} \ln \left( \frac{1.13 mA}{200 \mu A} \right) = 216.45 k\Omega$$

$$R_C = \frac{V_{diode} + V_{diode} - V_{BE}}{I} = \frac{0.7}{200\mu} = \boxed{3500\text{ k}\Omega}$$

(2)

$$R_7 = \frac{V_{CC} - 50\text{k} * I_5 - V_{BE7} - V_{BE9}}{I_{R7}} = \frac{12 - 50\text{k} * 100\mu - 0.7 - 0.7}{1.13\text{ mA}} = \boxed{4.95\text{ k}\Omega}$$

(3)

$$R_{in} = 2h_{ie} = 2\beta r_e = 2\beta * \frac{25\text{ mV}}{100\mu\text{A}} = \boxed{50\text{ k}\Omega} \text{ (high input impedance)}$$

$$R_o = 12\text{k} // \left( \frac{\frac{50\text{k} + h_{ie7}}{\beta_7} + R_7 + h_{ie9}}{\beta_9} \right)$$

$$h_{ie7} = \beta r_{e7} = 100 * \frac{25\text{ mV}}{1.13\text{ mA}} = \boxed{2.2\text{ k}\Omega}$$

$$h_{ie9} = \beta r_{e9} = 100 * \frac{25\text{ mV}}{I_{E9}} \quad I_{E9} = (V_0 + V_{EE}) / 12\text{k} = \frac{12\text{ V}}{12\text{ k}} = \boxed{1\text{ mA}}$$

$$\therefore h_{ie9} = \boxed{2.5\text{ k}\Omega} \Rightarrow R_o = \boxed{79\Omega} \text{ (low output impedance)}$$

(4)

$$A_{VT} = A_{V1} * A_{V2}$$

$$A_{V1} = -\frac{R_L}{r_{e2}} = -\left( \frac{50\text{k} // h_{ie4}}{r_{e2}} \right)$$

$$h_{ie4} = \beta r_{e4} = 100 * \frac{25\text{ mV}}{100\mu\text{A}} = \boxed{25\text{ k}\Omega}$$

$$\Rightarrow A_{V1} = \frac{-(50\text{k} // 25\text{k})}{250} = \boxed{-66.66} \quad r_{e2} = \frac{25\text{ mV}}{100\mu\text{A}} = \boxed{250\Omega}$$

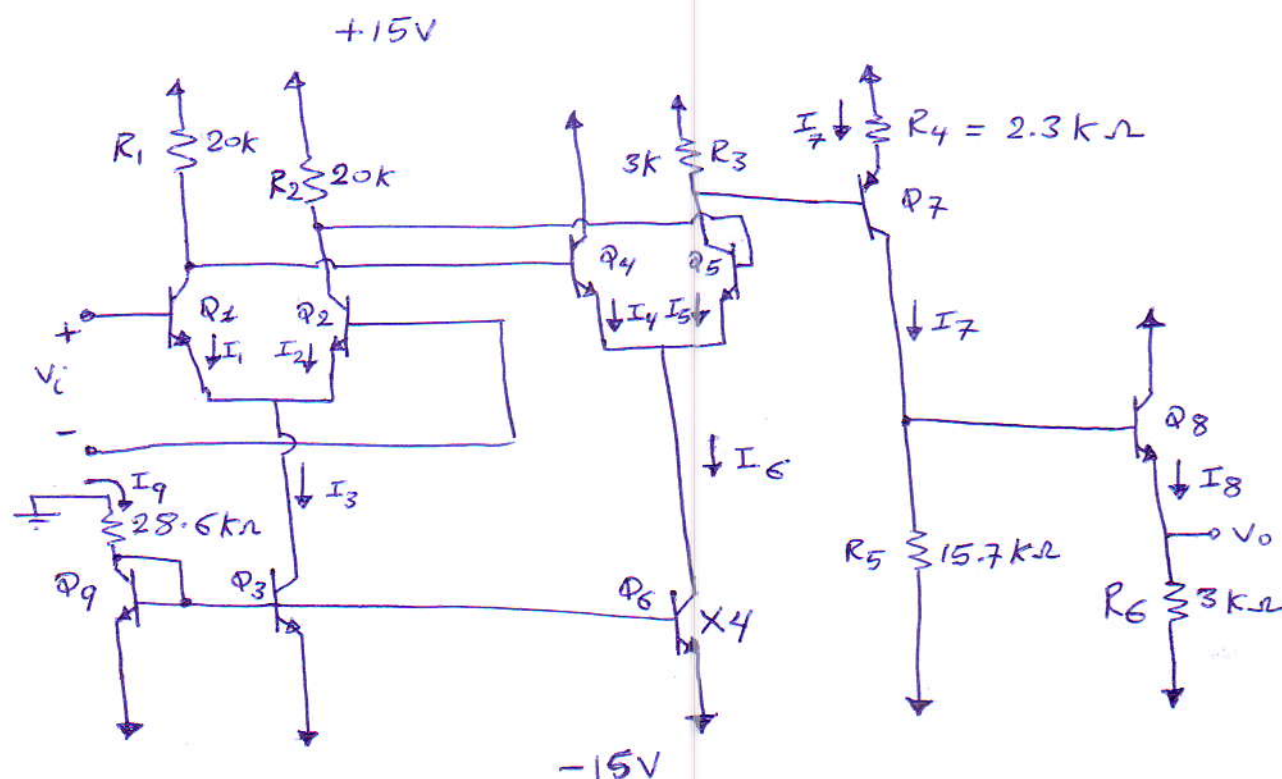
$$A_{V2} = -\frac{R_L}{2r_{e5}} = \frac{-50\text{k}}{2 * 250} = \boxed{-100}$$

$$A_{VT} = -66.66 * -100 = \boxed{6666.66}$$

(5) H.W.

Ex: For the circuit shown below, determine:

- ① The currents in all branches, if the emitter area of  $Q_6$  has four times the area of each of  $Q_4$  and  $Q_5$ .
- ② The Power dissipation in this circuit.
- ③ The input bias current of the op-amp, if all transistors have  $\beta = 100$ .
- ④  $R_{in}(diff)$  and  $R_o$ .
- ⑤ Is the level shifting stage Prevents D.C voltage in output
- ⑥ The voltage gain.



Solution:

$$① I_9 = \frac{15 - 0.7}{28.6k} = \boxed{0.5mA} = I_3 \text{ (Current mirror)}$$

$$I_6 = 4 * I_3 \text{ (four times of emitter area)}$$

$$\Rightarrow I_6 = 4 * 0.5mA = \boxed{2mA}$$

تسبغ

$$I_1 = I_2 = \frac{I_3}{2} = \frac{0.5 \text{ mA}}{2} = \boxed{0.25 \text{ mA}}$$

$$I_4 = I_5 = \frac{I_6}{2} = \frac{2 \text{ mA}}{2} = \boxed{1 \text{ mA}}$$

$$I_7 = I_{E7} = \frac{3 \text{ k} \Omega * 1 \text{ mA} - V_{BE7}}{R_4} = \frac{3 \text{ V} - 0.7}{2.3 \text{ k}} = \boxed{1 \text{ mA}}$$

$$I_8 = \frac{V_{EE} - V_{EE} - V_{BE8} + I_7 R_5}{3 \text{ k} \Omega} = \frac{1 \text{ mA} * 15.7 \text{ k} - 0.7}{3 \text{ k} \Omega} = \boxed{5 \text{ mA}}$$

②

$$P = IV$$

$$P_{\text{diss}} = I_{D.C} * V_{D.C}$$

$$P_{\text{diss (total)}} = P^- + P^+$$

$$P^- = (I_1 + I_2 + I_4 + I_5 + I_7 + I_8) V_{CC} \\ = (0.25 + 0.25 + 1 + 1 + 1 + 5) * 15 = \boxed{127.5 \text{ mW}}$$

$$P^+ = (I_3 + I_6 + I_7 + I_8) * V_{EE} \\ = (0.5 + 0.5 + 2 + 5) * 15 = \boxed{135 \text{ mW}}$$

$$P_{\text{diss or } P_D} = P^- + P^+ = 127.5 + 135 = \boxed{262.5 \text{ mW}}$$

$$③ I_{\text{bias}} = I_{B1} = I_{E1} / \beta + 1 = \frac{0.25 \text{ mA}}{101} \approx \boxed{2.5 \text{ } \mu\text{A}}$$

$$④ R_{\text{in(diff)}} = 2\beta r_e \quad r_e = \frac{25 \text{ mV}}{0.25 \text{ mA}} = \boxed{100 \text{ } \Omega}$$

$$\Rightarrow R_{\text{in(diff)}} = 2(100)(100) = \boxed{20 \text{ k} \Omega} \text{ high input impedance}$$

$$R_O = 3 \text{ k} \parallel \left( \frac{R_5 + h_{ie8}}{1 + \beta} \right) = 3 \text{ k} \parallel \left( \frac{15.7 \text{ k} + \left( \frac{25 \text{ mV}}{5 \text{ mA}} \right) (100)}{101} \right) = \boxed{152 \text{ } \Omega}$$

$$⑤ V_O = -V_{EE} + R_5 I_7 - 0.7 = -15 + (15.7 \text{ k})(1 \text{ mA}) - 0.7 = 0 \text{ V}$$

or

$$V_O = 3 \text{ k} * I_8 - V_{EE} = 3 \text{ k} * 5 \text{ mA} - 15 = 0 \text{ V}$$

Level Shifting Prevents the D.C voltage in o/p

$$⑥ \quad A_v = \frac{v_o}{v_{id}} = \frac{R_6 * i_{e8}}{R_{id} * i_i}$$

$$\frac{i_{e8}}{i_i} = \frac{i_{e8}}{i_{b8}} \cdot \frac{i_{b8}}{i_{c7}} \cdot \frac{i_{c7}}{i_{b7}} \cdot \frac{i_{b7}}{i_{e5}} \cdot \frac{i_{e5}}{i_{b5}} \cdot \frac{i_{b5}}{i_{c2}} \cdot \frac{i_{c2}}{i_i}$$

$$\frac{i_{e8}}{i_{b8}} = \beta + 1 = \boxed{101} ; \frac{i_{b8}}{i_{c7}} = \frac{R_5}{R_5 + Z_{b8}} = \frac{15.7k}{15.7k + (101)(3k) + \left(\frac{25m}{5m}\right)(100)}$$

$$\Rightarrow \frac{i_{b8}}{i_{c7}} = \boxed{0.049} ; \frac{i_{c7}}{i_{b7}} = \beta = \boxed{100} ; \frac{i_{b7}}{i_{e5}} = \frac{R_3}{R_3 + Z_{b7}}$$

$$\Rightarrow \frac{i_{b7}}{i_{e5}} = \frac{R_3}{R_3 + h_{ie7} + (1 + \beta)(R_4)} = \frac{3k}{3k + (100)\left(\frac{25mV}{1mA}\right) + (101)(2.3k)} = \boxed{0.0126}$$

$$\frac{i_{c5}}{i_{b5}} = \beta = \boxed{100} ; \frac{i_{b5}}{i_{c2}} = \frac{R_1 + R_2}{R_1 + R_2 + 2h_{ie(4,5)}}$$

$$\Rightarrow \frac{i_{b5}}{i_{c2}} = \frac{20k + 20k}{40k + 2(100)\left(\frac{25mV}{1mA}\right)} = \boxed{0.888}$$

$$\because i_{c2} \approx i_{e2} \quad \therefore \frac{i_{c2}}{i_i} = \beta = \boxed{100}$$

$$\Rightarrow \frac{i_{e8}}{i_i} = (101)(0.049)(100)(0.0126)(100)(0.888)(100) = \boxed{55373.4}$$

$$\Rightarrow A_v = \frac{3k}{20k} * 55373.4 = \boxed{8306 \text{ V/V}}$$

H.W:

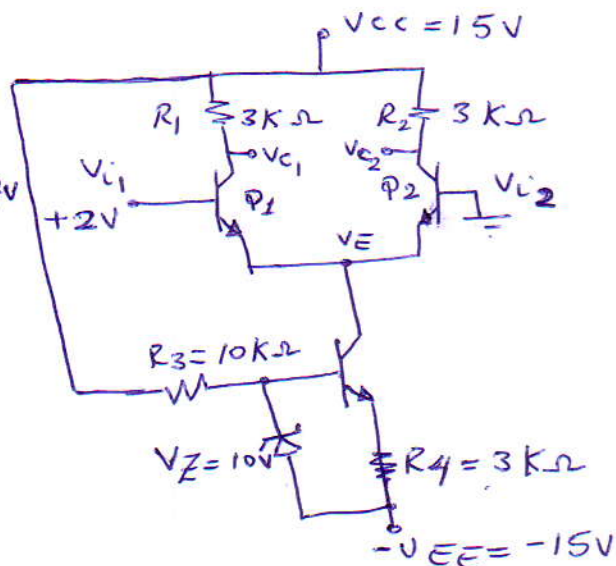
① for the circuit shown below, find

④  $V_{C1}$  and  $V_{C2}$  ? ⑥ If  $V_{i1} = 0V$  and  $V_{i2} = 5.7V$

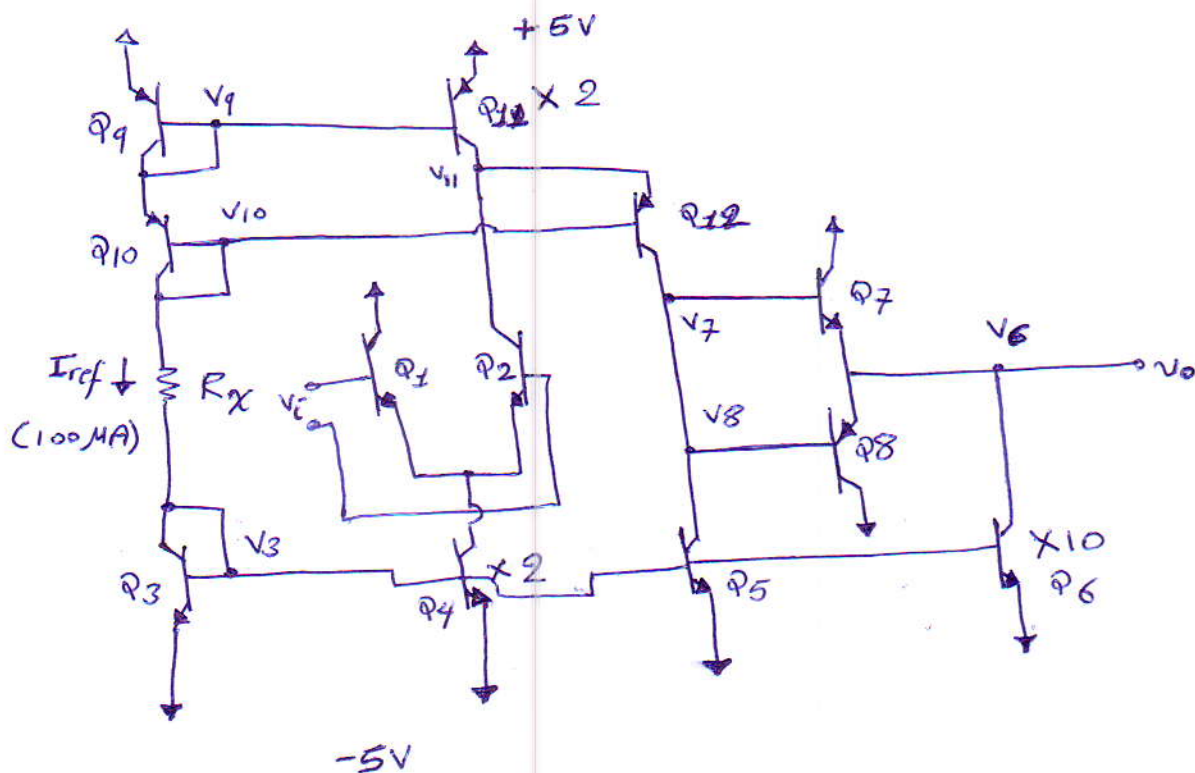
Repeat Part a ?

Ans: ④  $V_{C1} = 5.7V$ ;  $V_{C2} = 15V$

⑥  $V_{C1} = 15V$ ;  $V_{C2} = 5.7V$



② For the circuit shown below, find the voltages and currents in each branch as indicated on the circuit.



Ans:  $I_{ref} = I_3 = I_{10} = I_9$ ;  $I_4 = 200\mu A$ ,  $I_1 = I_2 = 100\mu A$ ;  $I_{11} = 200\mu A$

$I_{12} = I_5 = 100\mu A$ ,  $I_6 = 1\mu A$ ,  $I_8 = 0\mu A$ ,  $I_7 = I_6 = 1\mu A$

$Q_8$  (off);  $V_7 = V_8 = 0.7V$ ;  $V_{10} = 3.6V$ ;  $V_9 = 4.3V$ ;  $V_3 = -4.3V$

$V_{11} = 4.3V$ ;  $R = 79K\Omega$ ;  $V_6 = 0V$ .